

# Patient-specific B-cell lymphoma modeling identifies cooperating genetic alterations and the critical influence of patient context

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## 37 Abstract

38 Diffuse large B-cell lymphoma (DLBCL) is a molecularly heterogeneous disease with high  
39 genetic complexity and interpatient variability. Sequencing studies of representative  
40 patient cohorts have identified a comprehensive set of genetic driver alterations, enabling  
41 patient stratification for personalized treatment strategies. To date, it remains insufficiently  
42 understood how these oncogenic driver alterations operate in concert and shape  
43 malignant cell states. Here, we use a computational approach that embeds patient data  
44 and experimentally characterized molecular perturbations in mechanism-based  
45 mathematical modeling to study the effect of genetic alterations in a network context.  
46 Based on a detailed pathway model capturing key cellular processes, including apoptosis,  
47 cell division, and B-cell differentiation, we created personalized models for a cohort of 284  
48 patients, of which 90.5% reflect an aberrant cell state. Systematic assessment of the  
49 functional effects of individual and combinatorial alterations within these models identified  
50 previously not appreciated cooperating alterations that operate in synergy, such as  
51 mutated *NFKBIE* and *BCL6* structural variant. Notably, we identify a strong context  
52 dependency of functional effects, as identical alterations exert varying effects in different  
53 patient models. Incorporation of the network context is therefore essential for  
54 understanding DLBCL heterogeneity and selecting therapeutic targets for personalized  
55 and more efficient treatment strategies.

## 56 Introduction

57 Diffuse large B-cell lymphoma (DLBCL) is the most common Non-Hodgkin lymphoma,  
58 accounting globally for approximately 150 000 new cases each year<sup>1</sup>. The current first-  
59 line standard-of-care for DLBCL patients is an immunochemotherapy (R-CHOP-like),  
60 which leads to a cure in approximately two-thirds of the patients. A sizeable fraction of the  
61 remaining patients still succumb to their disease despite modern salvage strategies<sup>2</sup>.  
62 Molecularly, DLBCL is a heterogeneous disease, and these differences impact on biology  
63 and treatment (in)sensitivity, thereby affecting curability, disease progression, or relapse,  
64 and eventual death from the disease<sup>3-5</sup>.

65 To characterize the molecular heterogeneity and understand the impact of molecular-  
66 defined substructure to treatment response, DLBCL patient samples have been subjected  
67 to transcriptomic and genetic profiling<sup>6-15</sup>. Transcriptional stratification based on the  
68 putative cell-of-origin of the disease led to the identification of the activated B-cell (ABC)  
69 or germinal center-type B-cell (GCB) DLBCL subtypes<sup>6</sup>. Accordingly, GCB DLBCL exhibit  
70 high expression of germinal center markers, *e.g.* *BCL6*, and frequently harbor genetic  
71 alterations such as *EZH2* mutations, or *BCL2* and *MYC* translocations. ABC DLBCL  
72 originate from post-germinal center B-cells, frequently exhibits *MYD88* and *CD79*  
73 mutations, and are characterized by chronic-active B-cell receptor and associated NF- $\kappa$ B  
74 pathway signaling<sup>16</sup>.

75 Genetically, DLBCL is characterized by a considerable interindividual heterogeneity due  
76 to the variety, number, and composition of altered genes as well as the type of those  
77 alterations, comprising somatic mutations, copy number (CN) aberrations (CNAs) and  
78 structural variants (SVs). Sequencing of large DLBCL patient cohorts facilitated the

79 identification of driver alterations and cosegregated genetic signatures<sup>6-15</sup>. Among the  
80 identified genetically perturbed genes are regulators of NF- $\kappa$ B activity such as *NFKBIA*  
81 ( $\text{I}\kappa\text{B}\alpha$ ) or *TNFAIP3* (A20), but also well-known oncogenes and tumor suppressors,  
82 including *MYC*, *TP53*, *BCL6* and *PTEN*.

83 The centrality of the NF- $\kappa$ B pathway in DLBCL biology is due to its involvement in the  
84 regulation of critical cellular functions, including life-death cell fate decisions, cell-cycle  
85 control and B-cell differentiation. Of note, NF- $\kappa$ B is a family of transcription factors  
86 consisting of RELA, CREL, RELB, p105/p50 (NFKB1) and p100/p52 (NFKB2) that induce  
87 the expression of a multitude of target genes, e.g. cyclin D1, D2, D3, anti-apoptotic factors  
88 BCL2 and BCL-XL, as well as the transcription factor BLIMP1. Moreover, NF- $\kappa$ B mediates  
89 the expression of its own direct and indirect inhibitors, namely  $\text{I}\kappa\text{B}$ s and *TNFAIP3* (A20),  
90 and drives expression of many cytokines and chemokines.

91 To stratify patients based on their genetic signatures, classifiers have been developed  
92 (DLBclass and Lymphgen)<sup>13,17,18</sup>, enabling a better biological subgrouping and more  
93 detailed stratification of patients regarding treatment options and prediction of expected  
94 outcomes. In parallel, computational disease models have been developed to predict  
95 responses and to improve patient stratification of DLBCL patients<sup>19-23</sup> (recently reviewed  
96 in detail<sup>24</sup>). Among those approaches, mechanistic mathematical models have been used  
97 to study patient data by creating patient-specific models. In earlier work, we developed  
98 logical models to assess the effect of genetic alterations, single inhibitors, and inhibitor  
99 combinations in a patient-specific manner<sup>20</sup>. These models allowed to characterize  
100 patients based on the impact of the respective inhibitors on the individual NF- $\kappa$ B signaling

101 activity. In an alternative published patient-specific model, patients are stratified based on  
102 defined signaling patterns of the model<sup>21</sup>.

103 These approaches enable predictive insights into stratification and treatment responses,  
104 but systematic modeling of individual and cosegregated genetic alterations and their  
105 functional relationships in patient contexts is missing. The crucial role of functional  
106 relationships between alterations has been demonstrated in molecular studies, *e.g.* for  
107 the anti-apoptotic factor BCL2. While a delay or abrogation of apoptosis induction is  
108 associated with cancer<sup>25</sup>, an overexpression of BCL2 in mice, cell lines and human  
109 primary cells is not sufficient to cause malignant transformations or tumor  
110 development<sup>26,27</sup>. However, the combination with increased expression of the  
111 proliferation-promoting oncogene *MYC* results in a synergistic effect, causing strongly  
112 increased proliferation and the development of tumors<sup>28</sup>. This combination is known as  
113 double hit lymphoma and is associated with poor outcomes in patients<sup>16</sup>. Alterations of  
114 other drivers, including *MYC*, *CCND3*, *BCL6* and *TP53* were alone also insufficient to  
115 cause a strong cellular expansion of primary B-cells<sup>27</sup>. While combinations of BCL2 and  
116 *MYC* overexpression, or BCL2 and BCL6 overexpression, strongly prolonged primary B-  
117 cell survival, in immunodeficient mice, four of the five alterations are required for *in vivo*  
118 tumor formation<sup>27</sup>. These results strongly emphasize the importance to understand  
119 mutual effects of alterations and assessing the combined effect of patient-specific  
120 compositions of alterations.

121 We therefore employed here a computational approach that combines detailed  
122 mechanistic network modeling with patient cohort data and experimentally characterized  
123 functional effects of alterations to study the effect of genetic alterations in a network

124 context. The combined analysis of alteration insertions and drop out simulations in  
125 patient-specific models reveals previously unrecognized synergistic interactions and  
126 highlights the strong context dependency created by each individualized alteration  
127 signature.

## 128 Results

### 129 Constructing patient-specific models

130 To assess the impact of all genetic alterations in DLBCL patients on signaling network  
131 dynamics and their contribution to putative cancerous cell states, we first created a  
132 reference model and thereafter patient-specific models. We chose as a basis the model  
133 of Roy *et al.*<sup>29</sup>, in which crucial cellular functions, including apoptosis, cell division and B-  
134 cell differentiation, are described and which allows us to analyze the derived state of a  
135 cell. To enable efficient simulations and capture additional regulatory processes that play  
136 an important role in DLBCL, we substantially refined and expanded the model (Fig. 1A  
137 and Methods, Construction of the reference model). We visualized the complex  
138 underlying network of our reference model, representing a wild-type (WT) activated B-  
139 cell, in an automated way (Fig. 1A, Methods, Model visualization), highlighting the model  
140 wiring of important network components, their interconnection, and distinct subnetworks  
141 (Fig. 1B).

142 To investigate the heterogeneity of patients based on their individual composition of  
143 alterations, we created patient-specific models based on our reference model. We  
144 therefore captured key alterations that were directly or indirectly implemented into the  
145 reference model. From a recently published cohort consisting of 304 DLBCL patients<sup>13</sup>,  
146 we incorporated the molecular profiles at the timepoint of diagnosis of 284 patients based  
147 on mutations, CNAs and SVs of genes that could be mapped to components of the  
148 network model (for details, see Methods, Implementation of genetic alterations). The  
149 remaining patients did not show significant alterations that could be linked to our model  
150 components. Regarding the mutations, we distinguished between loss-of-function (LOF)

151 mutations, activating or inactivating mutations, and gain-of-function (GOF) mutations. In  
152 total, we were able to map 105 distinct alterations from the patient cohort onto our  
153 reference model. The implementation of the functional effects of 104 alterations (Table 1)  
154 was achieved by using the databases cBioPortal<sup>30–32</sup> and oncoKB<sup>33,34</sup>. Moreover, we  
155 performed a thorough literature search to collect information about functional effects of  
156 relevant mutations (Table S1). Among those is also the formation of the My-T-BCR super-  
157 complex in the presence of *MYD88* and *CD79B* mutations that accounts for chronic NF-  
158  $\kappa$ B and PI3K activity<sup>35</sup>. To incorporate the quantitative impact of the alterations, we defined  
159 perturbation strengths based on accessible quantitative data and sensitivity analyses  
160 (Fig. 1A). By combining patient-individual compositions of all implemented alterations, we  
161 successfully created 284 patient models capturing in total 638 mutations, 1778 CN gains,  
162 539 CN losses and 142 SVs (Fig. S1, Table 1). The number and type of alterations differed  
163 substantially among patients, ranging from 1 to 33 alterations per case implemented into  
164 the model (Fig. 1C). Simulating all patient models revealed diverse dynamics of key  
165 components (Fig. 1D), reflecting the heterogeneity of the patients (Fig. S1).

## 166 Patient models reflect aberrant cellular states

167 We first investigated whether the implemented patient-specific genetic signatures cause  
168 an aberrant cellular state for each patient model. Aberrant cell states differ from the  
169 reference cell state in terms of proliferation and/or cellular survival and contribute to the  
170 malignant transformation and eventual tumor formation in the patient. As we incorporated  
171 the patient-specific genetic signature into the patient models, we therefore simulated the  
172 network dynamics and estimated the timepoint of apoptosis and the division rate of each  
173 model (see Methods, Creating and simulating patient models).

174 The combination of both readouts, the apoptosis timepoint and the division rate define  
175 the cell state. Based on the physiological state of the reference model (Fig. 2, empty  
176 square), the division rate of the WT state is extrapolated for all time points of apoptosis  
177 (Fig. 2, dotted line). Importantly, from the 284 patient models developed, 257 (90.5%)  
178 show an aberrant state (Fig. 2). This data demonstrates that the specific combination of  
179 alterations present in a given patient model promote for the vast majority an aberrant  
180 state. The patient models in this state can be divided into two groups. While the  
181 proliferation rate is increased in both groups compared to the reference model, apoptosis  
182 is either entirely suppressed or is still induced - earlier or later than in the reference model.  
183 There are 27 models (9.5%) showing a “physiological state”.

184 The extensive coverage of aberrant states in the patient models provides a valuable  
185 baseline for dissecting the impact of individual and combined alterations as well as their  
186 functional interdependencies within patient-specific network contexts.

187

## 188 Individual alteration effects explain only a limited number of 189 aberrant states

190 To investigate the effect of individual alterations on the cell state, we used the reference  
191 model to simulate each alteration that is found in the patients and quantified the change  
192 in the timepoint of apoptosis and the division rate (Fig. 3A). From the 104 alterations, 42  
193 (40.4%) have the potential to individually promote an aberrant state (Table S2). These 42  
194 alterations correspond to 21 genes (45.7%). The strongest effects are observed for  
195 *TNFAIP3* mutations, SVs of *MYC* and the LOF mutation of *NFKBIA*. All these alterations  
196 strongly increase the division rate and, except for *MYC*, also prevent apoptosis induction

197 during the simulation time. The analysis reveals that specific alterations affecting the cell  
198 division directly or indirectly via the regulation of NF- $\kappa$ B are sufficient to promote an  
199 aberrant state. This is in line with the known tumor suppressor roles of *TNFAIP3* and  
200 *NFKBIA*, as their LOF mutations can cause constitutive NF- $\kappa$ B activity and thereby  
201 promote an aberrant cell state<sup>36–41</sup>.

202 In patients with DLBCL, genetic alterations usually occur not in isolation but as co-  
203 segregated genetic signatures<sup>12,13</sup>. Moreover, certain genetic alterations cooperate  
204 functionally and prominent examples include the synergy of *BCL2* SV and *MYC* SV (also  
205 known as double hit lymphoma)<sup>26,27,42</sup>.

206 Wet laboratory testing of all possible combinatorial effects of alterations is currently not  
207 feasible. To this end, we performed a systematic analysis of alteration effects by  
208 simulating the model, including all possible combinations of the 104 alterations. The  
209 simulation results show that 3,113 out of 5,356 pairs (58.1%) promote an aberrant state  
210 (Fig. 3B). From these 3,113 pairs, 27.7% are pairs in which both alterations already  
211 individually promote an aberrant state, while 71.6% contain one such alteration (Table 2).  
212 Interestingly, there are 22 pairs (0.7%) for which only their combined effect causes an  
213 aberrant state, but none of the individual perturbations. In contrast, from the 3,465 pairs  
214 containing at least one alteration causing an aberrant state, 11% show a WT-like state.  
215 Interestingly, this reveals the possibility of neutralizing and compensatory effects between  
216 alterations.

## 217 Identification of synergistic interaction effects

218 To compare the effect of individual and cosegregated alteration pairs, we defined a metric  
219 that captures the malignancy potential of alterations and computed it for all single

220 alterations and all pairs. This ‘malignancy score’ captures the shortest distance between  
221 the alteration-promoted state and the reference state, which we define here as the WT  
222 state (Fig. S2 and for details, see Methods, Defining a malignancy score to quantify effect  
223 sizes of alterations). A positive score indicates changes towards aberrant states, while  
224 negative scores cover physiological states. To assess whether the scores of alteration  
225 pairs reflect purely additive effects of the corresponding individual alterations, we  
226 computed an expected score for each alteration pair capturing the additive contribution  
227 alone. This is compared to the calculated true malignancy score (Fig. 4A).

228 The comparison of the true and expected scores reveals that 64% of all alteration pairs  
229 show a simple additive effect, *i.e.* the true value corresponds to the expected value.  
230 However, there are pairs with strong deviations between both values. We were most  
231 interested to identify those cases in which the combined effect causes an aberrant state  
232 while a physiological state was expected from the individual effects alone (true score > 0,  
233 expected score  $\leq$  0) or the aberrant state is more severe than expected (true score >  
234 expected score), (light orange and light red regions, respectively, Fig. 4A). The  
235 physiological-vs-aberrant region (light orange) contains the 22 pairs which only in  
236 combination, but not individually, promote an aberrant state (Table 2). Most of these pairs  
237 contain alterations affecting BCR signaling and mutations of *NFKBIE*. Interestingly, the  
238 detected combination *CARD11* mutation & *NFKBIE* mutation is also found in two patients  
239 (*CARD11* & *NFKBIE*, Fig. 4A).

240 We detected 372 pairs that promote an aberrant state stronger than expected (Fig. 4A,  
241 light red region). Notably, among the identified alteration pairs are the *BCL2* SV and *MYC*  
242 SV, which are known for their synergistic effect<sup>28</sup>. Interestingly, we find similar

243 discrepancies between scores for combinations of *MYC* SV and mutations of either *FAS*,  
244 *KMT2D*, *TP53*, or *MYD88*. The mutations cause, such as the *BCL2* SV, a cooperative  
245 effect by delaying or abrogating apoptosis and thereby potentiating the pro-proliferative  
246 *MYC* SV effect (Table 3). These additional *MYC* SV pairs are also found in the patient  
247 cohort (Table 3), supporting their contribution to the aberrant state in the patient context.

248 Pairs with even stronger cooperative effects are combinations in which the level of active  
249 BLIMP1 is affected, for example, by a LOF *PRDM1* mutation (the locus encoding BLIMP1)  
250 or *BCL6* translocation, together with a LOF mutation of *NFKBIE*. Intriguingly, their  
251 combined effect causes a synergy with a strongly enhanced proliferation and prolonged  
252 cellular survival (Fig. 4B). A list of alterations affecting the level of active BLIMP1 and  
253 therefore forming a synergy with *NFKBIE* mutations is given in table S3.

254 We checked if such a combination of mutated *NFKBIE* and alterations affecting BLIMP1  
255 is present in patient models and found ten patients in which *NFKBIE* is mutated. Six of  
256 them harbor an additional alteration such as *BCL6* SV, *CARD11* mutation or *EZH2*  
257 amplification that alone can cause a reduction in the level of BLIMP1 (Fig. S4B). In four  
258 patients, *BCL6* SV is present, including one patient in which only three alterations are  
259 present in the corresponding individual model: *BCL6* SV, *NFKBIE* mutation, and *CCND3*  
260 CN gain. Five out of the six patient models show indeed strongly increased levels of  
261 nuclear cREL:P50 and RELA:P50 (Fig. S4B), a dynamic pattern that was also observed  
262 in the corresponding alteration pair simulations (Fig. 4B and S4A).

263 In the broader signaling pathway context, this synergy indicates that alterations promoting  
264 both, the inactivation of BLIMP1 and activation of NF- $\kappa$ B synergize. This finding is further  
265 corroborated experimentally by two studies in mice, already reporting a strong

266 cooperative effect between constitutive active NF- $\kappa$ B and dysfunctional BLIMP1 with  
267 respect to increased cell numbers and shortened lifetime of mice<sup>43,44</sup>. We therefore  
268 analyzed if other alterations than *NFKBIE* mutations show a cooperative effect with *BCL6*  
269 SV alterations or *PRDM1* mutations. Interestingly, we find, although with a less  
270 pronounced effect compared to *BCL6* SV & *NFKBIE* mutation, alterations of *TNFAIP3*  
271 and *MYD88* causing a synergistic effect with *BCL6* and *PRDM1* alterations (Table 4).  
272 Strikingly, among those alteration pairs, *TNFAIP3* CN loss in combination with *PRDM1*  
273 CN loss are found in 91 patients (Table 4).

274 This demonstrates, that our identified synergistic effects might also be relevant for the  
275 cellular aberrant state in patient models. The results give a mechanistic insight how  
276 mutant *NFKBIE*, which was reported as driver in DLBCL<sup>11,13</sup>, cooperates with other  
277 alterations and allows to resolve how alterations in the NF- $\kappa$ B regulation cooperate with  
278 alterations affecting BLIMP1. Still, since we focused here on alteration pairs, the presence  
279 of additional alterations in the patient models opens the possibility of their interference  
280 with the synergistic effect, inducing variability in the models and affecting the aberrant  
281 state. This is exemplified by one patient model, that does not show strongly increased  
282 levels of cREL:P50 and RELA:P50 despite the *NFKBIE* mutation and the *BCL6* SV. This  
283 highlights the requirement for context-specific analyses of alteration effects.

284

## 285 **Alterations causing the aberrant state are patient-specific**

286 To comprehensively assess the impact of alterations in a patient-specific context, we used  
287 the personalized models, including all perturbations per patient and performed a drop out  
288 analysis in which we initially removed each alteration individually and then all possible

289 combinations of alteration pairs, triplets and quadruplets. This allowed the identification  
290 of alteration drop outs restoring the physiological state (Methods, Defining a malignancy  
291 score to quantify effect sizes of alterations). The identified alterations represent in each  
292 patient model a specific minimal genetic signature that causes the aberrant state. This  
293 way, we identified 54 patient models with single causative alterations (Fig. 5A). For other  
294 patient models, two (57 patients), three (55 patients) or four alterations (36 patients) have  
295 to be taken out simultaneously to reverse the aberrant state (Fig. 5A). Strikingly, for 55  
296 patient models removing all possible combinations of four alterations was not sufficient to  
297 reverse the aberrant state, revealing a very robust composition of alterations.

298 In the 202 patient models, where causative alterations were identified that way, we found  
299 overall 32 out of the 47 implemented genes including the MYD88-CD79B supercomplex  
300 to promote, upon alteration, an aberrant state (Fig. 5B). In our previous analysis,  
301 alterations in 21 genes were sufficient to individually promote an aberrant state in the  
302 reference model (Fig. 3A). Nineteen of those genes overlap with the 32 genes identified  
303 here by the drop out analysis as causative. Intriguingly, alterations in the remaining 13  
304 genes are causative in the patient models but do not induce an aberrant cell state when  
305 introduced into the WT model. These results show that the patient-specific signature  
306 strongly modulates the functional impact of genetic alterations.

307 Among the most frequent alterations that individually cause the aberrant state are  
308 *TNFAIP3*, *EZH2*, *BCL6* as well as *MYC* (Fig. 5B), which are well-known cancer drivers in  
309 DLBCL (Fig. S5). In some patient models, different individual drop outs have the potential  
310 to restore the physiological state, for example patient index 20 (Fig. 5B). In other patient  
311 models, those cancer drivers alone are not sufficient to restore a physiological state, but

312 require the drop out of additional alterations. This is evident from the fact that alterations  
313 of these genes are very frequently found in combinations with two or more alterations.  
314 Interestingly, there are alterations which only cause an aberrant state in combination with  
315 other alterations. For example, *MYD88* alterations are frequently found in combinations  
316 consisting of at least two alterations (Fig. 5B, e.g. patient index 64, 80 and 140),  
317 demonstrating that causative alteration combinations are variable in different patient  
318 models.

319 For the most frequent causative alterations comprising *TNFAIP3*, *EZH2* and *BCL6*, the  
320 analysis shows that they are also found in combination with each other in some of the  
321 patients (Fig. 5B, e.g. patient index 56 and 116). Of note, the pairs we identified in our  
322 previous analysis showing a synergistic effect between dysfunctional BLIMP1 and NF-κB  
323 regulation are found here responsible for the aberrant state of the patient models. Beside  
324 the drop outs of the pairs *BCL6* SV - *NFKBIE* mutation and *MYD88* - *PRDM1* mutation,  
325 that of *PRDM1* deletion - *TNFAIP3* deletion also restore the physiological state. The latter  
326 pair is also involved in causative drop outs of three and four alterations and occurs in 24  
327 patient models. Additionally, in 6 patient models, the pair is present and due to the  
328 synergy, the drop out of either *TNFAIP3* deletion or *PRDM1* deletion is sufficient to restore  
329 the physiological state.

330 Finally, we summarized how often identified genetic alterations occur as causative  
331 alterations in the drop out analysis of 1 to 4 alterations (Fig. 5C, red bars). The most  
332 prominent genes, *TNFAIP3*, *EZH2* and *BCL6* show frequent alterations in the patient  
333 cohort (between 100 and 150 patients) and are frequently part of the causative  
334 alterations. Interestingly, alterations of *MYC* and *NFKBIA* are less frequent in the cohort,

335 but are often identified as causative alterations for the altered cell state. In contrast, while  
336 *BCL2* is the most frequently altered gene in this patient model cohort, we only find it in  
337 very few cases to be the causative alteration. Such a low frequency is also true for *TP53*,  
338 *FAS* and *NFKBIE*. These results show that alterations that occur with high frequency not  
339 necessarily drive the aberrant state in patient models, and low frequent gene alterations  
340 can be causative. Intriguingly, the overall alteration signature of a patient model creates  
341 the context, enabling alteration interaction effects and therefore dictates the role of  
342 individual alterations.

343

## 344 Discussion

345 In this mathematical modeling approach, we integrated the genetic alterations of DLBCL  
346 patients into mechanism-based network modeling to infer the impact and mutual effects  
347 of highly heterogeneous alterations in patient-specific contexts. The use of recent cohort  
348 data to establish 284 patient models enabled us to dissect the effects of these alterations  
349 in a personalized manner, identifying established genetic drivers and predicting so far  
350 unknown combinatorial effects with a strong cancer-promoting potential.

351 While the effects of genetic alterations have been modeled before<sup>20,21</sup>, a detailed  
352 mechanistic analysis and understanding of combinatorial effects on the cell fate within  
353 individual patients is not covered. We addressed this here by a thorough analysis of  
354 individual and combinatorial alteration effects. Our study expands both the considered  
355 alteration types and the range of effect sizes exceeding previous approaches. We here

356 implemented CNAs, SVs, and mutations separated in LOF, modified activity and GOF  
357 mutations. For *CCND3* and *TP53* mutations, we were able to integrate quantitative data  
358 capturing the effect of the mutations on the degradation rate of *CCND3* and the  
359 transcription rate of the p53 target gene *BAX* (Table S1 and Schmitz *et al.*<sup>45</sup>, Kato *et al.*<sup>46</sup>).  
360 With this approach, we substantially expanded the coverage of distinct alterations  
361 captured in mathematical models. From the 127 high-confidence driver genes, defined by  
362 Coyle *et al.*<sup>47</sup>, 23 are included in our model. Drivers that are found by Coyle *et al.* in all  
363 twelve considered studies are *CREBBP*, *MYD88*, *EZH2*, *CD79B*, and *TP53*, all of which  
364 are not only included in our model but were also identified here as cancer-causing genes  
365 (Fig. 5). By implementing more alterations, we were able to cover 284 patients of the 304  
366 patients of a recent study<sup>13</sup>, which corresponds to 93.4%. The 284 models cover all  
367 DLBc/class-identified DLBCL subtypes<sup>17</sup>.

368 Our analysis of alteration effects is based on a malignancy score derived from model  
369 readouts for apoptosis and proliferation, which allows to distinguish between aberrant and  
370 physiological cell states. This score reflects important experimental observations. Caesar  
371 *et al.*<sup>27</sup> experimentally tested the effects of *MYC*, *CCND3*, *BCL6* and a non-functional  
372 variant of *TP53* in addition to the effect of *BCL2* overexpression, demonstrating that none  
373 of those alterations caused a strong increase in cell viability<sup>27</sup>. For *BCL2*, *CCND3* and  
374 *TP53*, these results are fully in line with our model, which predicts a score of zero for  
375 these cases. However, *MYC* overexpression in primary GC B-cells cause a reduced cell  
376 viability, whereas our model predicts a positive score and increased proliferation but does  
377 not capture the pro-apoptotic effect<sup>27</sup>. This is likely due to the multiple effects exerted by  
378 *MYC* including the promotion of apoptosis, global protein synthesis causing proteotoxic

379 stress<sup>48</sup>, and activation of p53 by triggering the DNA damage response<sup>49</sup> which are  
380 currently not captured by our model. Future model extensions incorporating DNA damage  
381 response<sup>50</sup> and more comprehensive p53 signaling<sup>51,52</sup> will not only allow for a refinement  
382 of the impact of dysfunctional p53 on the DNA damage response and the aberrant cell  
383 state, but also facilitate simulation of chemotherapeutic-based treatment responses.  
384 Additionally, integrating the DNA damage-induced activation of the NF-κB pathway would  
385 be important to capture the balance between pro- and anti-apoptotic signals upon DNA  
386 damage<sup>53,54</sup>.

387 To untangle the complexity of alteration combinations, we here performed simulations of  
388 more than 500.000 alteration combinations. This analysis prioritizes and short lists now  
389 putative oncogenic and synergistic combinations that should be explored functionally in  
390 the wet laboratory. For instance, one prediction of a striking synergy is the *NFKBIE*  
391 mutation in combination with a second alteration affecting BLIMP1 levels. Interestingly,  
392 LOF mutations of *NFKBIE* are markers for Aggressive Chronic Lymphocytic Leukemia  
393 and for poor prognosis in Primary Mediastinal B-cell Lymphoma<sup>55,56</sup>. Moreover, in six out  
394 of the twelve studies analyzed by Coyle *et al.*, *NFKBIE* was identified as a cancer driver  
395 and is defined as a tier 1 driver<sup>47</sup>. As detailed above, constitutive activation of NF-κB  
396 synergizes in mouse models with the deletion of BLIMP1<sup>43,44</sup>, and we find this alteration  
397 pair also in our model simulations, suggesting that these alterations promote NF-κB  
398 signaling and enhance the effect of dysfunctional BLIMP1 in a non-additive way. Such a  
399 cooperative effect is also supported by *ex vivo* culture of human primary GC B-cells  
400 overexpressing *BCL2* and *BCL6*, followed by a CRISPR knockout screen of almost 700  
401 genes. Strikingly, *NFKBIE* has the twelfth highest CRISPR gene score<sup>27</sup>. As *BCL6*

402 overexpression downregulates BLIMP1 due to transcriptional repression<sup>57</sup>, those results  
403 show the critical role of dysfunctional *NFKB1E* in this alteration context.

404 Our approach and findings distilled thereby have important clinical implications. While  
405 DLBCL-treating lymphoma specialists are well aware of the highly variable outcomes their  
406 patients achieve, and see this diversity linked to the underlying molecular heterogeneity  
407 of the disease, systematic interrogations of the functional cooperativity between key  
408 genetic aberrations and their impact on individual patients' long-term responses are  
409 largely missing., Mathematical network modeling allows to link basal cellular growth  
410 properties and major recurrent driver mutations and thereby enabled us to derive here  
411 various cell states that reflect specific functional properties and dependencies. We  
412 identified those dependencies in a personalized manner and mechanistically resolved  
413 their functional effects. While our framework recapitulates the well-established synergistic  
414 effect of the BCL2-MYC double hit lymphomas, the approach also predicts multiple  
415 additional candidates of synergistic hit combinations observed in patients of the cohort.  
416 These insights will facilitate the prioritization of genetic alterations that might synergize  
417 functionally for wet laboratory validation and eventually enhance the molecular  
418 understanding of genetically defined patient subtypes.

419 Overall our results highlight the critical impact of integrating patient-specific alteration data  
420 and mechanism-derived network models capturing nonlinear effects for the prediction of  
421 functional alteration effects, demonstrating the necessity of personalized computational  
422 modeling for the reliable prediction of targeted therapeutic strategies in DLBCL.

423

## 424 Methods

### 425 1. Construction of the reference model

426 Based on the goal to implement many genetic alterations and comprehensively test their  
427 individual and combinatorial effects, efficient model simulations are required. In order to  
428 reduce the computational costs, we transformed the population model of Roy *et al.*<sup>29</sup> into  
429 a single reference model that allows to simulate the processes of a representative WT B-  
430 cell. We first simulated a population of 500 cells without additional sampling of parameters  
431 for daughter cells and then selected a representative cell based on the following criteria:  
432 the cell i) differentiates into a plasma cell, ii) differentiates at a later timepoint than 24  
433 hours and iii) undergoes apoptosis in a time frame of 2 to 6 days.

434 To further increase the efficiency of model simulations, we replaced the delay differential  
435 equations (DDEs) describing the delayed transcription of *REL*, *NFKBIE* and *NFKB1* (P50)  
436 by ordinary differential equations (ODEs). To preserve the dynamics, we applied the linear  
437 chain trick<sup>58</sup> by adding a chain of intermediate components and reactions representing  
438 the process of transcription. To estimate the parameter values of these reactions, we  
439 trained the ODE model on simulated time course data (0 to 240 minutes) of *REL*, *NFKBIE*  
440 and *NFKB1* from the DDE model. For simulations and optimization, the tools AMICI<sup>59</sup> and  
441 PESTO<sup>60</sup> for MATLAB (R2023b, The Mathworks Inc., Natick, MA) and pyPESTO<sup>61</sup> for  
442 Python (version 3.12, Python Software Foundation, <https://www.python.org/>) were used.  
443 As the chain length can be variable, we trained the model on different chain lengths (1,  
444 2, 3, 5). Using the corrected Akaike Information Criterion<sup>62,63</sup>, we identified an optimal  
445 length of one and replaced the DDEs by one intermediate step (Text S1, eq. 1.16 and eq.  
446 1.141, eq. 1.7 and eq. 1.139, eq. 1.13 and eq. 1.40). Additionally, we adapted the originally

447 discontinuous piecewise differential equation describing the transcription of *BCL2* by  
448 removing the conditional rule for a threshold for the RELA:P50 and cREL:p50-promoted  
449 *BCL2* transcription (eq. 1.114 and 2.4). This was necessary to enable a continuous effect  
450 of our implemented genetic alterations on *BCL2* expression and it allows for more stable  
451 simulations.

452 In the original model (Roy *et al.*<sup>29</sup>) two inputs initiate signal transduction. Both inputs are  
453 not implemented as ODEs but as hard-coded time course data. To include genetic  
454 alterations that affect upstream processes of the inputs as well as alterations directly  
455 affecting the regulation of the input components, we replaced the two inputs by ODEs.  
456 For the pIKK regulation, we included the negative regulator of NF- $\kappa$ B activity TNFAIP3  
457 (A20) based on the model of Mothes *et al.*<sup>64</sup> (Text S1, eq. 1.142, eq. 143, eq. 144).  
458 Importantly, by including *TNFAIP3*, we capture a frequently altered gene in DLBCL  
459 patients (Fig. S1, 43% of patient samples contain a *TNFAIP3* alteration). For the second  
460 input, we implement ODEs for the transcription factor AKT which is regulated by PTEN  
461 (Text S1, eq. 1.145, eq. 1.146, eq. 1.147). The transcription of *PTEN* is regulated by  
462 multiple transcription factors among which NF- $\kappa$ B RELA:P50 is a suppressor<sup>65</sup>. Thus, we  
463 included an inhibitory term into the regulation of PTEN expression (Text S1, eq. 1.146).  
464 To reproduce the input dynamics, we trained the model based on the hard-coded time  
465 course data of the two inputs and additionally included simulated time course data of  
466 RELA:P50, BLIMP1 and cleaved PARP1 for model training. Note, that we only fitted the  
467 newly implemented parameters and fixed almost all remaining parameters to their  
468 nominal value. One exception is the parameter  $k2_{13}$ , which was changed from  
469  $0.0102s^{-1}$  to  $0.0162s^{-1}$  to enhance the E2F-mediated expression of *CCNE*. Simulations

470 showed that this modification allows to reproduce the stronger impact of the *MYC* and  
471 *BCL2* double hit scenario. With the abovementioned steps, we constructed a reference  
472 model that allows for efficient and comprehensive simulations of the WT state.  
473 For the manuscript publication, the model will be made accessible at Biomodels  
474 (biomodels.org).

475

## 476 **2. Model visualization**

477 To visualize the model in an automated manner, we created the reference model as  
478 described in the previous section. We then created a YAML file that was converted into  
479 an SBML file using the python package `yaml2sbml`<sup>66</sup>. To create a model scheme, we used  
480 Cytoscape (version 3.10.1, <https://cytoscape.org/>) in combination with the plugin `cy3sbml`  
481 (version 0.3.0, König *et al.*<sup>67</sup>). Since the ODE-based input did not result in a clear model  
482 overview, we converted the ODE system into rate equations using the `atomize` function  
483 of the python package `PyBioNetGen` (version 0.7.4, <https://pypi.org/project/bionetgen/>).  
484 With the final conversion of the rate equation based Bionetgen model format into SBML  
485 using the `pysb` python package (version v1.13.2, Lopez *et al.*<sup>68</sup>), the model can be  
486 visualized using the Prefuse Force Directed Layout algorithm. The algorithm produces a  
487 force-directed graph with clearly distinguishable modules of the model structure (Fig. 1B).  
488 The modules represent regulatory networks of apoptosis, B-cell differentiation, cell cycle  
489 and NF- $\kappa$ B signaling.

490

### 491 **3. Implementation of genetic alterations**

492 We implemented three different alteration types into the model: copy number alterations,  
493 structural variants and mutations (Table 1). We first identified all genes and proteins in  
494 the model that are affected by genetic alterations in the cohort of 304 DLBCL patients  
495 (Chapuy *et al.*<sup>13</sup>). To map genetic alterations to genes and proteins, we converted the  
496 corresponding labels of model variables into HUGO Gene Nomenclature Committee  
497 (HGNC) symbols (<https://www.genenames.org/>) using HGNCHELPER (Oh *et al.*<sup>69</sup>, version  
498 0.8.1). We extended the resulting list of genetic alterations by additional frequent genetic  
499 alterations that affect implemented processes without the direct inclusion of the altered  
500 gene or protein in the model. Those “indirect” alterations include for example upstream  
501 processes of IKK and AKT activation. To include those alterations, we map them to the  
502 affected processes in the model. Moreover, some components of the model represent  
503 complexes where not all individual proteins are modelled. Additionally, model components  
504 not necessarily represent only a specific isoform or homologue. Thus, we also mapped  
505 isoforms and homologues to the corresponding model component. The list of all  
506 implemented alterations including the specification about direct and indirect  
507 implementations is given in table S4.

508 To implement the effect of the collected genetic alterations into the model, we assessed  
509 the functional consequence of a given alteration and defined a perturbation value. Details  
510 are shown below.

511

## 512 **Functional effects of alterations**

### 513 Copy Number Alterations

514 We implemented the copy number alterations (loss or gain) by modulating the parameter  
515 representing the synthesis of a given gene or gene product.

### 516 Structural Variants

517 Structural variants are implemented by assuming that the chromosomal translocation of  
518 a given gene changes the regulation of its transcription. Particularly, we introduce a new  
519 parameter that represents an ectopic expression rate and that has an increased value  
520 compared to the nominal transcription rate constant. Additionally, the regulatory  
521 processes including co-activators and co-repressors are no longer affecting transcription  
522 of the given gene and are therefore set to zero. Due to their relevance and available  
523 biological characterization, we focus on structural variants of the genes *MYC*, *BCL2* and  
524 *BCL6*<sup>16</sup>. In the lymphoma context, these genes can be translocated into the  
525 immunoglobulin loci<sup>26</sup>. Consequently, their expression becomes dysregulated as the  
526 endogenous regulation is lost but strongly promoted by enhancers of immunoglobulin  
527 expression. The concomitant overexpression of BCL2 counteracts apoptosis or in case  
528 of MYC promotes proliferation<sup>26</sup>. Dysregulation of BCL6 expression by mimicking a  
529 translocation was shown to cause DLBCL in mice<sup>70</sup>.

### 530 Mutations

531 Based on the variant classifications of mutations specified in the MAF-file of the analyzed  
532 DLBCL cohort<sup>13</sup>, we defined four mutation categories: loss-of-function (LOF), modified  
533 activity (MA), mutations missing additional information (info n/a) and gain-of-function

534 (GOF). To the first category we assign non-sense, splice site, frame shift indels, non-stop,  
535 de novo start in frame mutations which lead to a non-functional protein. For the second  
536 category, we assume that missense or in frame indel mutations lead to i) a reduced  
537 activity of the protein, such as reduced binding affinity towards its binding partners or ii)  
538 an increased activity. To determine if a mutation causes a reduced or increased activity  
539 or results in a GOF, we searched in literature for effects of mutations of the given genes  
540 and checked the frequency of the given alterations in DLBCL using cBioportal<sup>30-32</sup> (using  
541 the datasets of Chapuy *et al.*<sup>13</sup>, Lohr *et al.*<sup>8</sup>, Reddy *et al.*<sup>11</sup> and Morin *et al.*<sup>9</sup>) as well as  
542 the annotation of oncoKB<sup>33,34</sup> for the functional effect and if its oncogenic in DLBCL or not  
543 (Table S1). If there was no information for its oncogenic effect in DLBCL, neither for LOF  
544 nor MA mutations, and there was no information in literature for given mutations causing  
545 oncogenic effects, we neglected the alteration. Based on these criteria, we did not  
546 implement an effect for the following alterations:

547 CCNA1 (MA & LOF), CCNA2 (MA), CCNB3 (MA & LOF), CCNE1 (MA), CD79A (MA),  
548 CDC20 (MA), CDK1 (MA), E2F1 (MA), FADD (MA), FZR1 (MA), MCL1 (MA), NFKB1  
549 (LOF), PIK3CA (CN gain), PPP4C (MA), REL (MA), XIAP (MA)

550 Silent mutations are not considered to have an effect and were therefore not included.  
551 For the mutations with missing information about the variant classification, the mutation  
552 effect is defined similar to the effect in the category modified activity (MA) if not stated  
553 otherwise (Table S4).

554

## 555 **Defining perturbation strengths**

### 556 Copy Number Alterations

557 The parameter value is multiplied with a perturbation strength of 1.5 for amplifications and  
558 0.67 for deletions to resemble the addition or loss of one copy. To test the impact of  
559 stronger or weaker effects of copy number alterations, we perturbed the corresponding  
560 parameters (Fig. S6, S7).

561

### 562 Structural Variants

563 The perturbation strength for structural variants is chosen in a way that this strength is  
564 small while an effect is still present. We tested different parameter values and quantified  
565 the corresponding impact on the malignancy score (Fig. S8A, S8D, S8G), timepoint of  
566 apoptosis (Fig. S8B, S8E, S8H) and number of divisions (Fig. S8C, S8F, S8I). We  
567 selected the lowest tested value that still shows the expected effect.

568

### 569 Mutations

570 To implement the effect of LOF, MA and GOF mutations, we select the processes that are  
571 affected by a given alteration and change the corresponding model parameters by a factor  
572 that is specific for the different mutation types. The link between alterations, parameters  
573 and perturbation values are given in table S4. As a gene in a patient sample can have  
574 multiple point mutations, we take the amount of point mutations into account by assigning  
575 to each point mutation the specified factor and multiplying the factors.

576 For LOF mutations, we assume the corresponding protein to be non-functional and  
577 therefore set the affected rate constants to a value close to zero ( $1e-10$ ). Exceptions are  
578 truncating mutations of *BCL10* which have been observed to result in increased activity  
579 (for details and experimental references see Table S1) and are therefore assigned to the  
580 increased activity factor of 3.2 ( $\log_{10}$  value of 0.5). MA mutations causing an increased  
581 protein activity are also associated with this factor. In contrast, MA mutations causing a  
582 decreased protein activity are multiplied with a factor of  $1e-2$ . Note that for MA mutations  
583 the specified factor is multiplied to the corresponding model parameter in contrast to the  
584 LOF mutations for which the corresponding parameter value is set to an absolute value  
585 of  $1e-10$ . For GOF mutations, we introduce processes into the model that have a rate of  
586 zero if the mutation is absent and change it to a value of 100 a.u./min (MYD88 gain-of-  
587 function) or 1 a.u./min (My-T-BCR supercomplex), if the mutation is present (Table S1).

588 We chose the abovementioned perturbation strengths for mutations in a way that they  
589 are in a physiological range, biologically meaningful and show, if applicable, an impact on  
590 the malignancy score. We therefore tested the impact of different perturbation strengths  
591 on the malignancy score, apoptosis timepoint and proliferation (Fig. S9, S10, S11, S12).

592 For missense mutations of *TP53*, we use experiment-derived information from the study  
593 of Kato *et al.*, in which a yeast-based assay of 2314 *TP53* point mutations was performed  
594 to assess p53 functionality (Kato *et al.*<sup>46</sup>, The *TP53* Database (R21, Jan 2025):  
595 <https://tp53.cancer.gov>, deAndrade *et al.*<sup>71</sup>). The quantified readout of expression level  
596 changes of p53 target genes can be used to simulate the effects of *TP53* mutations<sup>72</sup>. If  
597 multiple point mutations of *TP53* are present within one patient sample, we average the  
598 value of the given point mutations. Moreover, if the information about the point mutation

599 in the patient sample causes a LOF, we set the expression rate constant for BAX  
600 expression to  $1e-10$ .

601

## 602 **Handling the effect sizes of multiple alterations of the same gene**

603 Within a patient sample, the same gene can be affected by multiple alterations. We model  
604 different alteration types in an accumulative manner. For LOF mutations, we set the  
605 affected processes to a value close to zero instead of multiplying a factor to the rate  
606 constants to prevent compensating effects between copy number gains and LOF  
607 mutations.

## 608 **4. Creating and simulating patient models**

609 After associating genetic alterations to model parameters and defining perturbation  
610 strengths, patient models can be created by defining patient-specific parameter sets.  
611 Each patient model is thereby based on the reference model (Methods, section 1) and  
612 only those parameters are perturbed that are affected by the patient-specific set of genetic  
613 alterations. From the 292 patients with significant alterations (Chapuy *et al.*<sup>13</sup>), we were  
614 able to create 284 patient models. For 8 individuals there were no alterations that could  
615 be mapped to our model. We ran the simulations using MATLAB (R2023b, The  
616 Mathworks Inc., Natick, MA) and Python (version 3.12, Python Software Foundation,  
617 <https://www.python.org/>) in combination with AMICI<sup>59</sup>. For all our analyses, we define the  
618 simulation end point at 10 days. The timepoint of apoptosis is defined as cPARP reaching  
619 a level of 2500 a.u.<sup>29</sup> While the reference model shows apoptosis induction upon 6.4 days,  
620 perturbations can lead to shorter or longer survival times. Note that in the latter case, the

621 simulation end point can be reached and the apoptosis timepoint is then given as endpoint  
622 of simulations. To assess the impact of the simulation end point on our score, we  
623 simulated the 284 patient models for 30 days (Fig. S3). Most of the models that showed  
624 no apoptosis induction before 10 days also did not show apoptosis until the end point of  
625 30 days. Only a small number of patient models undergo apoptosis between 10 and 30  
626 days. This shows that 10 day-simulation robustly capture apoptosis decisions. To quantify  
627 the number of divisions, we track CDH1 crossing a threshold value of 0.02 a.u. as it was  
628 defined in the original model of Roy *et. al*<sup>29</sup>.

## 629 **5. Defining a malignancy score to quantify effect sizes of alterations**

630 We here use the timepoint of apoptosis and the division rate as readout. We separate the  
631 space of apoptosis timepoint and division rate into a physiological and aberrant state  
632 based on the state of the reference model. We assume that increased cell numbers  
633 compared to the reference model correspond to an aberrant state and less or equal  
634 numbers are physiological. The separator of these two cell states is therefore the  
635 calculated reference division rates for each timepoint of apoptosis with the separator  
636 function

$$637 \quad f(x) = \frac{5 \text{ divisions}}{x \text{ days}}$$

638 Using the separator function, one can relate an alteration-mediated change to the  
639 reference-like state by computing the shortest Euclidean distance, the perpendicular,  
640 between the changed cell state and the separator function (Fig. S2). This way, the score  
641 represents the distance between the changed cell state and the reference-like state. We  
642 define a negative sign for the score, if the division rate at the given timepoint of apoptosis

643 is smaller than the reference value. Consequently, a positive score represents a change  
644 causing an aberrant cell state and a negative or zero score is associated with a  
645 physiological state.

646

647 For the analyses of causative alterations (Fig. 5), we check if a drop out causes a state  
648 that is equal or below the separator function of the reference WT model. If this is the case  
649 and the patient model is in the aberrant cell state, the tested alteration is defined as  
650 causative.

651

## 652 **6. Computing expected effects for alteration pairs**

653 To determine the expected state, we performed a vector addition of the two individual  
654 alteration-induced changes in the state. From this expected state we then calculated the  
655 score as described in Methods. This expected score is then compared to the simulated  
656 true score which is the result of simulating the two alterations simultaneously. The  
657 deviations between expected and simulated true effect of alteration pairs are shown in  
658 Fig. 4A.

659 Note that the vector addition can result in some cases to infeasible states. In these cases,  
660 the states are corrected by setting the value to zero for negative values, or to the  
661 simulation end point for values exceeding the end point.

### 662 **Definition of additive, synergistic and dominating effects**

663 For the definition of additive effects, we compare for each alteration pair its true and  
664 expected score. We consider effects as purely additive if the absolute difference between

665 true and expected effect is smaller than or equal to 0.01. Changes higher than 0.01 show  
666 unexpected effects that can be synergistic, compensating or dominating. We define  
667 synergistic effects as the combined effect of an alteration pair that show a greater effect  
668 in combination than the expected sum of the individual effects. Unexpected effects are  
669 also observed for alterations affecting similar regulations or parts of the model network.  
670 In these cases, one alteration can show a dominant effect compared to the second  
671 alteration resulting in a deviation between the expected and true score.

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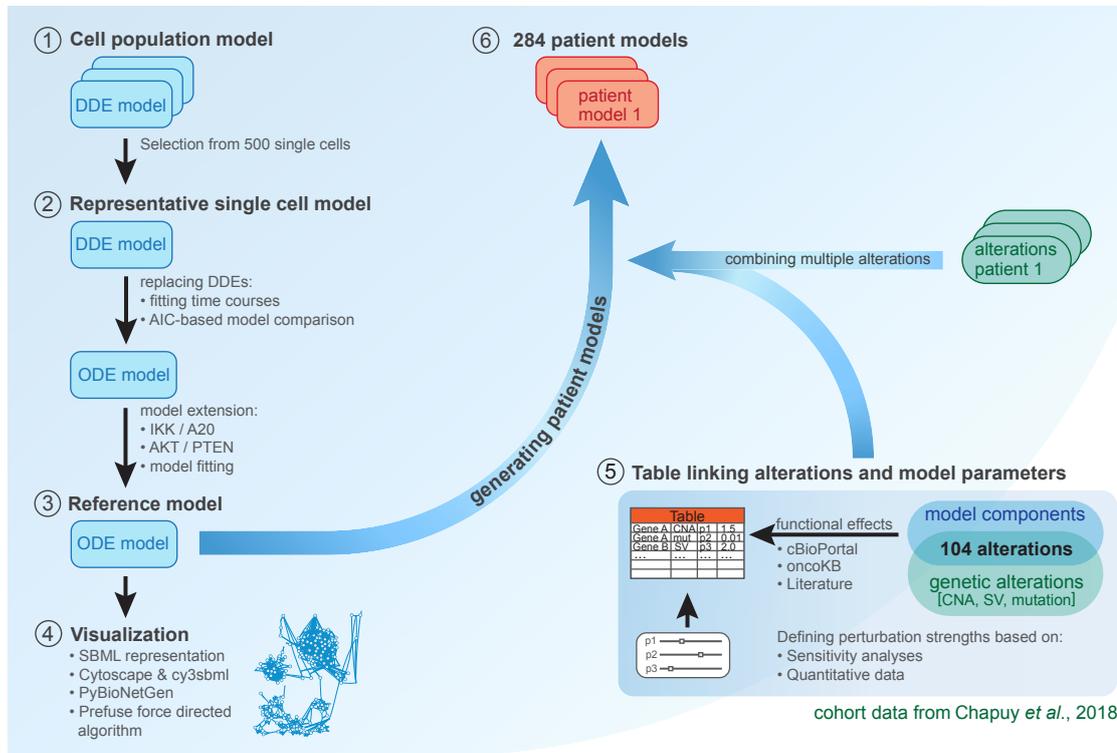
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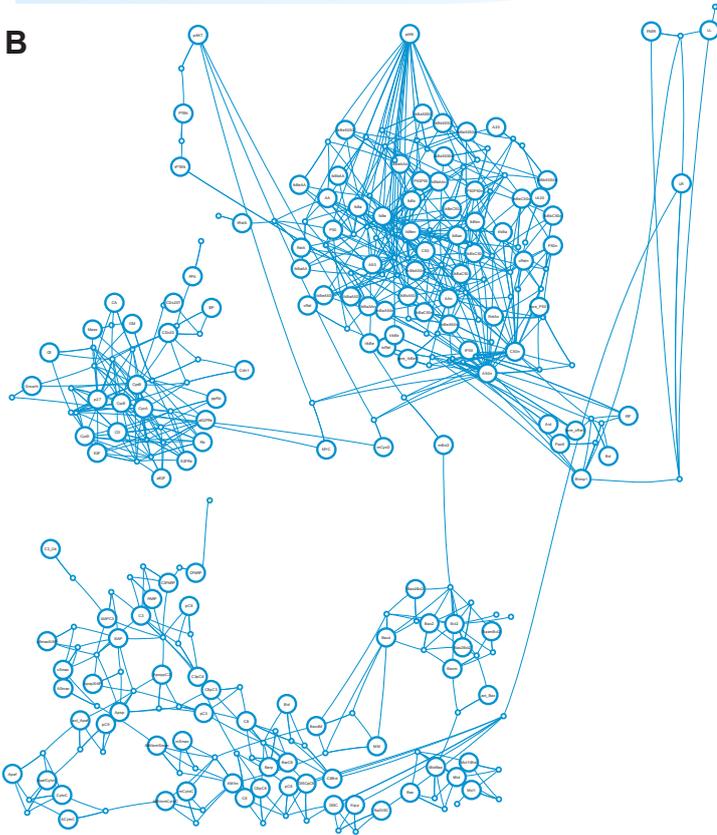
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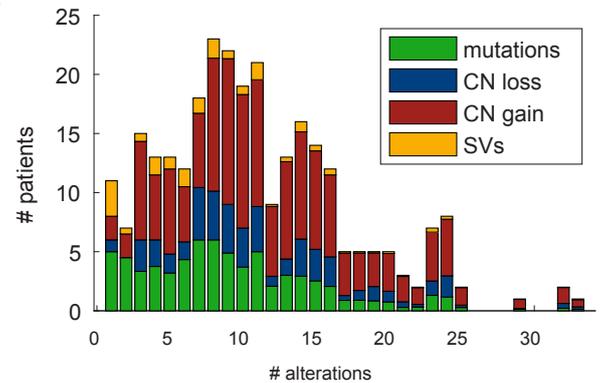
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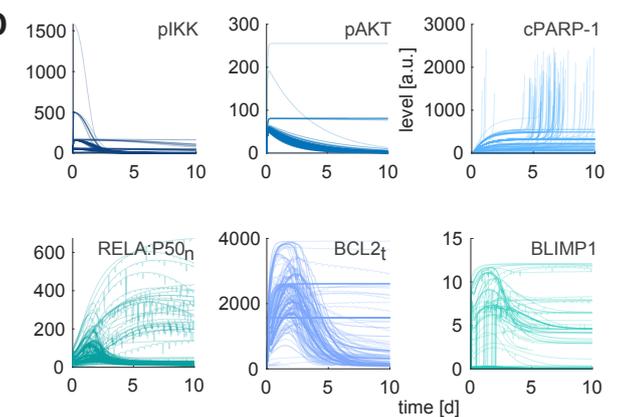
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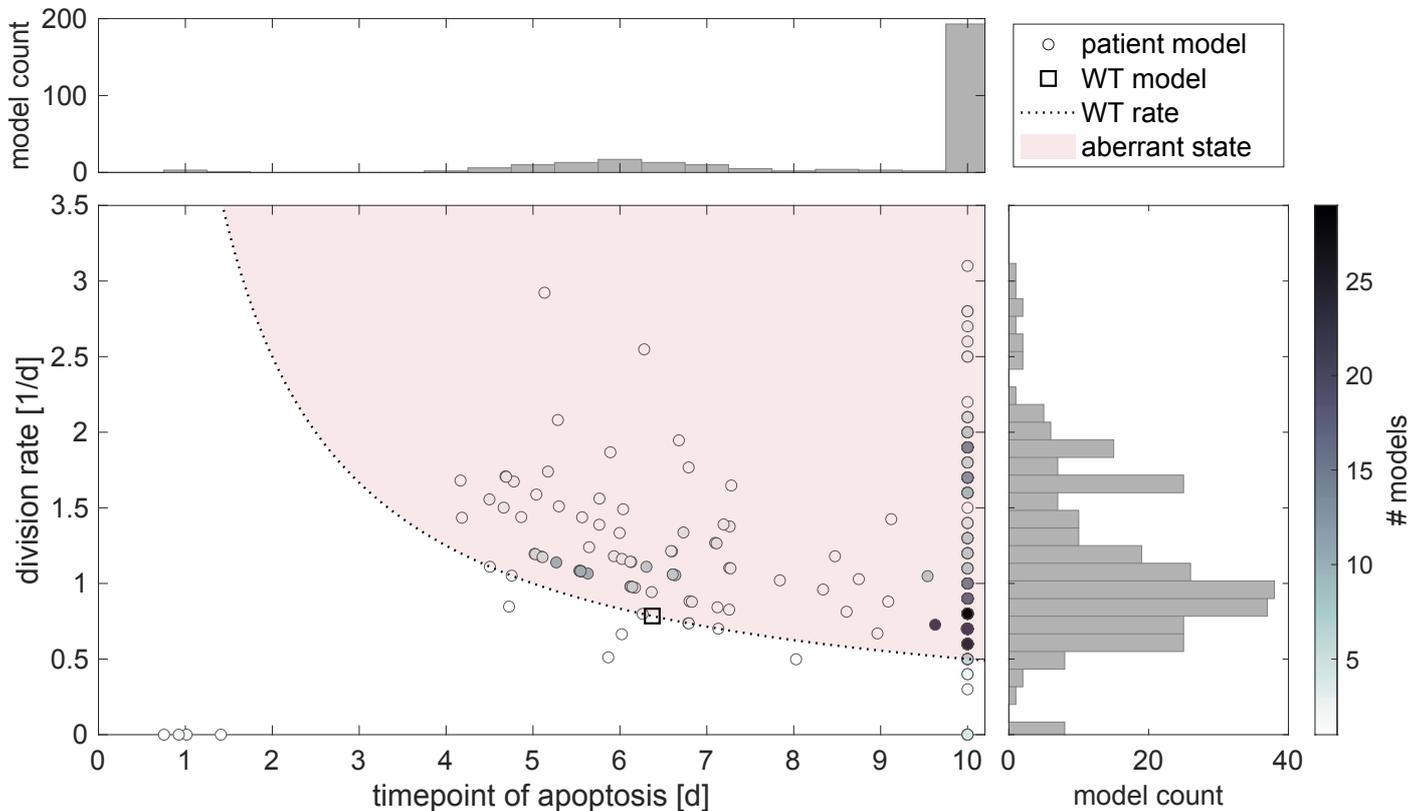


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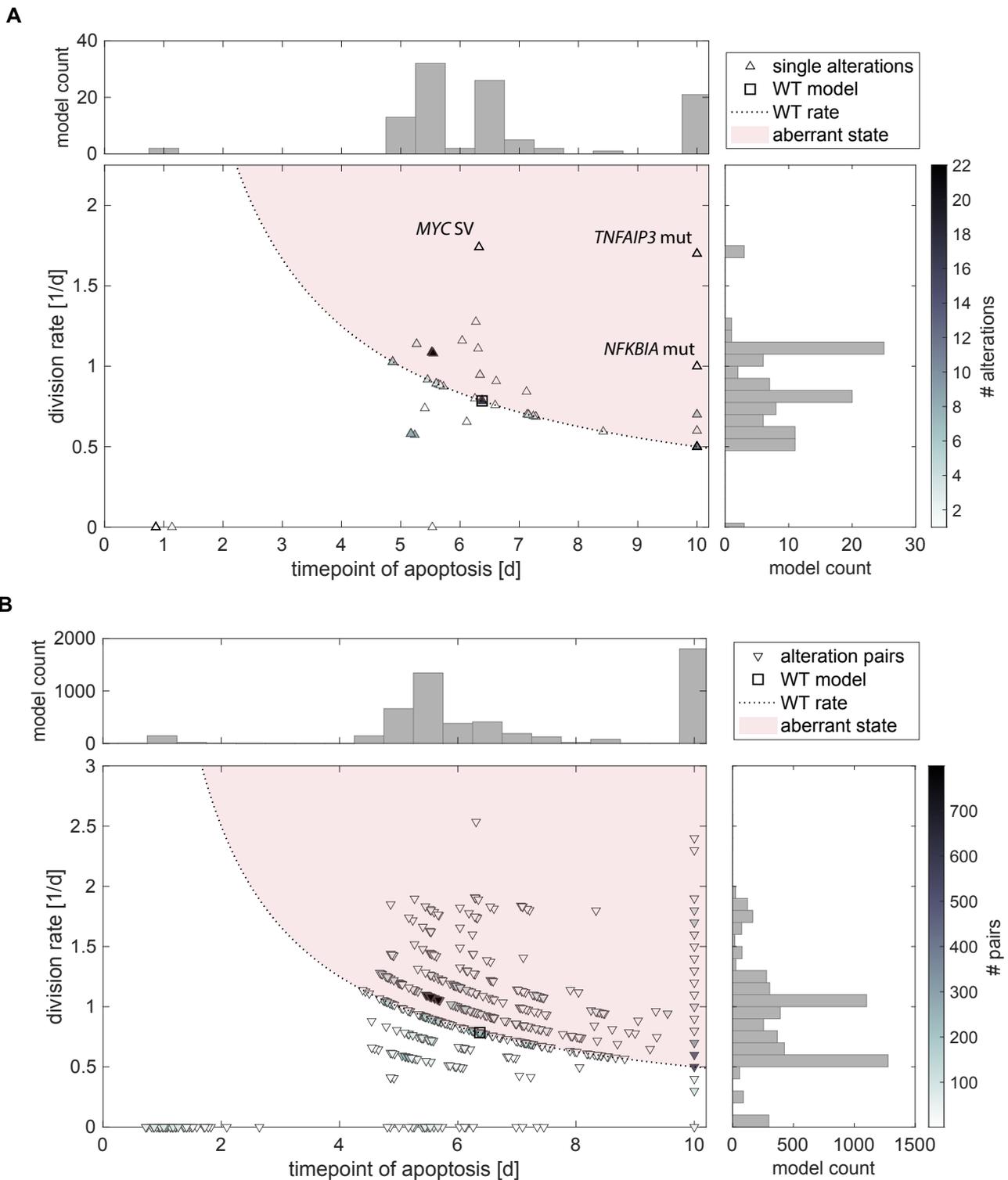
## Figure 1. Generation of patient-specific DLBCL models.

**(A)** Workflow describing the development of patient-specific models based on the population model of Roy et al.<sup>29</sup>. We reduced the cell population model into a representative single cell model (1), transformed the delay differential equations into ordinary differential equations (2) and extended the initial model to capture TNFAIP3 (A20) and the PTEN-PI3K-AKT-mediated signaling (3). For the latter, we included the negative feedback regulation of NF- $\kappa$ B via A20, and PI3K signaling via AKT and its regulation by PTEN. After visualizing the reference model (4), we created a table linking all mapped alterations with model parameters and specific perturbation strengths (5). Incorporation of the patient-specific alterations led to 284 patient models (6). For details of all workflow steps, see Methods. **(B)** Scheme of the derived computational model. The network model consists of 158 variables, 544 parameters and describes regulatory interactions of NF- $\kappa$ B signaling, differentiation of naïve B-cells to antibody-producing cells, proliferation as well as apoptosis. **(C)** The number of alterations is given per DLBCL patient. Moreover, the distribution of implemented alteration types (mutations, copy number (CN) loss, CN gain and structural variants (SV)) is given for each amount of alterations. **(D)** Dynamics of six selected model components for all patient models. Cleaved Parp-1 (cPARP-1) is used as marker for the timepoint of apoptosis. pIKK: phosphorylated IKK, pAKT: phosphorylated AKT, RELA:P50<sub>n</sub>: nuclear complex of RELA and P50, BCL2<sub>t</sub>: BCL2 mRNA and BLIMP1: BLIMP1 protein, a marker for B-cell differentiation.



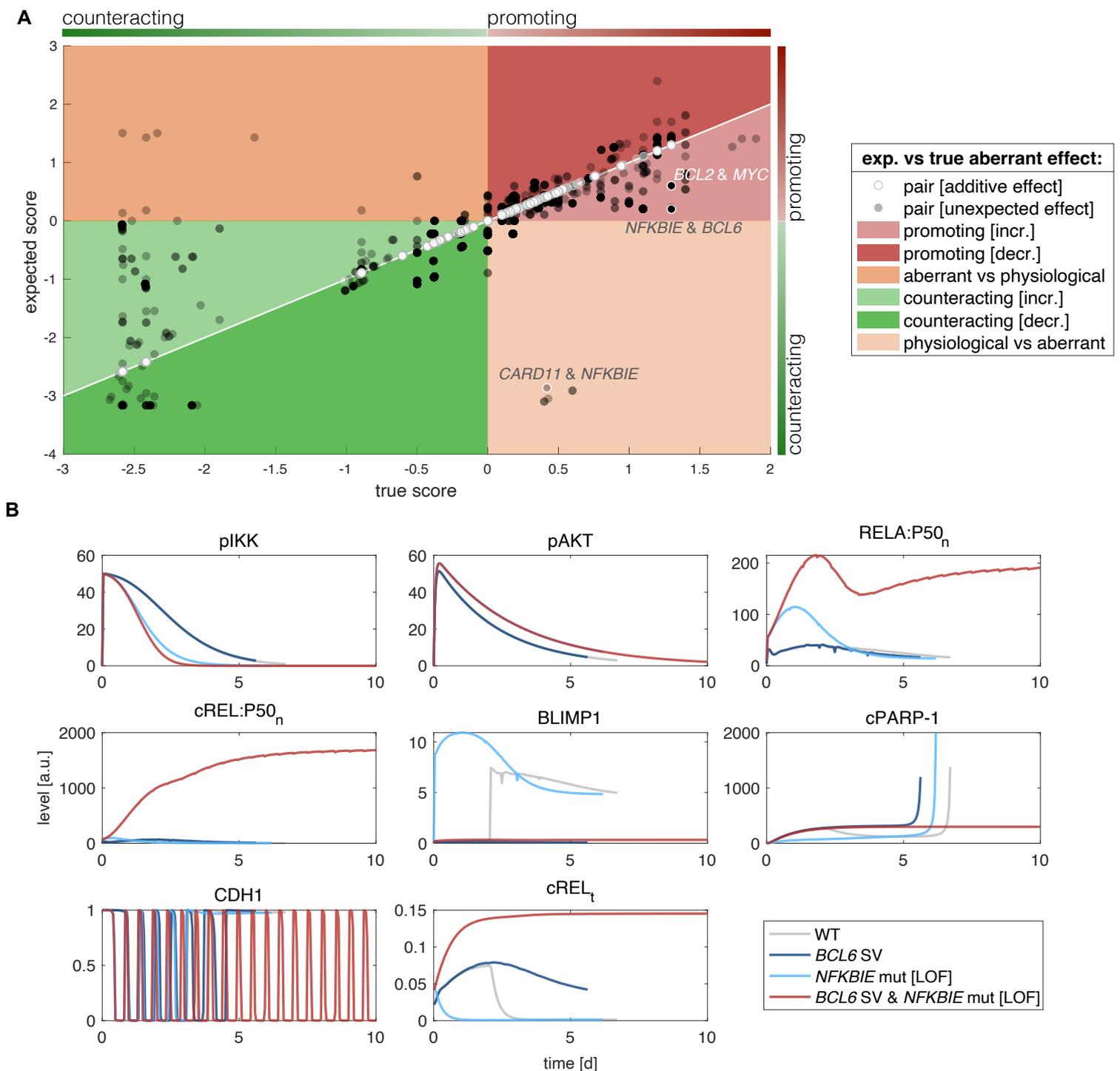
**Figure 2. Cellular state of 284 patient models.**

In the WT model (indicated by an empty square), the cell undergoes apoptosis upon around 6.4d and divides 5 times resulting in a division rate of around  $0.8d^{-1}$ . The dotted line marks the reference division rate at which cells are in a WT-like state according to the given timepoint of apoptosis. Empty circles show patient models; the color intensity represents the amount of models found in a given state. 90.5% of patient models are above the dotted line and thereby show, compared to the reference division rate, increased proliferation. These models therefore represent an aberrant state. The simulation end point is 10 days. Patient models in which apoptosis is induced later than 10 days or never, are therefore plotted at a timepoint of apoptosis of 10 days, longer simulation time does not change the results (Fig. S3). Histograms depict the model count for specific timepoints of apoptosis (top) or the number of divisions (right).



**Figure 3. Effects of single and paired alterations in the WT model.**

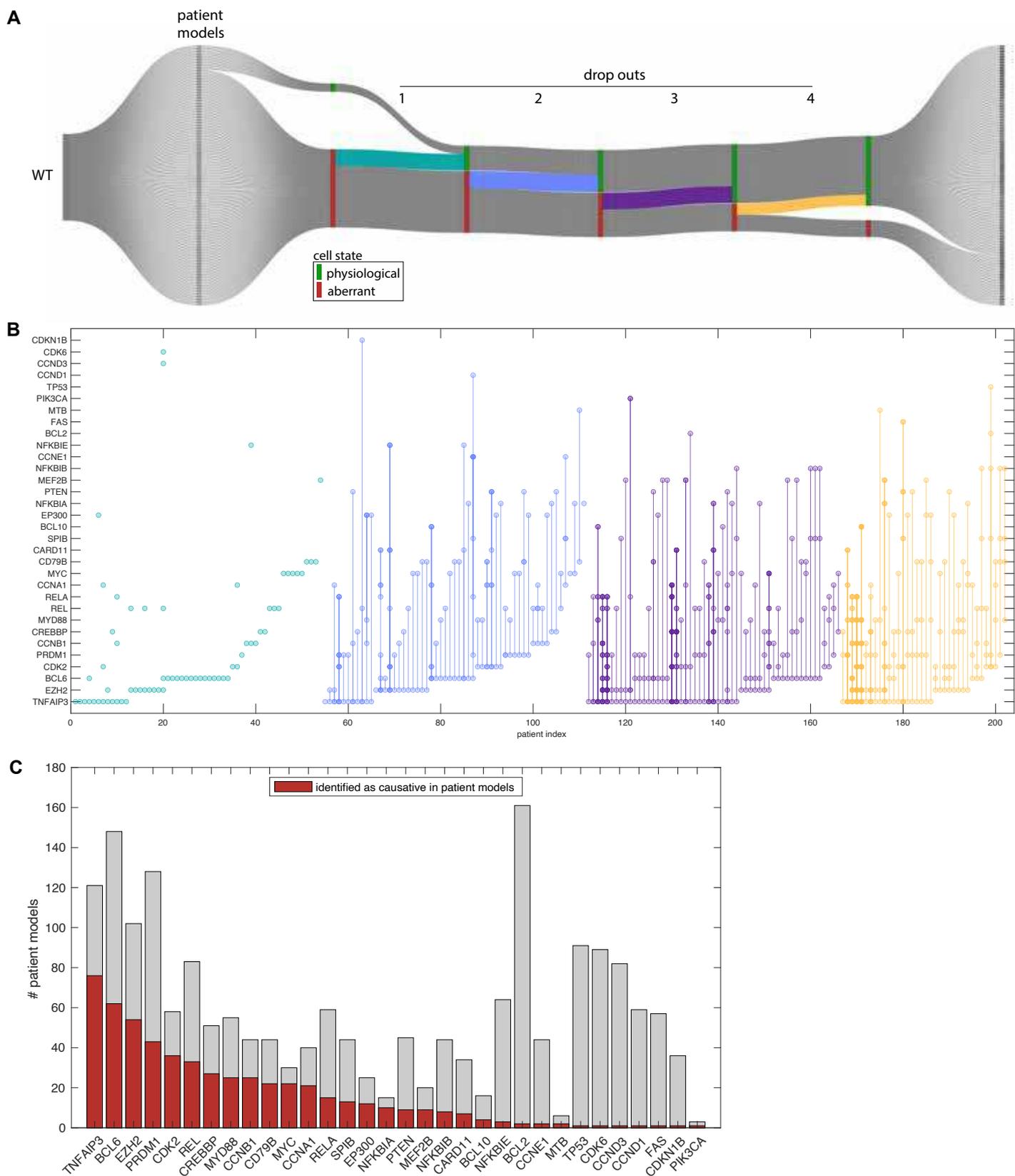
**(A)** Effect of single alterations on the cell state. 40.4% of single alterations promote an aberrant state. Example alterations labeled: *MYC* SV: structural variant of *MYC*, *TNFAIP3* mut: LOF mutation of *TNFAIP3*, *NFKBIA* mut: LOF mutation of *NFKBIA*. **(B)** Simulated effect of all possible combinations of two alterations. For 58.1% of all pairs, the combined effect results in an aberrant state.



**Figure 4. Identification of synergistic effects of alteration pairs.**

**(A)** The expected score of all alteration pairs is plotted against the corresponding true calculated score. The bars on the top and on the right mark aberrant state promoting effects for positive scores (red) and counteracting effects for negative scores (green). The different colored regions allow to classify the combinatorial effects. The white line marks the effects where the true score corresponds to the expected score, that is, the alteration pairs have a purely additive effect. All alteration pairs with an absolute difference between true and expected score smaller or equal than 0.01 are defined as additive and are given by white dots. The grey and black dots represent all pairs with an unexpected effect.

**(B)** Simulated time courses of selected model components mechanistically explain the identified synergistic effect between a *BCL6* SV and an *NFKBIE* LOF mutation. While both alterations individually reduce the survival time and number of divisions (dark and light blue lines), their combination (red line) causes a strong increase in the proliferation rate (CDH1) with abrogated apoptosis induction (cPARP-1). The *NFKBIE* mutation alone causes a dysfunctional inhibition of NF- $\kappa$ B family members and in turn a transient hyperactivation of the NF- $\kappa$ B system, i.e. a strongly increased activity of RELA:P50 and cREL:P50. In addition, PRDM1 transcription is induced by NF- $\kappa$ B signaling and its hyperactivation triggers a fast increase in the BLIMP1 (PRDM1) protein level, which, in turn, leads to a reduced transcription of cREL (Fig. 4B, cREL<sub>t</sub>). Together, this regulation prevents the transition to an aberrant state which is why *IkB $\epsilon$*  alone is not sufficient to promote an aberrant state. However, the case of additional genetic alterations that diminish BLIMP1 activity, such as *BCL6* SV, allow elevated levels of cREL. This effect can be reproduced by simulating the *NFKBIE* mutation in combination with a reduced transcription rate of PRDM1 (Fig. S4A).



**Figure 5. Identification of personalized aberration-causing alterations.**

**(A)** Representation of all 284 patient models by individual lines. The cellular state of the models is physiological (green bars) for 27 (9.5%) models or aberrant (red bars) for 257 (90.5%). From left to right: successive removal of 1, 2, 3 or 4 alterations from models in aberrant states. For each removal all possible combinations are tested. Out of the 257 patient models with an aberrant state, 54 show a switch from the aberrant state to a physiological state after dropping out a single alteration (turquoise). Therefore, these alterations are identified as a single aberration-causing alteration. For the remaining patient models, the removal of more than one alteration is required for a switch to a benign state: For 57 patient models two alterations (light blue), for 55 models three alterations (purple), for 36 models four alterations (yellow). For 55 patient models, more than four alterations need to be removed in order to reach a benign state. The plot was created using plotly (version 5.3.1, <https://plotly.com/graphing-libraries/>). **(B)** Causative genes and their combinations for 202 patient models (given by patient index). Colors present the number of required causative genes, see Fig. 5A. Each circle represents a causative gene in a given patient model. Multiple causative genes within a patient model are connected through a line. Since there can be multiple combinations promoting a cancer state in the same patient model, circles and lines can overlap. **(C)** Number of patient models in which a causative genetic alteration is present (height of bars), and number of patients in which it is the aberration-causing gene (red part of the bars).

**Table 1. Implemented genetic alterations.** For each alteration, the number of patients harboring the specified genetic alteration are shown. CN: Copy number, SV: Structural variant, GOF: Gain-of-function mutation, MA: Modified activity (mutation causing increased or decreased activity), LOF: Loss-of-function mutation, mutation [info n/a]: mutation with missing information about the mutation type (assigned to LOF or MA).

Gene	CN gain	CN loss	SV	mutation [info n/a]	mutation [LOF]	mutation [MA]	mutation [GOF]
APAF1	58	0	0	0	0	0	0
BAX	44	0	0	0	0	0	0
BCL10	0	0	0	10	4	3	0
BCL2	116	0	61	23	0	56	0
BCL6	88	25	56	5	1	12	0
CARD11	0	0	0	16	1	22	0
CASP3	0	45	0	0	0	0	0
CCNA1	40	0	0	0	0	0	0
CCNB1	44	0	0	0	0	0	0
CCND1	59	0	0	0	0	0	0
CCND3	70	0	0	8	3	3	0
CCNE1	44	0	0	0	0	0	0
CD79B	0	0	0	24	5	15	0
CDK2	58	0	0	0	0	0	0
CDK4	58	0	0	0	0	0	0
CDK6	89	0	0	0	0	0	0
CDKN1B	0	35	0	0	1	0	0
CREBBP	0	0	0	23	17	28	0
CYCS	96	0	0	0	0	0	0
DIABLO	58	0	0	0	0	0	0
EP300	0	0	0	16	2	7	0
EZH2	89	0	0	13	0	10	0
FADD	59	0	0	0	0	0	0
FAS	0	36	0	15	9	3	0
FBXO11	0	0	0	0	2	2	0
IRF4	55	0	0	0	0	1	0
KMT2D	58	0	0	40	48	10	0
MALT1	116	0	0	0	0	0	0
MCL1	91	0	0	0	0	0	0
MEF2B	0	0	0	8	2	10	0
MTB	0	0	0	0	0	0	6
MYC	0	0	25	0	0	21	0
MYD88	0	0	0	33	0	22	0
NFKBIA	0	0	0	9	6	10	0
NFKBIB	44	0	0	0	0	0	0
NFKBIE	55	0	0	6	2	3	0
PARP1	63	25	0	0	0	1	0
PAX5	0	0	0	0	4	2	0
PIK3CA	0	0	0	0	1	2	0
PRDM1	0	120	0	11	8	4	0
PTEN	0	36	0	5	3	2	0
RB1	40	42	0	0	0	1	0
REL	83	0	0	0	0	0	0
RELA	59	0	0	0	0	0	0
SPIB	44	0	0	0	0	0	0
TNFAIP3	0	109	0	21	5	0	0
TP53	0	66	0	34	6	26	0

**Table 2: Composition of aberrant states of pair alterations**

<b>number of individual alterations leading to an aberrant state</b>	<b>number of pairs in aberrant state [%]</b>
both	861 [27.7%]
one	2230 [71.6%]
none of them	22 [0.7%]

**Table 3. Pairs including MYC SV with a synergistic effect.** For each alteration pair the malignancy score, expected score, FC (fold change: score divided by expected score) and number of patients harboring the alteration pair is given.

alteration 1	alteration 2	score	expected score	FC score	# patients	
MYC SV	<i>BCL2</i> SV	1.3	0.6	2.16	9	
	<i>FAS</i> mutation [info n/a]	1.3	0.6	2.16	2	
	<i>FAS</i> mutation [MA]	1.3	0.6	2.16	0	
	<i>FAS</i> mutation [LOF]	1.3	0.6	2.16	0	
	<i>KMT2D</i> mutation [info n/a]	1.3	0.6	2.16	3	
	<i>KMT2D</i> mutation [MA]	1.3	0.6	2.16	0	
	<i>KMT2D</i> mutation [LOF]	1.3	0.6	2.16	3	
	<i>PARP1</i> mutation [MA]	1.3	0.6	2.16	0	
	<i>TP53</i> mutation [info n/a]	1.3	0.6	2.16	2	
	<i>TP53</i> mutation [MA]	1.3	0.6	2.16	2	
	<i>TP53</i> mutation [LOF]	1.3	0.6	2.16	0	
	<i>MYD88</i> mutation [info n/a]	1.4	0.7	1.99	4	
	<i>MYD88</i> mutation [MA]	1.4	0.7	1.99	0	
	<i>NFKBIA</i> mutation [info n/a]	1.4	0.8	1.74	2	
	<i>NFKBIA</i> mutation [MA]	1.4	0.8	1.74	1	
	<i>PTEN</i> mutation [info n/a]	1.4	0.8	1.74	0	
	<i>PTEN</i> mutation [MA]	1.4	0.8	1.74	0	
	<i>PTEN</i> mutation [LOF]	1.4	0.8	1.74	0	
	<i>CASP3</i> CN loss		1.2	0.72	1.67	3
	<i>CCNB1</i> CN gain		1.73	1.27	1.36	4
	<i>BCL2</i> mutation [info n/a]		1.1	0.83	1.34	3
	<i>BCL2</i> mutation [MA]		1.1	0.83	1.34	5
	<i>BCL2</i> CN gain		1.13	0.84	1.34	7
	<i>FAS</i> CN loss		1.11	0.83	1.34	1
<i>MCL1</i> CN gain		1.12	0.84	1.34	6	
<i>TP53</i> CN loss		1.12	0.84	1.34	4	
Sum					24	

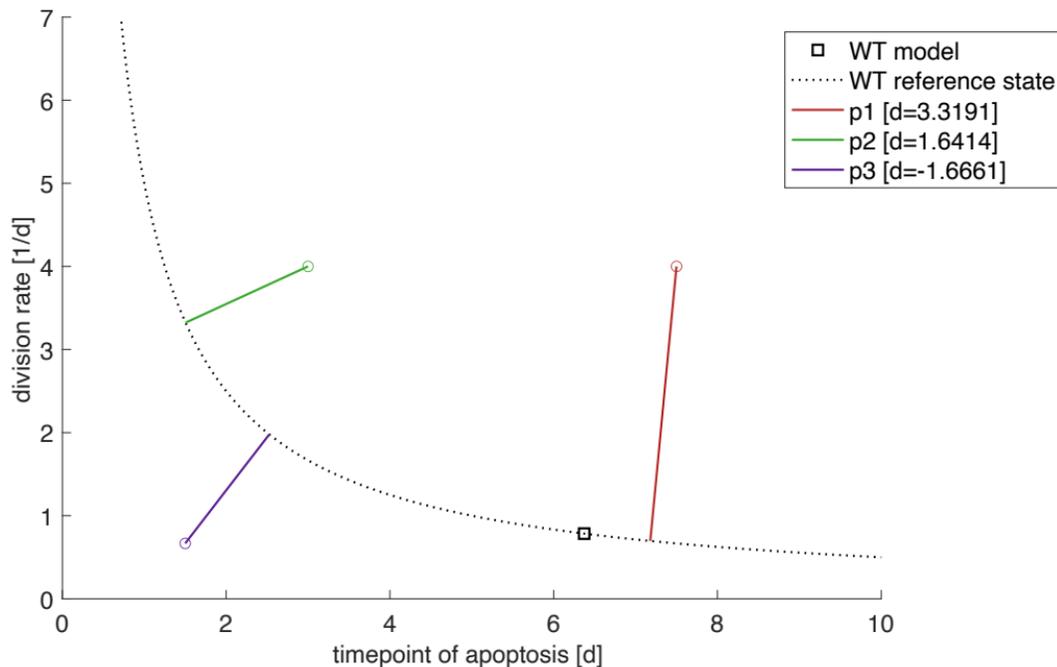
**Table 4. Pairs including *BCL6* SV or mutated *PRDM1* in combination with alterations affecting NF- $\kappa$ B activity.** For each alteration pair the malignancy score, expected score, FC (fold change: score divided by expected score) and number of patients harboring the alteration pair is given.

<b>alteration 1</b>	<b>alteration 2</b>	<b>score</b>	<b>expected score</b>	<b>FC score</b>	<b># patients</b>
<i>BCL6</i> SV	<i>NFKBIE</i> mutation [info n/a]	1.1	0.2	5.37	4
<i>MYD88</i> mutation [MA]	<i>PRDM1</i> mutation [LOF]	0.36	0.22	1.65	2
<i>MYD88</i> mutation [info n/a]	<i>PRDM1</i> mutation [info n/a]	0.36	0.22	1.64	2
<i>MYD88</i> mutation [info n/a]	<i>PRDM1</i> CN loss	0.35	0.22	1.62	19
<i>MYD88</i> mutation [MA]	<i>PRDM1</i> CN loss	0.35	0.22	1.62	12
<i>BCL6</i> SV	<i>MYD88</i> mutation [info n/a]	0.35	0.22	1.62	8
<i>BCL6</i> SV	<i>MYD88</i> mutation [MA]	0.35	0.22	1.62	6
<i>BCL6</i> SV	<i>TNFAIP3</i> CN loss	0.45	0.32	1.43	29
<i>PRDM1</i> CN loss	<i>TNFAIP3</i> CN loss	0.45	0.32	1.43	91
<i>PRDM1</i> mutation [LOF]	<i>TNFAIP3</i> CN loss	0.45	0.32	1.43	2
<i>PRDM1</i> mutation [info n/a]	<i>TNFAIP3</i> CN loss	0.45	0.32	1.43	4
<i>PRDM1</i> mutation [MA]	<i>TNFAIP3</i> CN loss	0.45	0.32	1.43	2
Sum					104



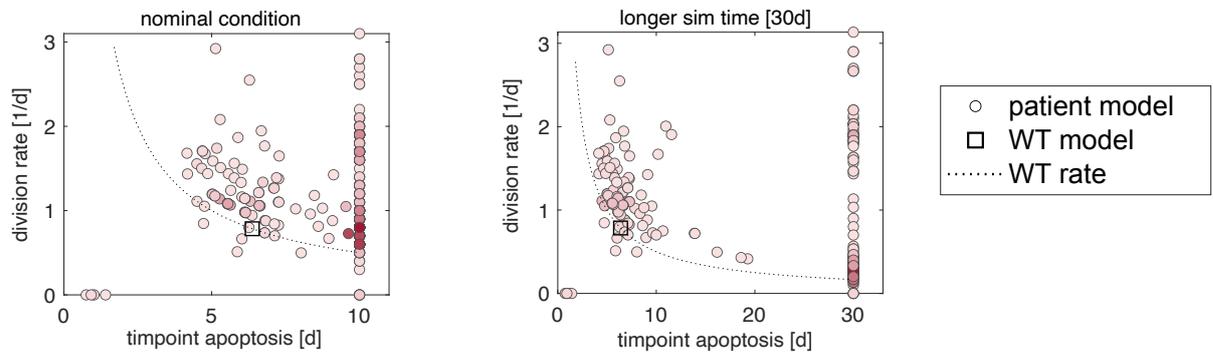
**Figure S1. Oncoprint of the cohort data from Chapuy et al., 2018<sup>13</sup> for all genes that could be mapped to the model.**

The shown alterations are the basis for creating the patient-specific DLBCL models. To create the oncoprint plot, the R (version 4.5.1, <https://www.r-project.org>) package ComplexHeatmap from the Bioconductor repository was used (version 2.24.0, Gu et al.<sup>73,74</sup>).



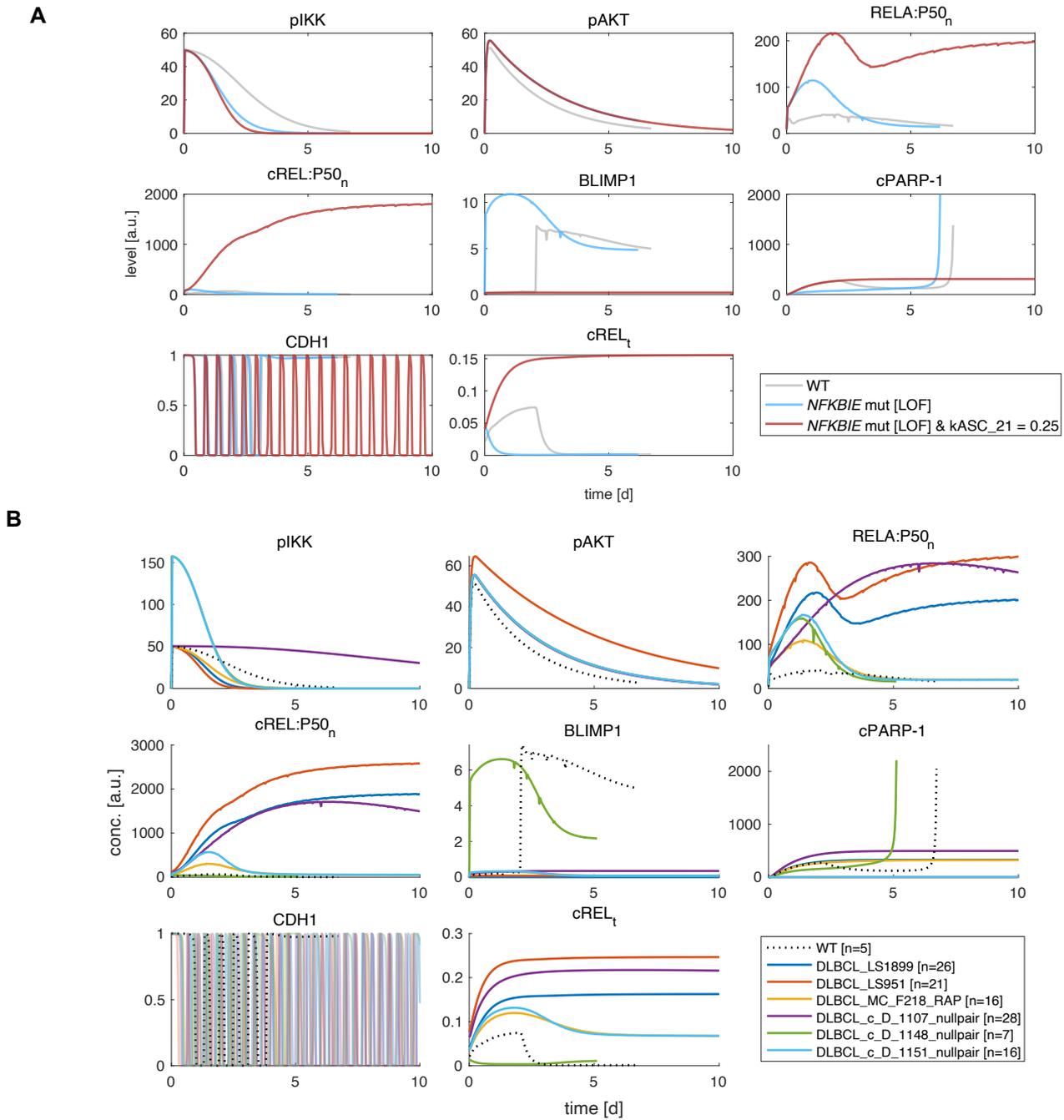
### Figure S2. Illustration of malignancy score calculation.

Based on the WT model (empty square), we calculated a reference state (dotted line) representing for each timepoint of apoptosis the corresponding WT division rate. Examples p1 and p2 show alterations that cause increased proliferation rates and therefore result in an aberrant cell state. Example p3 shows a transition below the reference state and is therefore in a physiological cell state. The calculated score for each of the examples is given in brackets.



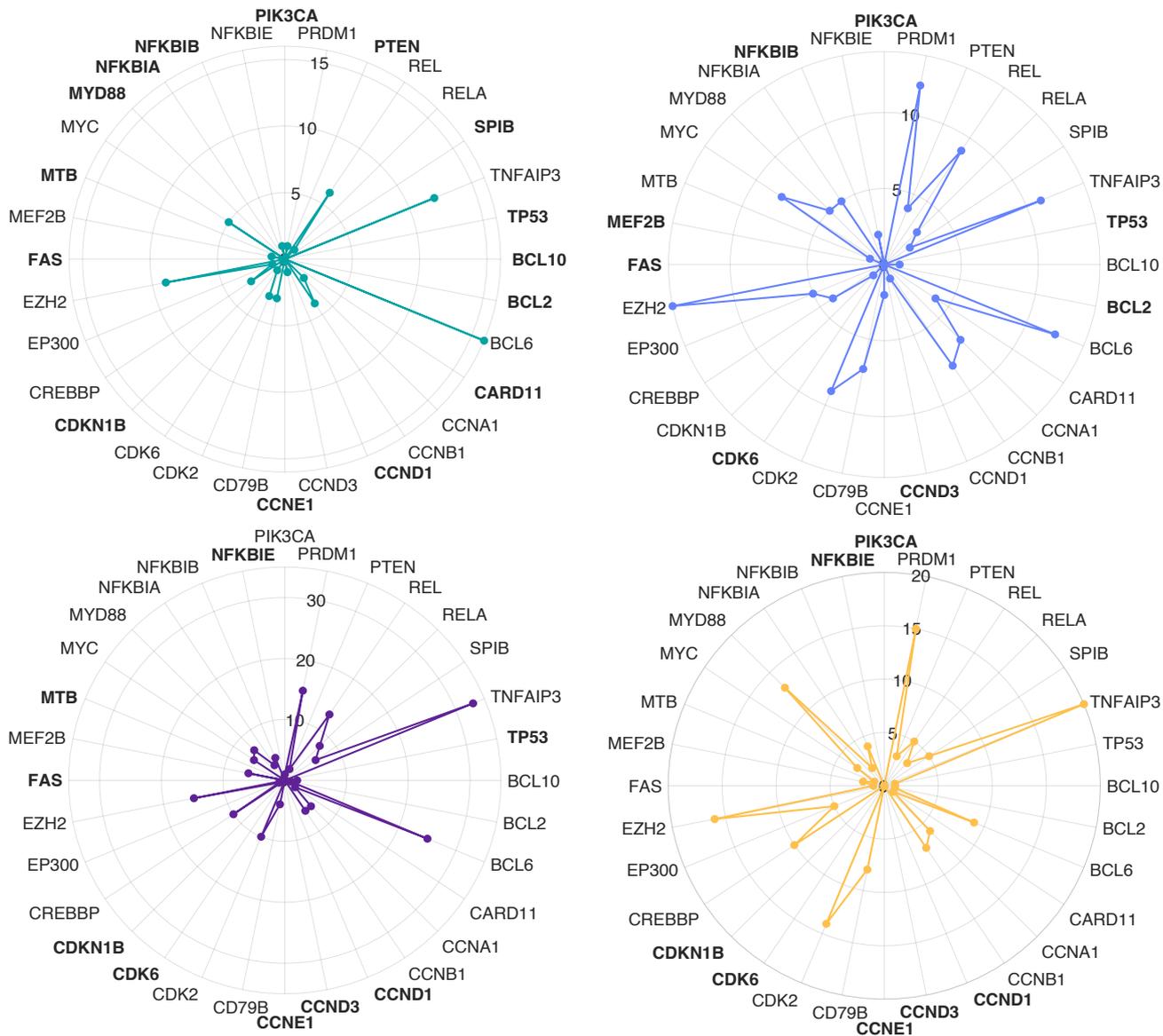
**Figure S3. Predicted cell states for longer simulation time.**

Shown are the cell states of the patient models with a simulation time of 10d (left, compare Fig 2) and a prolonged simulation time of 30d (right) The percentage of patient models with an aberrant state (90.5%) is not changed by the longer simulation time.



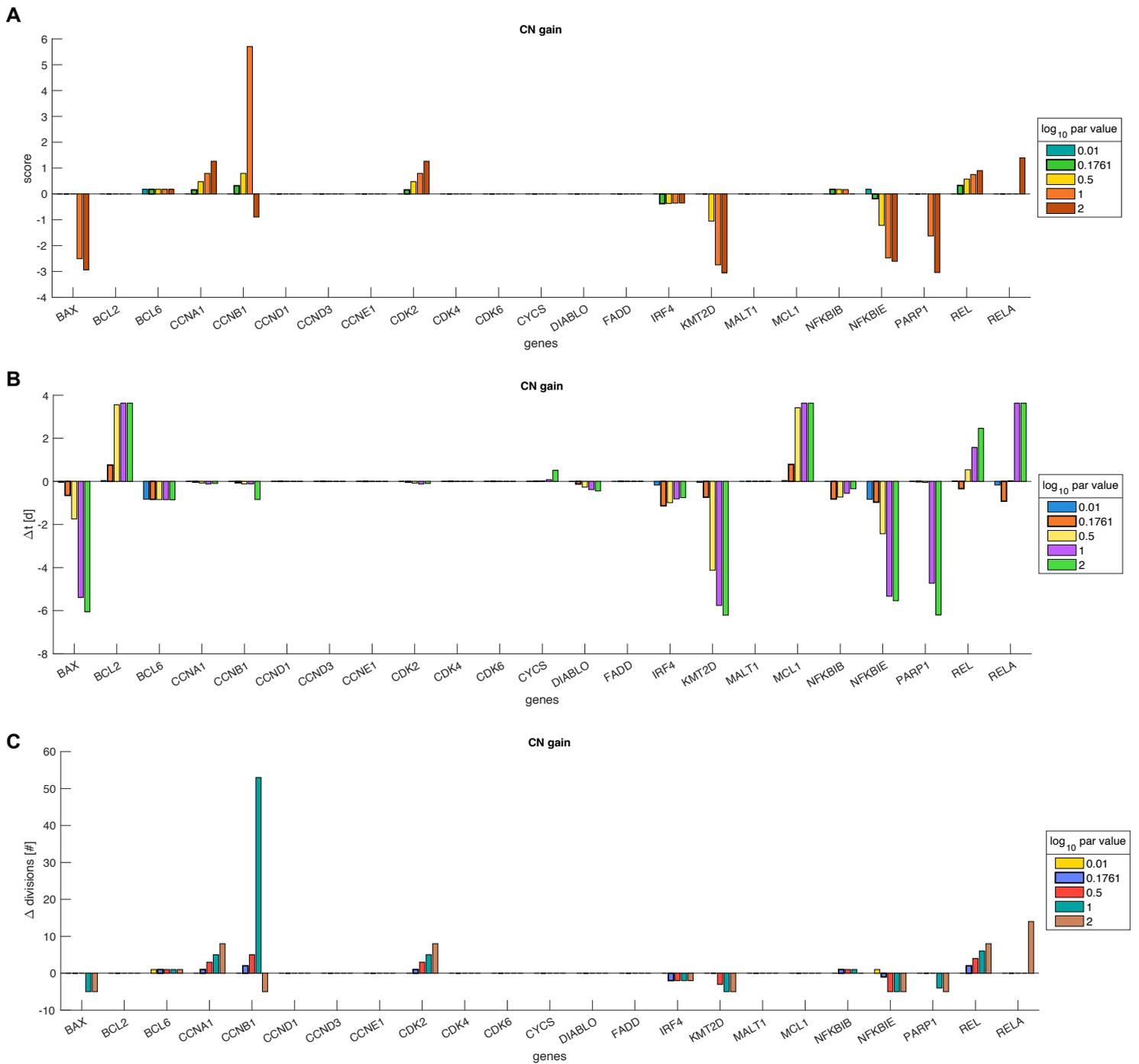
**Figure S4. Simulation results capturing synergistic effects of NFKBIE mutations.**

**(A)** Reducing the transcription rate of BLIMP1/PRDM1 to 0.25 demonstrates the effect of the NFKBIE synergy.  
**(B)** Simulation of patient models in which, NFKBIE is mutated and in addition one of the PRDM1 (BLIMP1)-enhancing alterations (Table S3) is present. The number in brackets gives the number of divisions that are observed for the given patient model.



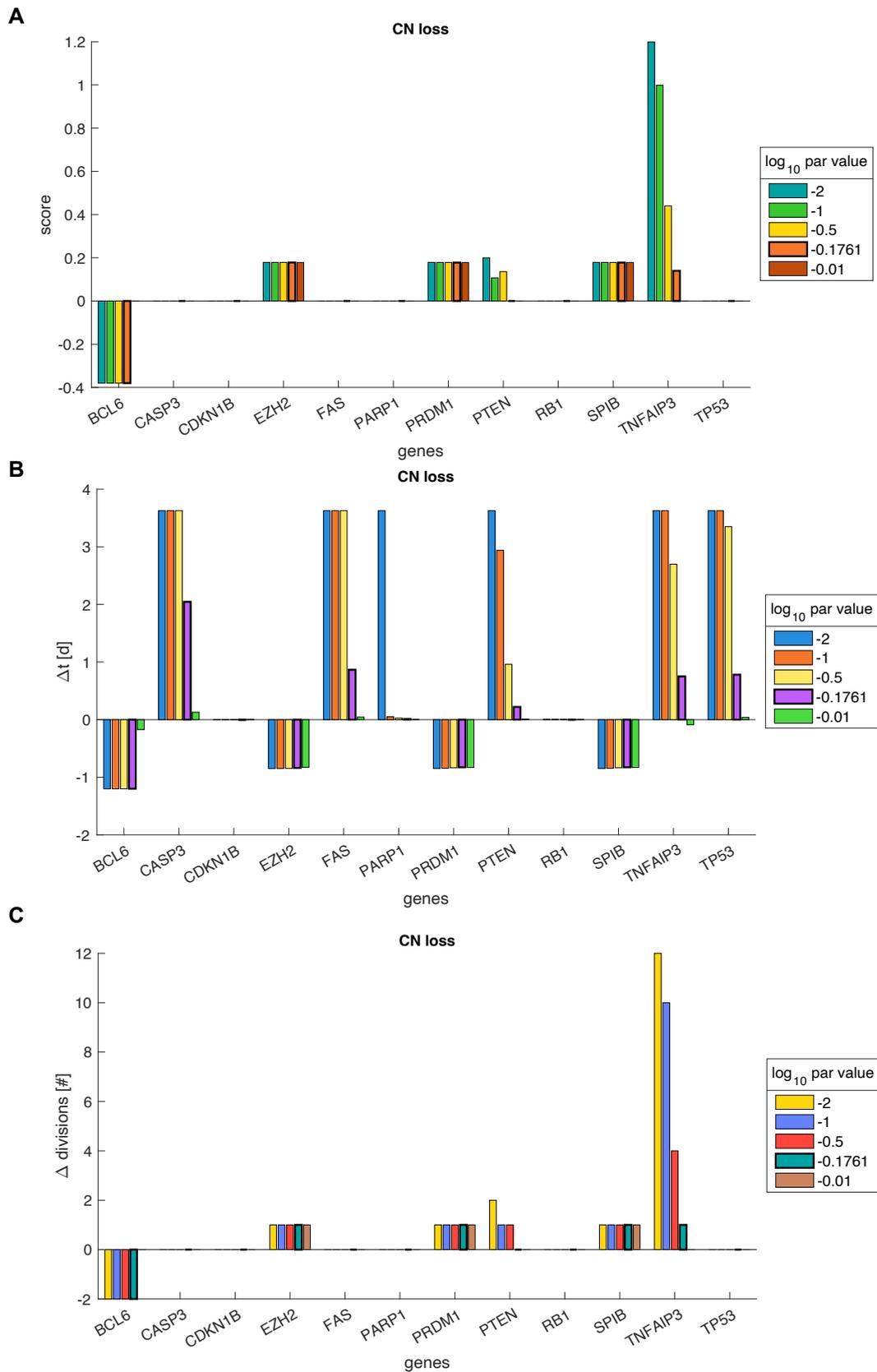
**Figure S5. Frequency of causative genes in patient models based on drop out analyses.**

For the 32 identified causative genes and the supercomplex MTB (labels given on outer circles), the number of patient models (radius) in which they are causative is shown. The four circles represent the different number of required causative genes in accordance to Fig. 5A (upper left: turquoise, one altered gene; upper right: light blue, two altered genes; lower left: purple, three altered genes; lower right: yellow, four altered genes).



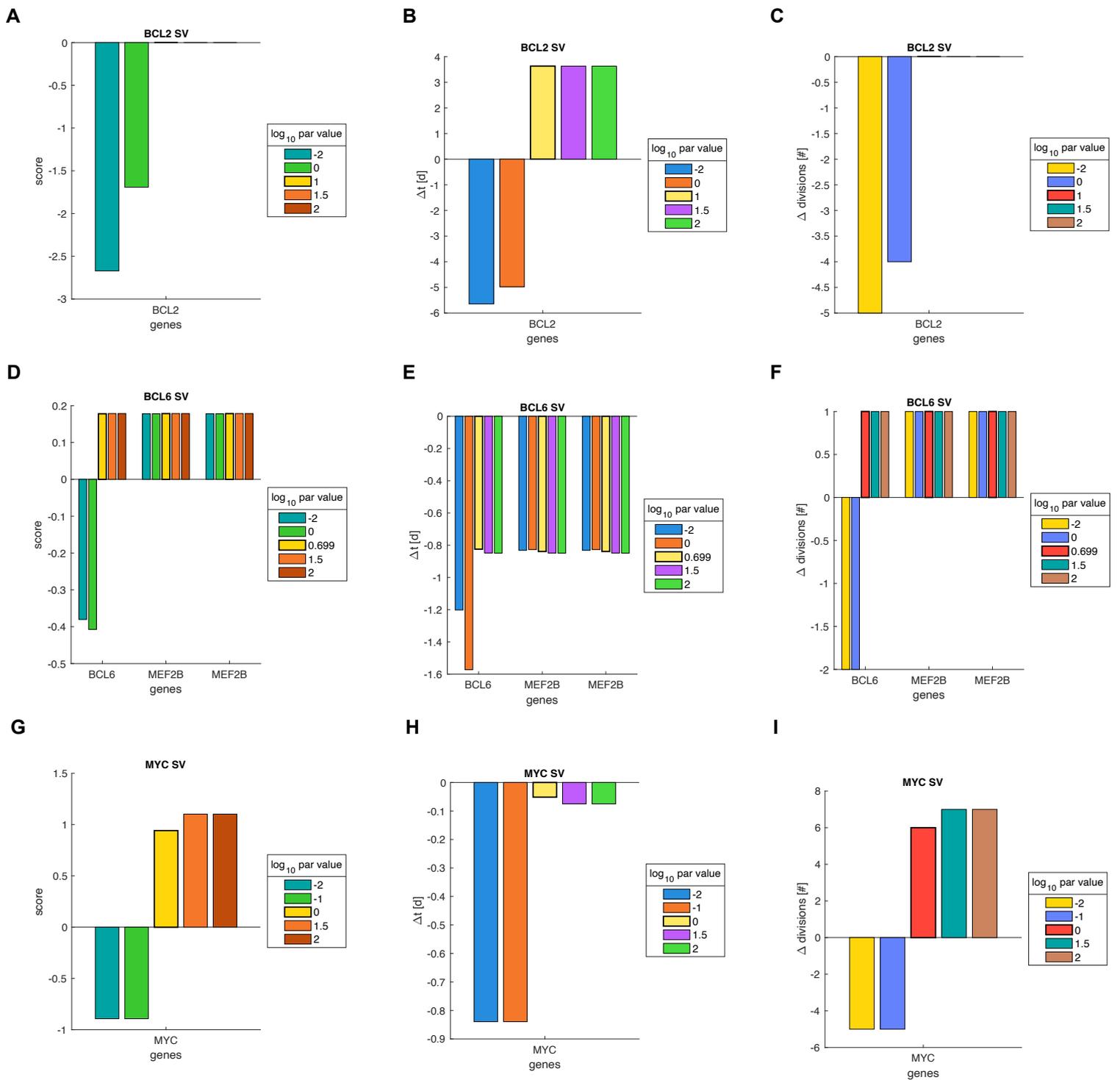
**Figure S6. Perturbation strength analyses for CN gain alterations.**

The effect of multiple perturbation strengths on the score (A), difference in timepoint of apoptosis (B) and difference in division rate (C) was calculated.  $\Delta t = t_{WT} - t$ , where  $t$  is the timepoint of apoptosis for the given perturbation strength.  $\Delta$ divisions = divisions<sub>WT</sub> - divisions, where divisions correspond to the number of divisions for the given alteration strength. For the copy number alterations affecting the score, the increasing perturbation strengths cause stronger effects on the score. The amplifications of the genes BAX and PARP-1 only show an effect on the score if the expression would be strongly increased ( $\log_{10}$  factor  $\geq 1$ ).



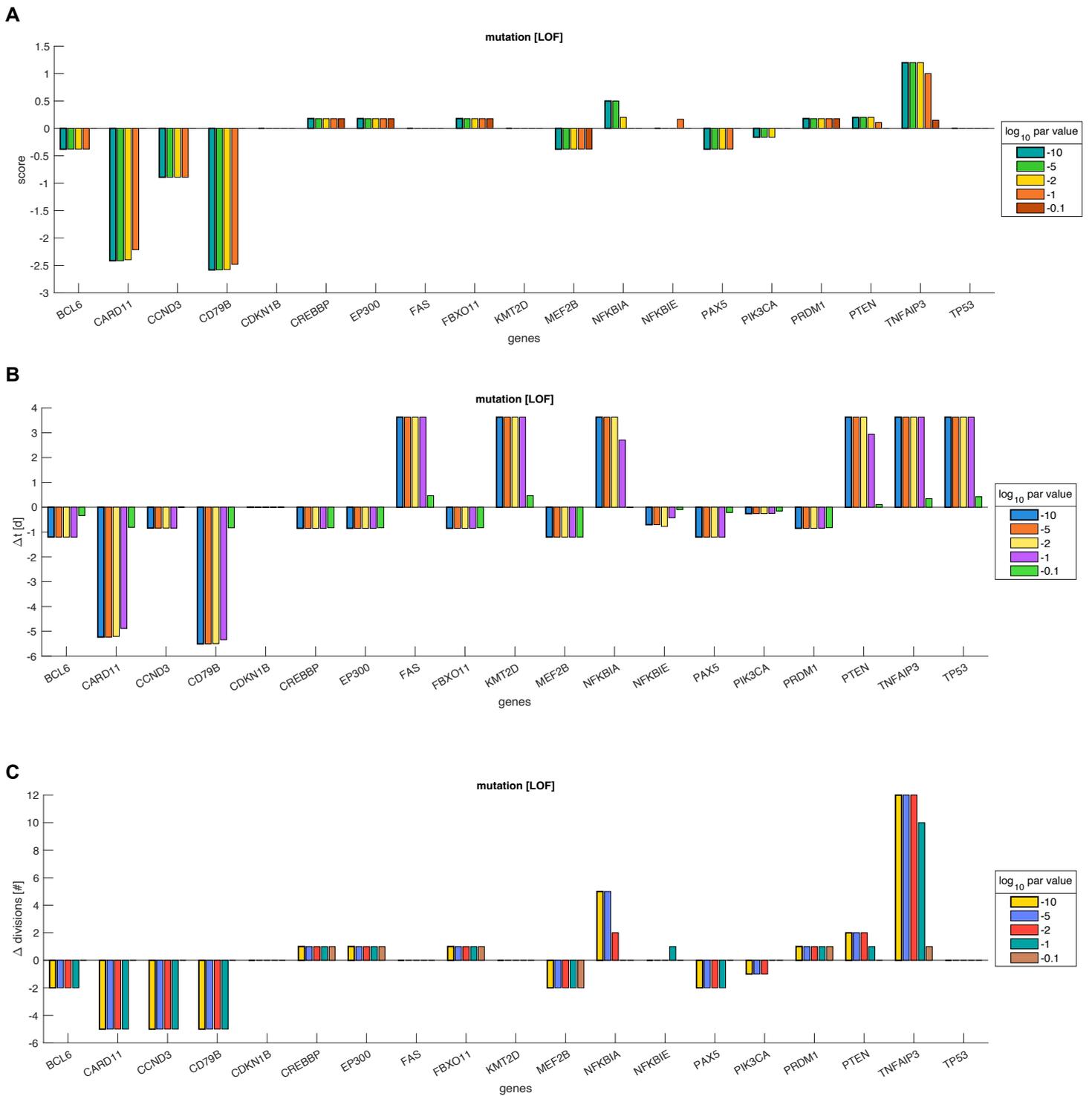
**Figure S7. Perturbation strength analyses for CN loss alterations.**

The effect of multiple perturbation strengths on the score **(A)**, difference in timepoint of apoptosis **(B)** and difference in division rate **(C)** was calculated.  $\Delta t = t_{WT} - t$ , where  $t$  is the timepoint of apoptosis for the given perturbation strength.  $\Delta \text{divisions} = \text{divisions}_{WT} - \text{divisions}$ , where divisions correspond to the number of divisions for the given alteration strength.



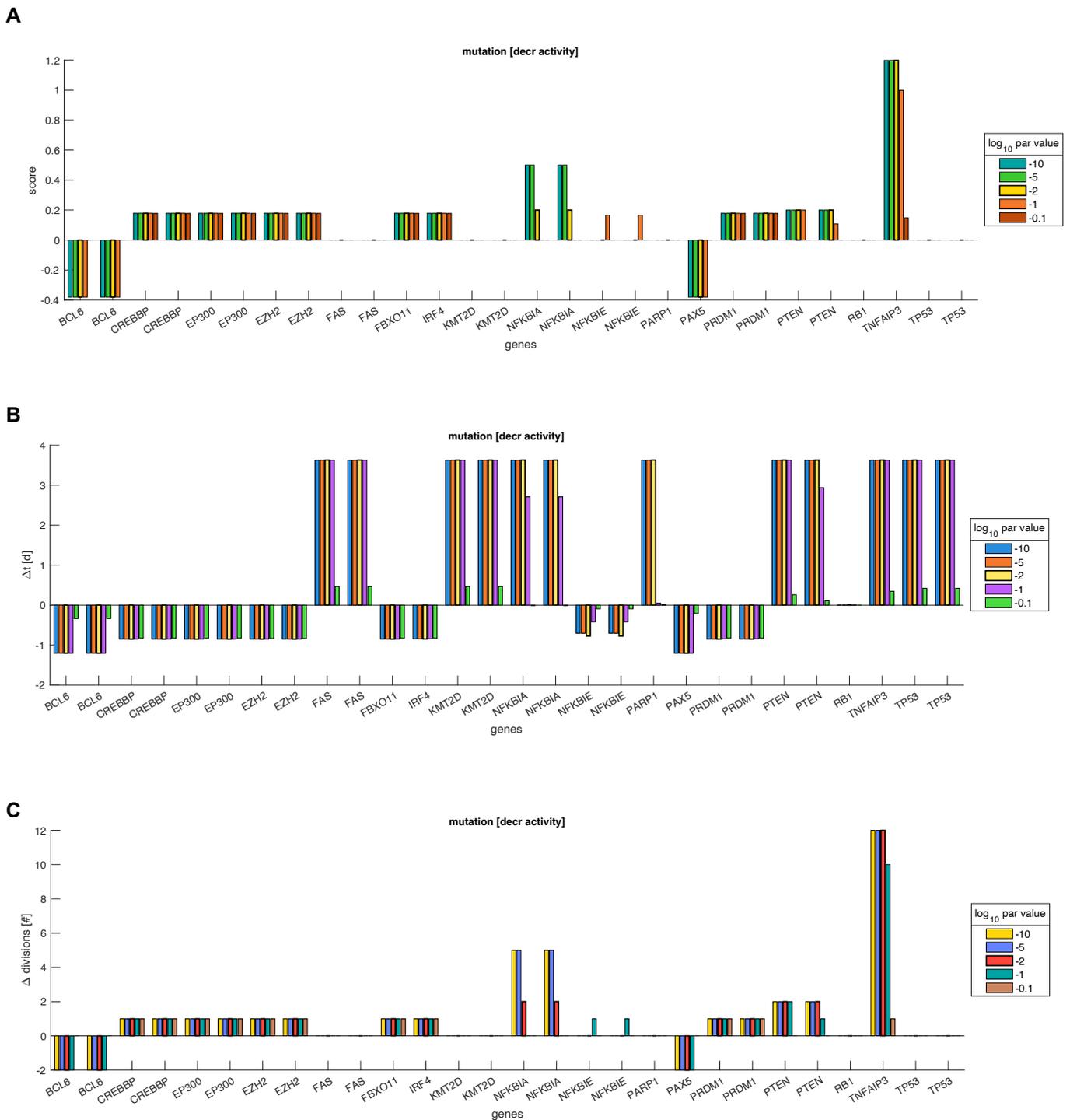
**Figure S8. Perturbation strength analyses for SV alterations.**

The effect of multiple perturbation strengths on the score (A, D, G), difference in timepoint of apoptosis (B, E, H) and difference in division rate (C, F, I) was calculated.  $\Delta t = t_{WT} - t$ , where  $t$  is the timepoint of apoptosis for the given perturbation strength.  $\Delta \text{divisions} = \text{divisions}_{WT} - \text{divisions}$ , where divisions correspond to the number of divisions for the given alteration strength. For *BCL2* SV, we expect an increase in the timepoint of apoptosis. For  $\log_{10}$  values of 0 and -2, the score, the timepoint of apoptosis and the number of divisions is reduced compared to the WT (A-C) and therefore unexpected. The reason for the unexpected effect is the implemented abrogation of its endogenous positive and negative regulation. In the scenario of a translocation, the gene expression is only dependent on the ectopic expression rate. By reducing the ectopic expression rate below a certain value (here  $\log_{10}$  value of 0 or -2), the resulting expression rate of *BCL2* is below the expression rate of the WT. Consequently, the anti-apoptotic effect of *BCL2* is reduced and apoptosis is induced earlier (B) which coincides with less divisions (C). We therefore chose for the ectopic basal expression rate constant a value of 10 a.u./min ( $\log_{10}$  value of 1). For *BCL6* SV and *MYC* SV, an increase in the number of divisions is expected. We therefore chose a value of 5 a.u./min ( $\log_{10}$  value of 0.7) and 1 a.u./min ( $\log_{10}$  value of 0), respectively. The impact of the perturbation strengths on the number of divisions for *BCL6* SV and *MYC* SV is shown in F and I.



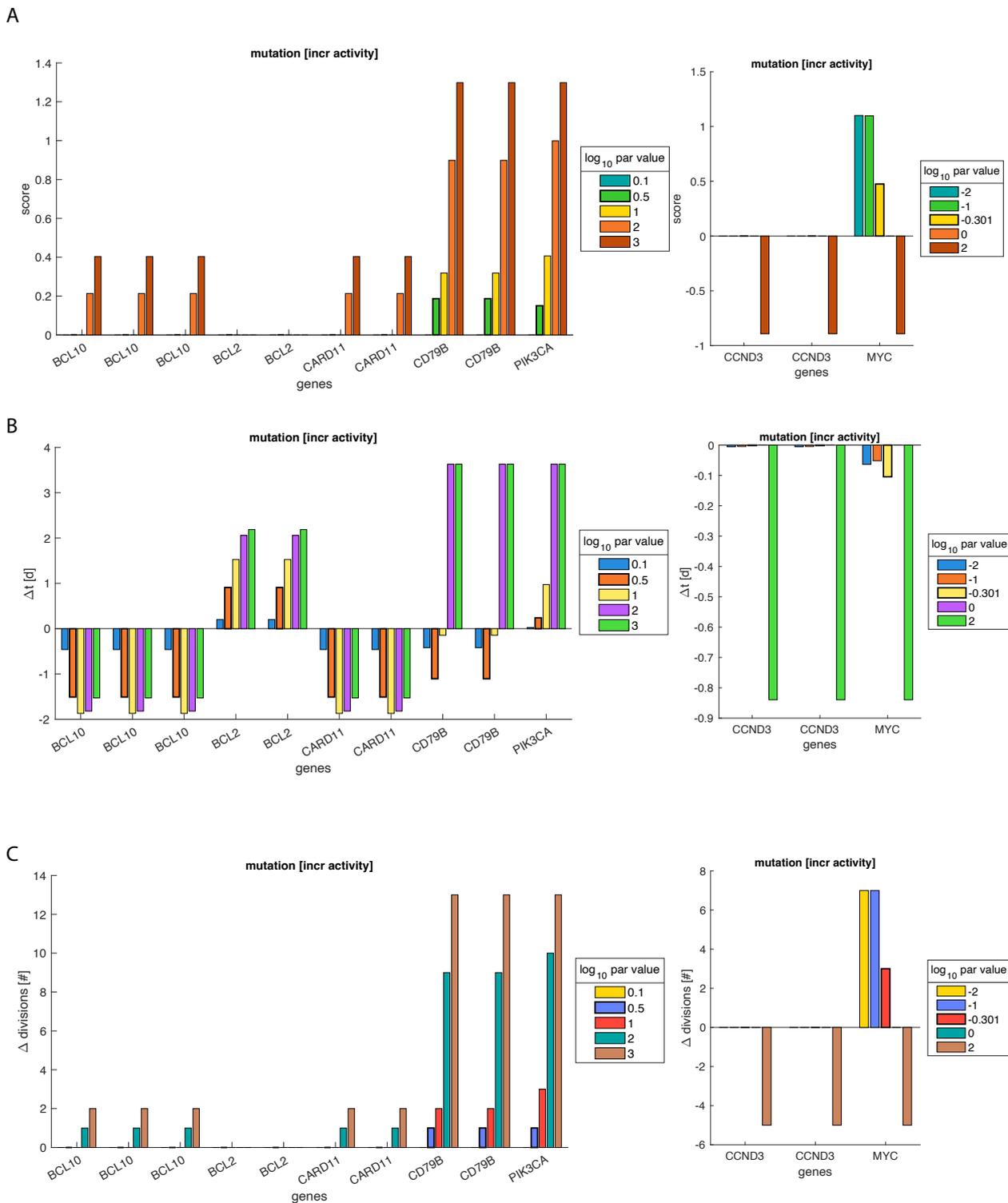
**Figure S9. Perturbation strength analyses for LOF mutations.**

The effect of multiple perturbation strengths on the score (A), difference in timepoint of apoptosis (B) and difference in division rate (C) was calculated.  $\Delta t = t_{WT} - t$ , where  $t$  is the timepoint of apoptosis for the given perturbation strength.  $\Delta \text{divisions} = \text{divisions}_{WT} - \text{divisions}$ , where divisions correspond to the number of divisions for the given alteration strength. For LOF mutations, a value of  $1e-10$  is chosen.



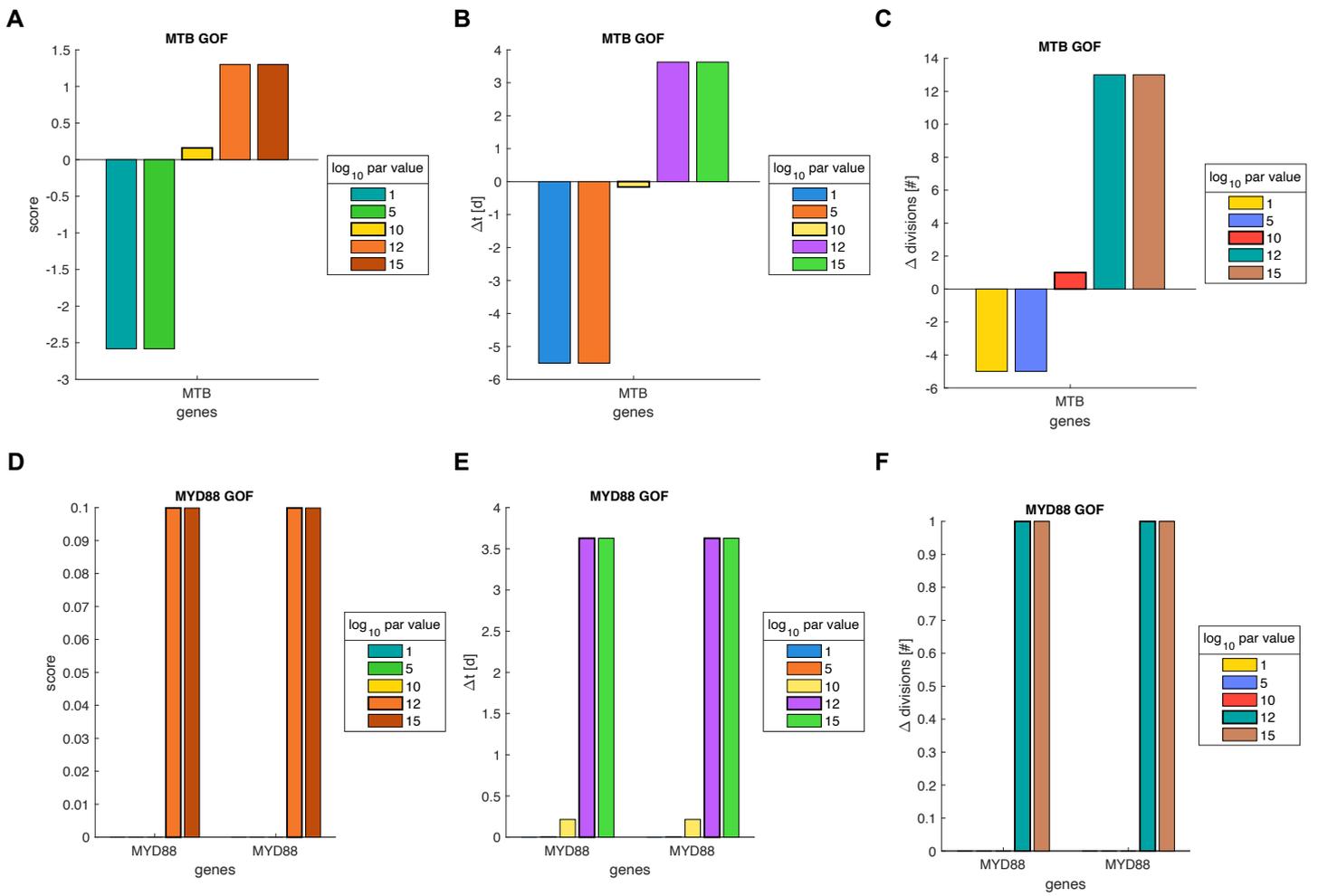
**Figure S10. Perturbation strength analyses for decreased activity mutations.**

The effect of multiple perturbation strengths on the score (A), difference in timepoint of apoptosis (B) and difference in division rate (C) was calculated.  $\Delta t = t_{WT} - t$ , where  $t$  is the timepoint of apoptosis for the given perturbation strength.  $\Delta$  divisions = divisions<sub>WT</sub> - divisions, where divisions correspond to the number of divisions for the given alteration strength. For the MA mutations causing a reduced protein activity, we chose a value of  $1e-2$  as all MA mutations, except *NFKBIE* mutations, show an effect on the score (A). *NFKBIE* mutations show a negative effect on the apoptosis time (B) but only an effect on the score and number of divisions for a  $\log_{10}$  value of  $-1$  (A, C). For lower and higher values, *NFKBIE* mutations show no impact. This is due to the fact that if the activity of NF- $\kappa$ B is too strongly increased by a strong reduction (e.g. factor of  $1e-5$ ) of the functionality of the I $\kappa$ B $\epsilon$  protein (*NFKBIE* gene product), the negative feedback mechanism via I $\kappa$ B $\alpha$  reduces NF- $\kappa$ B activity after an activation overshoot resulting in a shorter lifetime (B) but unchanged number of divisions and therefore an unchanged score (A, C). If the reduction is too small (e.g.  $\log_{10}$  value of  $-0.1$ ) the effect on NF- $\kappa$ B activity is too small to result in any changes on the number of divisions and the score. As the *NFKBIE* mutation effect is specific for a single factor and leads to value-specific results while the effect of *NFKBIA* mutations is dose dependent and valid for a broader range of values, we decided for a factor of  $1e-2$ . Nevertheless, the effect of the MA mutations causing a reduced activity and affecting the score is robust over a wide range of values except for *NFKBIA* and *NFKBIE*.



**Figure S11. Perturbation strength analyses for increased activity mutations.**

The effect of multiple perturbation strengths on the score (**A**), difference in timepoint of apoptosis (**B**) and difference in division rate (**C**) was calculated.  $\Delta t = t_{WT} - t$ , where  $t$  is the timepoint of apoptosis for the given perturbation strength.  $\Delta \text{divisions} = \text{divisions}_{WT} - \text{divisions}$ , where divisions correspond to the number of divisions for the given alteration strength. For the MA mutations causing an increased activity, we chose a  $\log_{10}$  value of 0.5 as this results in effects of the *CD79B*, *MYC* and *PIK3CA* mutations on the score (**A**). However, the chosen value is not sufficient to enable an effect of *BCL10* and *CARD11* missense mutations (for an effect the value would need to be increased very strongly (>100)).



**Figure S12. Perturbation strength analyses for GOF mutations.**

The effect of multiple perturbation strengths on the score (**A, D, G**), difference in timepoint of apoptosis (**B, E, H**) and difference in division rate (**C, F, I**) was calculated.  $\Delta t = t_{WT} - t$ , where  $t$  is the timepoint of apoptosis for the given perturbation strength.  $\Delta \text{divisions} = \text{divisions}_{WT} - \text{divisions}$ , where divisions correspond to the number of divisions for the given alteration strength.

**Table S1. List of implemented modified activity (MA) mutations and gain-of-function (GOF) mutations with the corresponding assigned alteration effect and reference.**

**MA Mutations:**

<b>Gene</b>	<b>Activity</b> increased: + decreased: -	<b>Description</b>	<b>Annotation based on cBioportal &amp; oncoKB <sup>1</sup></b> likely oncogenic: <b>O</b> oncogenic: <b>O+</b> likely GOF: <b>G</b> / likely LOF: <b>L</b> GOF: <b>G+</b> / LOF: <b>L+</b>
<i>BCL10</i>	+	Missense mutation R58Q and non-sense truncation E140X and K146Nfs lead to strongly increased NF-κB activity compared to WT BCL10 [1]. Increased levels of active NF-κB were also observed in DLBCL patients with <i>BCL10</i> mutations [1].	Most frequent missense mutation is R58Q [O/G]. Effect of other missense mutations is unknown. E140* nonsense mutation: [O/G] Other nonsense and frameshift mutations: [O/L]
<i>BCL2</i>	+	Missense mutations in the <i>BCL2</i> gene (G33R and A43T) can increase the affinity of BCL2 towards BIM and PUMA and thereby enhance its anti-apoptotic property [2]. In the model, only the binding of BCL2 to BAX is implemented. Based on the finding that a missense mutation can modify the binding affinity of BCL2 towards pro-apoptotic proteins, we assume that this can also be the case for the binding to BAX.	Several missense mutations: [O/G+] and [O/G]
<i>BCL6</i>	+/-	Missense mutations found in DLBCL can change binding sites of BCL6 and IRF4 to the BCL6 promotor and thereby cause a dysfunctional repression of BCL6 transcription ([3], [4], reviewed in [5]). We also assume that the BLIMP1-mediated repression of BCL6 is impaired as well as the BCL6-mediated repression of BLIMP1 transcription.	Effect of missense/nonsense mutations unknown. Only Fusions: [O/G]
<i>CARD11</i>	+	Multiple point mutations of <i>CARD11</i> cause elevated levels of activated basal NF-κB as well as elevated levels of activated NF-κB upon stimulation [6]. The gain-of-function phenotype was also demonstrated on the level of expression of NF-κB target genes.	Multiple missense mutations: [O+/G+] or [O/G]
<i>CCND3</i>	+	Multiple point mutations of <i>CCND3</i> cause increased levels of Cyclin D3 and consequently enhanced proliferation [7]. The increased protein levels were due to lower degradation rates [7]. Based on the conducted pulse chase experiment [7], we determined a change	Multiple missense mutations: [O+/G+] or [O/G]

		between WT CCND3 and mutated CCND3 in the degradation rate by a factor of around 0.5.	
<i>CD79B</i>	+	The most frequent missense mutations of <i>CD79B</i> in DLBCL (Y197H, Y197S, Y197D, cBioportal) can lead to chronic B-Cell-Receptor activity in DLBCL which promotes NF-κB signaling and AKT signaling [8]. The survival of ABC-DLBCL cell lines with missense mutations in <i>CD79B</i> and chronic B-Cell-Receptor signaling were thereby dependent on <i>CD79B</i> and NF-κB signaling [8].	for missense mutations Y197(C,N,F,H,D,S) and E198G: [O+/G+] or [O/G] other missense mutations: unknown effect
<i>CREBBP</i>	-	Most of tested missense mutations that were found in DLBCL patients are incapable to mediate BCL6 acetylation and therefore strongly reduce repression of BCL6 [9]. As <i>CREBBP</i> is not included in the model, we modulate the level of active BCL6 in presence of <i>CREBBP</i> missense mutations.	Majority of missense mutations: [O/L]
<i>EP300</i>	-	<i>EP300</i> mutations are also found in DLBCL although less frequent than <i>CREBBP</i> mutations [9]. Based on the structural and functional similarity of EP300 and <i>CREBBP</i> [9], we assume for <i>EP300</i> missense mutations a reduced functionality in inhibiting BCL6.	multiple missense mutations: [O/L]; for others unknown effect
<i>EZH2</i>	+	The most frequent missense mutations of <i>EZH2</i> are found for Y641 (Y646) in DLBCL ([10] and cBioportal taking [11], [12], [13], [14] data sets into account). This missense mutation was shown to enhance EZH2-mediated repression of BLIMP1 and IRF4 ([15], [16], reviewed in [5]).	vast majority variant: Y646N/F/H [O/G]
<i>FAS</i>	-	We assume a LOF effect due to the crucial role of FAS in the negative B-Cell selection in the germinal center ([17], [18], [19]). However, there is no information in literature about the experimentally assessed effects of <i>FAS</i> mutations. There is also no information in the oncoKB database about predictions of the oncogenic potential.	For non-sense mutations and fusions: [O/L] For missense mutations the effect is unknown
<i>FBXO11</i>	-	<i>FBXO11</i> missense mutations can reduce the degradation rate of BCL6 and therefore lead to increased BCL6 levels [20].	Non-sense mutations: [O/L] For missense mutations the effect is unknown
<i>IRF4</i>	-	<i>IRF4</i> missense mutations are present in DLBCL mostly in the IRF domain (cBioPortal). Based on the missense mutation (C99R) which is predicted to be likely-oncogenic, we assume a reduced activity of IRF4 which in turn causes reduced i) inhibition of BCL6, ii) expression of BLIMP1 and iii) expression of AID. As BCL6 is an oncogene due to its constitutive activation causing the development of lymphomas [21], the effect of IRF4 on BCL6 activity could link its reduced functionality to the likely-oncogenic effect.	For one missense mutation (C99R): [O/unknown]
<i>KMT2D</i>	-	A reduction in the level of <i>KMT2D</i> affects expression of multiple genes. One of them is the FAS receptor [22]. As most of the point mutations in DLBCL patients are predicted by OncoKB to be likely-LOF and likely-oncogenic, we assume a LOF mutation for <i>KMT2D</i> .	[O/L]

<i>MCL1</i>		The oncogenic effect of <i>MCL1</i> in DLBCL is based on increased protein levels due to copy number gains or upstream signaling events [23]. The frequency of mutations of <i>MCL1</i> in DLBCL are low and the effect is unknown ([24], cBioportal). As we did not find reports about effects of non-sense or LOF mutations, we did not implement an effect for <i>MCL1</i> missense mutations.	effect unknown
<i>MEF2B</i>	+	The transcription factor <i>MEF2B</i> promotes <i>BCL6</i> expression [25]. Missense mutations of <i>MEF2B</i> frequently found in DLBCLs increase the transcriptional activity of <i>MEF2B</i> and enhance <i>BCL6</i> transcription [25]. We therefore implement a GOF effect for <i>MEF2B</i> missense mutations.	multiple mutations: [O+/L+] and [O/L]
<i>MYC</i>	+	Missense mutations can lead to a GOF protein due to less efficient degradation [26] (and can be oncogenic due to impaired/prolonged apoptosis induction [27]) (reviewed in [28]). Based on these reports, we assumed that the level of <i>MYC</i> is increased.	multiple mutations: [O/G]
<i>NFKBIA</i>	-	Based on the effects of deletions and LOF mutations of <i>NFKBIA</i> , the negative regulator of NF- $\kappa$ B is a known tumor suppressor ([29], [30]). Moreover, dysfunctional I $\kappa$ B $\alpha$ can cause constitutive NF- $\kappa$ B activity [31] which is one of the main characteristics of ABCs [32]. Consequently, we assume for the missense mutations of <i>NFKBIA</i> reduced affinity of the I $\kappa$ B $\alpha$ protein for NF- $\kappa$ Bs (RELA:RELA, P50:P50, CREL:P50, RELA:P50).	non-sense mutations: [O/L] missense mutations: unknown
<i>NFKBIE</i>	-	<i>NFKBIE</i> is like <i>NFKBIA</i> a negative regulator of NF- $\kappa$ B activity. Deletions of <i>NFKBIE</i> can cause increased proliferation and survival of B-Cells [33]. Moreover, LOF mutations can be a marker for an aggressive form of chronic lymphocytic leukemia [34] and poor outcome in primary mediastinal B-Cell lymphoma [35]. For the missense mutations of <i>NFKBIE</i> we assume a reduced activity, i.e. reduced binding rates of the corresponding protein I $\kappa$ B $\epsilon$ and NF- $\kappa$ Bs (RELA:RELA, P50:P50, CREL:P50, RELA:P50).	effect unknown
<i>PARP1</i>	-	Based on the predicted likely-LOF and likely-oncogenic function of PARP-1 non-sense mutations by oncoKB ( <a href="https://www.oncoKB.org/gene/PARP1/Truncating%20Mutations">https://www.oncoKB.org/gene/PARP1/Truncating%20Mutations</a> , [36]), we assume for missense mutations a reduced binding affinity towards caspases and thus a reduced amount of cleaved PARP-1.	non-sense mutations: [O/L] missense mutations: effect unknown
<i>PAX5</i>	-	The oncoKB prediction for non-sense mutations of <i>PAX5</i> are likely-LOF with a likely-oncogenic effect. Moreover, one missense mutation (V26G) is likely-LOF and likely-oncogenic as well. Consequently, we assume a reduced activity of <i>PAX5</i> resulting in a reduced synthesis of <i>BCL6</i> and <i>AID</i> .	1 missense mutation (V26G): [O/L] Others: effect unknown
<i>PIK3CA</i>	+	There are three missense mutations of <i>PIK3CA</i> mutations in DLBCL (E545K, R108H, H1047L) with a known GOF resulting in an oncogenic effect (oncoKB, cBioPortal). The gene is found to be frequently mutated in different cancers [37] and mutations can increase the enzymatic activity of PI3K and thereby lead to a constitutive activation of	multiple mutations: [O+/G+]

		AKT [38]. We therefore assume that missense mutations of <i>PIK3CA</i> are activating mutations enhancing the activation of AKT.	
<i>PRDM1</i>	-	Missense mutations of <i>PRDM1</i> can lead to altered splicing and reduced DNA binding affinity [39]. Thus, we assume a reduced level of the protein BLIMP1 ( <i>PRDM1</i> ) that can bind to DNA and repress PAX5 as well as BCL6.	non-sense mutations: [O/L] missense mutations: effect unknown
<i>PTEN</i>	-	Missense mutations are oncogenic or likely-oncogenic due to LOF (oncoKB, cBioportal, [40]).	[O+/L+] and [O/L]
<i>RB1</i>	-	Based on the observation that loss of <i>RB1</i> can cause enhanced proliferation (oncoKB, cBioPortal, [41]) and missense mutations are likely-oncogenic (oncoKB, [42]), we assume for <i>RB1</i> missense mutations a reduced binding affinity for E2F which in turn can lead to increased proliferation.	1 missense mutation: [O/L] Others: unknown effect Multiple nonsense mutations: [O/L]
<i>TNFAIP3</i>	-	Non-sense mutations and indel frameshifts lead to non-functional A20 ( <i>TNFAIP3</i> ) and consequently, as A20 is an inhibitor of NF-κB, constitutive NF-κB activity in Hodgkin lymphoma and primary mediastinal B-Cell lymphoma [43]. <i>TNFAIP3</i> is also frequently mutated in DLBCL and dysfunctional due to mutations or deletions [44]. Re-introducing functional A20 into cell lines, abrogates constitutive activity of NF-κB and restores apoptotic capability and cellular growth arrest ([43], [44]). <i>TNFAIP3</i> (A20) is therefore defined as a tumor suppressor. Seven tested missense mutations of <i>TNFAIP3</i> showed either no effect on NF-κB activity or a much less prominent effect compared to non-sense or indel frameshifts causing a truncated A20 variant [45].	missense mutations: unknown effect multiple nonsense mutations: [O/L]
<i>TP53</i>	-	The <i>TP53</i> gene is the most mutated gene across different cancers [46] and is among the most frequently mutated genes in DLBCL patients with poor outcomes [47]. The majority of mutations are missense mutations located in the DNA binding domain of P53 ([48] and for DLBCL: cBioportal taking [11], [12], [13], [14] data sets into account). Missense mutations in the DNA binding domain can lead to abrogated DNA binding and therefore dysfunctional P53 transcriptional activity [48]. Missense mutations can also cause a GOF of P53 but these variants are mostly associated with promoted metastasis which is not covered by our model and is also not relevant in non-solid tumors [49]. As P53 is not implemented in our model, we capture <i>TP53</i> mutations by altering the synthesis of one of its target genes BAX which is involved in inducing apoptosis. Here, we use additional information to capture the effects of point mutations on transcription of BAX (see Methods, “Defining perturbation strengths” for details).	[O+/L+]

**GOF mutations:**

Gene(s)	Label	Description	prediction oncogenicity
<i>MYD88</i>	MYD88	Most frequent and well-known point mutation in <i>MYD88</i> in DLBCL, specifically ABCs, is L265P [50]. This mutation causes K63-linked polyubiquitination of MYD88 and subsequent activation of NF-κB [51]. Depletion of A20 ( <i>TNFAIP3</i> ) further promotes the MYD88-mediated activation of NF-κB [51]. This GOF mutation alone induces DLBCL in mice [52]. But also other MYD88 variants (M232T, S243N, T294P, S222R) strongly enhance NF-κB activity [50]. To implement MYD88 alterations, we introduce a new term in the model representing a constant activation of IKK in presence of MYD88 GOF mutations (Text S1, eq. 1.142). As A20 can counteract the MYD88-mediated NF-κB activation [51], we included A20 as negative regulator of this process.	especially L265P mutation: [O+/G+] other point mutations: [O/G]
<i>MYD88</i> + <i>CD79A/B</i>	MTB	In (ABC-)DLBCL cell lines and patient samples a My-T-BCR supercomplex was found that causes constitutive B-Cell receptor (BCR) signaling and concomitant NF-κB as well as PI3K activity [53]. The supercomplex consists of the toll-like receptor 9, MYD88, the BCR as well as the CARMA (CARD11-MALT1-BCL10) complex which interact with the IKK complex and thereby induce its activation. It could be shown that ABC-DLBCL cell lines with mutations of <i>CD79A/B</i> and <i>MYD88</i> (L265P) forming the supercomplex are dependent on the toll-like receptor 9, MYD88 as well as CD79A [53]. Based on these observations, we assume that in presence of both, <i>MYD88</i> missense mutations as well as <i>CD79A/B</i> missense mutations, a supercomplex exists that constitutively activates IKK and PI3K. Similar to the <i>MYD88</i> GOF mutation, we introduce in the model a term constantly activating IKK (Text S1, eq. 142) and increased AKT/PI3K-mediated expression of target genes (Text S1, eq. 1.113, 1.114, 1.133).	

<sup>1</sup> Prevalence information based on cBioportal ([54], [55], [56]) and [oncogenic annotation (likely oncogenic: O, oncogenic: O+) and predicted functional effect (likely GOF: G, GOF: G+, likely LOF: L, LOF: L+)] based on oncoKB ([57], [58]). We took the following data sets on DLBCL cohort studies in cBioportal into account: [11], [12], [13], [14].

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**Table S2. List of individual alterations that lead to an aberrant cell state and their induced effect size.** CN gain/loss: Copy number gain/loss, SV: Structural variant, mutation [GOF]: gain-of-function mutation, mutation [MA]: mutation causing modified activity (increased or decreased activity), mutation [LOF]: loss-of-function mutation, mutation [info n/a]: mutation with missing information about the mutation type (LOF or MA).

Gene	alteration type	apoptosis time [d]	div rate [1/d]
TNFAIP3	mutation [info n/a]	10	1.7
	mutation [LOF]	10	1.7
MYC	SV	6.32	1.74
NFKBIA	mutation [LOF]	10	1
MYC	mutation [MA]	6.27	1.28
REL	CN gain	6.04	1.16
CCNB1	CN gain	6.3	1.11
NFKBIA	mutation [info n/a]	10	0.7
	mutation [MA]	10	0.7
PTEN	mutation [info n/a]	10	0.7
	mutation [MA]	10	0.7
	mutation [LOF]	10	0.7
CD79B	mutation [info n/a]	5.27	1.14
	mutation [MA]	5.27	1.14
PRDM1	mutation [LOF]	5.52	1.09
CREBBP	mutation [LOF]	5.52	1.09
EP300	mutation [LOF]	5.52	1.09
FBXO11	mutation [LOF]	5.52	1.09
CREBBP	mutation [info n/a]	5.52	1.09
	mutation [MA]	5.52	1.09
EP300	mutation [info n/a]	5.52	1.09
	mutation [MA]	5.52	1.09
FBXO11	mutation [MA]	5.52	1.09
EZH2	mutation [info n/a]	5.52	1.09
	mutation [MA]	5.52	1.09
PRDM1	mutation [info n/a]	5.52	1.09
	mutation [MA]	5.52	1.09
IRF4	mutation [MA]	5.53	1.09
EZH2	CN gain	5.53	1.08
MEF2B	mutation [info n/a]	5.53	1.08
	mutation [MA]	5.53	1.08
BCL6	CN gain	5.54	1.08
PRDM1	CN loss	5.54	1.08
SPIB	CN gain	5.54	1.08
BCL6	SV	5.55	1.08
NFKBIB	CN gain	5.55	1.08
CDK2	CN gain	6.34	0.95
CCNA1	CN gain	6.34	0.95
PIK3CA	mutation [MA]	6.61	0.91
TNFAIP3	CN loss	7.12	0.84
MYD88	mutation [info n/a]	10	0.6
	mutation [GOF]	10	0.6

**Table S3. Alterations forming a synergistic effect with mutated *NFKBIE*.** CN gain/loss: Copy number gain/loss, SV: Structural variant, mutation [GOF]: gain-of-function mutation, mutation [MA]: mutation causing modified activity (increased or decreased activity), mutation [LOF]: loss-of-function mutation, mutation [info n/a]: mutation with missing information about the mutation type (LOF or MA).

alteration 1	alteration 2	apop [d]	div [1/d]	score	exp. score
BCL6 CN gain	NFKBIE mutation [info n/a]	10	1.6	1.1	0.2
	NFKBIE mutation [MA]	10	1.6	1.1	0.2
BCL6 SV	NFKBIE mutation [info n/a]	10	1.6	1.1	0.2
	NFKBIE mutation [MA]	10	1.6	1.1	0.2
	NFKBIE mutation [LOF]	10	1.8	1.3	0.2
CARD11 mutation [LOF]	NFKBIE mutation [info n/a]	10	1.1	0.6	-2.91
	NFKBIE mutation [MA]	10	1.1	0.6	-2.91
	NFKBIE mutation [LOF]	9.55	0.94	0.42	-2.86
CD79B mutation [LOF]	NFKBIE mutation [info n/a]	10	0.9	0.4	-3.1
	NFKBIE mutation [MA]	10	0.9	0.4	-3.1
	NFKBIE mutation [LOF]	9.35	0.96	0.43	-3.05
CREBBP mutation [LOF]	NFKBIE mutation [info n/a]	10	1.6	1.1	0.21
	NFKBIE mutation [MA]	10	1.6	1.1	0.21
	NFKBIE mutation [LOF]	10	1.8	1.3	0.2
CREBBP mutation [MA]	NFKBIE mutation [info n/a]	10	1.6	1.1	0.21
	NFKBIE mutation [MA]	10	1.6	1.1	0.21
	NFKBIE mutation [LOF]	10	1.8	1.3	0.2
CREBBP mutation [info n/a]	NFKBIE mutation [info n/a]	10	1.6	1.1	0.21
	NFKBIE mutation [MA]	10	1.6	1.1	0.21
	NFKBIE mutation [LOF]	10	1.8	1.3	0.2
EP300 mutation [LOF]	NFKBIE mutation [info n/a]	10	1.6	1.1	0.21
	NFKBIE mutation [MA]	10	1.6	1.1	0.21
	NFKBIE mutation [LOF]	10	1.8	1.3	0.2
EP300 mutation [MA]	NFKBIE mutation [info n/a]	10	1.6	1.1	0.21
	NFKBIE mutation [MA]	10	1.6	1.1	0.21
	NFKBIE mutation [LOF]	10	1.8	1.3	0.2
EP300 mutation [info n/a]	NFKBIE mutation [info n/a]	10	1.6	1.1	0.21
	NFKBIE mutation [MA]	10	1.6	1.1	0.21
	NFKBIE mutation [LOF]	10	1.8	1.3	0.2
EZH2 CN gain	NFKBIE mutation [info n/a]	10	1.6	1.1	0.21
	NFKBIE mutation [MA]	10	1.6	1.1	0.21
	NFKBIE mutation [LOF]	10	1.8	1.3	0.2
EZH2 mutation [MA]	NFKBIE mutation [info n/a]	10	1.6	1.1	0.21
	NFKBIE mutation [MA]	10	1.6	1.1	0.21
	NFKBIE mutation [LOF]	10	1.8	1.3	0.2
EZH2 mutation [info n/a]	NFKBIE mutation [info n/a]	10	1.6	1.1	0.21
	NFKBIE mutation [MA]	10	1.6	1.1	0.21
	NFKBIE mutation [LOF]	10	1.8	1.3	0.2
FBXO11 mutation [LOF]	NFKBIE mutation [info n/a]	10	1.6	1.1	0.21
	NFKBIE mutation [MA]	10	1.6	1.1	0.21
	NFKBIE mutation [LOF]	10	1.8	1.3	0.2
FBXO11 mutation [MA]	NFKBIE mutation [info n/a]	10	1.6	1.1	0.21
	NFKBIE mutation [MA]	10	1.6	1.1	0.21
	NFKBIE mutation [LOF]	10	1.8	1.3	0.2
IRF4 mutation [MA]	NFKBIE mutation [info n/a]	10	1.6	1.1	0.21
	NFKBIE mutation [MA]	10	1.6	1.1	0.21
	NFKBIE mutation [LOF]	10	1.8	1.3	0.2
MEF2B mutation [MA]	NFKBIE mutation [info n/a]	10	1.6	1.1	0.21
	NFKBIE mutation [MA]	10	1.6	1.1	0.21

<b>alteration 1</b>	<b>alteration 2</b>	<b>apop [d]</b>	<b>div [1/d]</b>	<b>score</b>	<b>exp. score</b>
	NFKBIE mutation [LOF]	10	1.8	1.3	0.2
MEF2B mutation [info n/a]	NFKBIE mutation [info n/a]	10	1.6	1.1	0.21
	NFKBIE mutation [MA]	10	1.6	1.1	0.21
	NFKBIE mutation [LOF]	10	1.8	1.3	0.2
PRDM1 mutation [LOF]	NFKBIE mutation [info n/a]	10	1.6	1.1	0.21
	NFKBIE mutation [MA]	10	1.6	1.1	0.21
	NFKBIE mutation [LOF]	10	1.8	1.3	0.2
PRDM1 mutation [MA]	NFKBIE mutation [info n/a]	10	1.6	1.1	0.21
	NFKBIE mutation [MA]	10	1.6	1.1	0.21
	NFKBIE mutation [LOF]	10	1.8	1.3	0.2
PRDM1 mutation [info n/a]	NFKBIE mutation [info n/a]	10	1.6	1.1	0.21
	NFKBIE mutation [MA]	10	1.6	1.1	0.21
	NFKBIE mutation [LOF]	10	1.8	1.3	0.2

**Table S4. Implementation of alterations.** CN gain/loss: Copy number gain/loss, SV: Structural variant, mutation [GOF]: gain-of-function mutation, mutation [MA]: mutation causing modified activity (increased or decreased activity), mutation [LOF]: loss-of-function mutation, mutation [info n/a]: mutation with missing information about the mutation type (LOF or MA).

Gene	alteration type	parameter_label	log10_parameter_value	implementation
APAF1	CN gain	init_Apaf	0.17609	direct
BAX	CN gain	k86	0.17609	direct
BCL10	mutation [info n/a]	pikk1	0.5	indirect
	mutation [info n/a]	pikk3	0.5	indirect
	mutation [MA]	pikk1	0.5	indirect
	mutation [MA]	pikk3	0.5	indirect
	mutation [LOF]	pikk1	0.5	indirect
	mutation [LOF]	pikk3	0.5	indirect
BCL2	CN gain	k2.80	0.17609	direct
	mutation [info n/a]	k36	0.5	direct
	mutation [info n/a]	k40	0.5	direct
	mutation [info n/a]	k44	0.5	direct
	mutation [MA]	k36	0.5	direct
	mutation [MA]	k40	0.5	direct
	mutation [MA]	k44	0.5	direct
	SV	ke_bcl2	1	direct
	SV	k2.80	-10	direct
BCL6	CN gain	kASC42	0.17609	direct
	CN loss	kASC42	-0.17609	direct
	mutation [info n/a]	k_bclRep	-2	direct
	mutation [info n/a]	k_bclRep2	-2	direct
	mutation [MA]	k_bclRep	-2	direct
	mutation [MA]	k_bclRep2	-2	direct
	mutation [LOF]	k_bclRep	-10	direct
	mutation [LOF]	k_bclRep2	-10	direct
	SV	ke_bcl6	0.69897	direct
	SV	kASC42	-10	direct
	SV	k_bclRep	-10	direct
CARD11	mutation [info n/a]	pikk1	0.5	indirect
	mutation [info n/a]	pikk3	0.5	indirect
	mutation [MA]	pikk1	0.5	indirect
	mutation [MA]	pikk3	0.5	indirect
	mutation [LOF]	pikk1	-10	indirect
	mutation [LOF]	pikk3	-10	indirect
CASP3	CN loss	k101	-0.17609	direct
CCNA1	CN gain	k2.21	0.17609	direct
CCNB1	CN gain	k2.23	0.17609	direct
	CN gain	k2.24	0.17609	direct
CCND1	CN gain	k2.78	0.17609	direct
CCND3	CN gain	k2.78	0.17609	indirect
	mutation [info n/a]	k2.9	-0.30103	indirect
	mutation [MA]	k2.9	-0.30103	indirect
	mutation [LOF]	k2.10	-10	indirect
CCNE1	mutation [LOF]	k2.36	-10	indirect
	CN gain	k2.12	0.17609	direct
	CN gain	k2.13	0.17609	direct
	mutation [info n/a]	pikk1	0.5	indirect
CD79B	mutation [info n/a]	pikk3	0.5	indirect
	mutation [info n/a]	kp_PMBC	0.5	indirect
	mutation [info n/a]			

Gene	alteration type	parameter_label	log10_parameter_value	implementation
	mutation [MA]	pikk1	0.5	indirect
	mutation [MA]	pikk3	0.5	indirect
	mutation [MA]	kp_PMBC	0.5	indirect
	mutation [LOF]	pikk1	-10	indirect
	mutation [LOF]	pikk3	-10	indirect
	mutation [LOF]	kp_PMBC	-10	indirect
CDK2	CN gain	k2.21	0.17609	indirect
	CN gain	k2.12	0.17609	indirect
	CN gain	k2.13	0.17609	indirect
CDK4	CN gain	k2.78	0.17609	indirect
CDK6	CN gain	k2.78	0.17609	indirect
CDKN1B	CN loss	k2.29	-0.17609	direct
	mutation [LOF]	k2.29	-10	direct
CREBBP	mutation [info n/a]	kASC48	-2	indirect
	mutation [MA]	kASC48	-2	indirect
	mutation [LOF]	kASC48	-10	indirect
CYCS	CN gain	k113	0.17609	direct
DIABLO	CN gain	k97	0.17609	direct
EP300	mutation [info n/a]	kASC48	-2	indirect
	mutation [MA]	kASC48	-2	indirect
	mutation [LOF]	kASC48	-10	indirect
EZH2	CN gain	kASC22	-0.17609	indirect
	CN gain	kASC15	-0.17609	indirect
	CN gain	kASC12	-0.17609	indirect
	mutation [info n/a]	kASC22	-2	indirect
	mutation [info n/a]	kASC15	-2	indirect
	mutation [info n/a]	kASC12	-2	indirect
	mutation [MA]	kASC22	-2	indirect
	mutation [MA]	kASC15	-2	indirect
	mutation [MA]	kASC12	-2	indirect
FADD	CN gain	k3	0.17609	indirect
FAS	CN loss	k71	-0.17609	direct
	mutation [info n/a]	k1	-2	direct
	mutation [MA]	k1	-2	direct
	mutation [LOF]	k1	-10	direct
FBXO11	mutation [MA]	kASC48	-2	indirect
	mutation [LOF]	kASC48	-10	indirect
IRF4	CN gain	kASC15	0.17609	direct
	mutation [MA]	kirfmut	-2	direct
KMT2D	CN gain	k71	0.17609	indirect
	mutation [info n/a]	k71	-2	indirect
	mutation [MA]	k71	-2	indirect
	mutation [LOF]	k71	-10	indirect
MALT1	CN gain	pikk7	0.17609	indirect
MCL1	CN gain	k_mcl	0.17609	direct
MEF2B	mutation [info n/a]	ke_bcl6	0.69897	indirect
	mutation [MA]	ke_bcl6	0.69897	indirect
	mutation [LOF]	kASC42	-10	indirect
MYC	mutation [MA]	k2.86	-0.30103	direct

Gene	alteration type	parameter_label	log10_parameter_value	implementation
MYC	SV	ke_myc	0	direct
	SV	k2.85	-10	direct
MYD88	mutation [info n/a]	ktlr	12	indirect
	mutation [GOF]	ktlr	12	indirect
NFKBIA	mutation [info n/a]	pdi111	-2	direct
	mutation [info n/a]	pdi211	-2	direct
	mutation [info n/a]	pdi121	-2	direct
	mutation [info n/a]	pdi221	-2	direct
	mutation [info n/a]	pdi131	-2	direct
	mutation [info n/a]	pdi231	-2	direct
	mutation [info n/a]	pdi141	-2	direct
	mutation [info n/a]	pdi241	-2	direct
	mutation [MA]	pdi111	-2	direct
	mutation [MA]	pdi211	-2	direct
	mutation [MA]	pdi121	-2	direct
	mutation [MA]	pdi221	-2	direct
	mutation [MA]	pdi131	-2	direct
	mutation [MA]	pdi231	-2	direct
	mutation [MA]	pdi141	-2	direct
	mutation [MA]	pdi241	-2	direct
	mutation [LOF]	pdi111	-10	direct
	mutation [LOF]	pdi211	-10	direct
	mutation [LOF]	pdi121	-10	direct
	mutation [LOF]	pdi221	-10	direct
mutation [LOF]	pdi131	-10	direct	
mutation [LOF]	pdi231	-10	direct	
mutation [LOF]	pdi141	-10	direct	
mutation [LOF]	pdi241	-10	direct	
NFKBIB	CN gain	pii12	0.17609	direct
NFKBIE	CN gain	pii13	0.17609	direct
	mutation [info n/a]	pdi113	-2	direct
	mutation [info n/a]	pdi213	-2	direct
	mutation [info n/a]	pdi123	-2	direct
	mutation [info n/a]	pdi223	-2	direct
	mutation [info n/a]	pdi133	-2	direct
	mutation [info n/a]	pdi233	-2	direct
	mutation [info n/a]	pdi143	-2	direct
	mutation [info n/a]	pdi243	-2	direct
	mutation [MA]	pdi113	-2	direct
	mutation [MA]	pdi213	-2	direct
	mutation [MA]	pdi123	-2	direct
	mutation [MA]	pdi223	-2	direct
	mutation [MA]	pdi133	-2	direct
	mutation [MA]	pdi233	-2	direct
	mutation [MA]	pdi143	-2	direct
	mutation [MA]	pdi243	-2	direct
	mutation [LOF]	pdi113	-10	direct
	mutation [LOF]	pdi213	-10	direct
	mutation [LOF]	pdi123	-10	direct
mutation [LOF]	pdi223	-10	direct	

Gene	alteration type	parameter_label	log10_parameter_value	implementation
	mutation [LOF]	pdi133	-10	direct
	mutation [LOF]	pdi233	-10	direct
	mutation [LOF]	pdi143	-10	direct
	mutation [LOF]	pdi243	-10	direct
PARP1	CN gain	k108	0.17609	direct
	CN loss	k108	-0.17609	direct
	mutation [MA]	k23	-2	direct
PAX5	mutation [MA]	kpax5mut	-2	direct
	mutation [LOF]	kpax5mut	-10	direct
PIK3CA	mutation [MA]	pakt1	0.5	indirect
	mutation [MA]	pakt3	0.5	indirect
	mutation [LOF]	pakt1	-10	indirect
	mutation [LOF]	pakt3	-10	indirect
PRDM1	CN loss	kASC22	-0.17609	direct
	mutation [info n/a]	kASC22	-2	direct
	mutation [MA]	kASC22	-2	direct
	mutation [LOF]	kASC22	-10	direct
PTEN	CN loss	pakt4	-0.17609	direct
	mutation [info n/a]	kpi3kmut	-2	direct
	mutation [info n/a]	kpi3kmut	-2	direct
	mutation [MA]	kpi3kmut	-2	direct
	mutation [LOF]	kpi3kmut	-10	direct
RB1	CN gain	init_ppRb	0.17609	direct
	CN gain	init_Rb	0.17609	direct
	CN gain	init_E2FRb	0.17609	direct
	CN gain	init_pE2FRb	0.17609	direct
	CN loss	init_ppRb	-0.17609	direct
	CN loss	init_Rb	-0.17609	direct
	CN loss	init_E2FRb	-0.17609	direct
	CN loss	init_pE2FRb	-0.17609	direct
	mutation [MA]	k2.72	-2	direct
REL	CN gain	pm13	0.17609	direct
RELA	CN gain	pm11	0.17609	direct
SPIB	CN gain	kASC22	-0.17609	indirect
TNFAIP3	CN loss	pikk4	-0.17609	direct
	mutation [info n/a]	ka20mut	-2	direct
	mutation [LOF]	ka20mut	-10	direct
TP53	CN loss	k86	-0.17609	indirect
	mutation [info n/a]	k86	-2	indirect
	mutation [MA]	k86	-2	indirect
	mutation [LOF]	k86	-10	indirect

# 1 ODE system

$$\frac{d(tIkBa)}{dt} = \frac{pii\_11 \cdot \left( pdi\_721 \cdot \left( \frac{A50n}{pii\_101} \right)^{pii\_91} + pdi\_711 \cdot \left( \frac{AA_n}{pii\_101} \right)^{pii\_91} + pdi\_741 \cdot \left( \frac{C50n}{pii\_101} \right)^{pii\_91} + 1 \right)}{\left( \frac{A50n}{pii\_101} \right)^{pii\_91} + \left( \frac{AA_n}{pii\_101} \right)^{pii\_91} + \left( \frac{C50n}{pii\_101} \right)^{pii\_91} + 1} - pii\_21 \cdot tIkBa \quad (1.1)$$

$$\begin{aligned} \frac{d(IkBa)}{dt} = & IkBaA50 \cdot pd\_112 + IkBaC50 \cdot pd\_114 + IkBaAA \cdot pd\_111 + IkBa5050 \cdot pd\_113 + IkBaA50 \cdot pdi\_321 + IkBaAA \cdot pdi\_311 \\ & + IkBaC50 \cdot pdi\_341 + IkBa5050 \cdot pdi\_331 - IkBa \cdot pii\_41 - IkBa \cdot pii\_61 + IkBan \cdot pii\_71 - A50 \cdot IkBa \cdot pdi\_121 \\ & - AA \cdot IkBa \cdot pdi\_111 - C50 \cdot IkBa \cdot pdi\_141 - IkBa \cdot P50P50 \cdot pdi\_131 - IkBa \cdot pIKK \cdot pii\_111 + k2\_77 \cdot pii\_31 \cdot tIkBa \end{aligned} \quad (1.2)$$

$$\begin{aligned} \frac{d(IkBan)}{dt} = & IkBaA50n \cdot pd\_122 + IkBaC50n \cdot pd\_124 + IkBaAA_n \cdot pd\_121 + IkBa5050n \cdot pd\_123 + IkBaA50n \cdot pdi\_421 \\ & + IkBaAA_n \cdot pdi\_411 + IkBaC50n \cdot pdi\_441 + IkBa5050n \cdot pdi\_431 + IkBa \cdot pii\_61 - IkBan \cdot pii\_51 - IkBan \\ & \cdot pii\_71 - A50n \cdot IkBan \cdot pdi\_221 - AA_n \cdot IkBan \cdot pdi\_211 - C50n \cdot IkBan \cdot pdi\_241 - IkBan \cdot P50P50n \cdot pdi\_231 \end{aligned} \quad (1.3)$$

$$\frac{d(tIkBb)}{dt} = \frac{pii\_12 \cdot \left( pdi\_722 \cdot \left( \frac{A50n}{pii\_102} \right)^{pii\_92} + pdi\_712 \cdot \left( \frac{AA_n}{pii\_102} \right)^{pii\_92} + pdi\_742 \cdot \left( \frac{C50n}{pii\_102} \right)^{pii\_92} + 1 \right)}{\left( \frac{A50n}{pii\_102} \right)^{pii\_92} + \left( \frac{AA_n}{pii\_102} \right)^{pii\_92} + \left( \frac{C50n}{pii\_102} \right)^{pii\_92} + 1} - pii\_22 \cdot tIkBb \quad (1.4)$$

$$\begin{aligned} \frac{d(IkBb)}{dt} = & IkBbA50 \cdot pd\_112 + IkBbC50 \cdot pd\_114 + IkBbAA \cdot pd\_111 + IkBb5050 \cdot pd\_113 + IkBbA50 \cdot pdi\_322 + IkBbAA \cdot pdi\_312 \\ & + IkBbC50 \cdot pdi\_342 + IkBb5050 \cdot pdi\_332 - IkBb \cdot pii\_42 - IkBb \cdot pii\_62 + IkBbn \cdot pii\_72 - A50 \cdot IkBb \cdot pdi\_122 \\ & - AA \cdot IkBb \cdot pdi\_112 - C50 \cdot IkBb \cdot pdi\_142 - IkBb \cdot P50P50 \cdot pdi\_132 - IkBb \cdot pIKK \cdot pii\_112 + k2\_77 \cdot pii\_32 \cdot tIkBb \end{aligned} \quad (1.5)$$

$$\begin{aligned} \frac{d(\text{IkBbn})}{dt} = & \text{IkBbA50n} \cdot \text{pd}_{.122} + \text{IkBbC50n} \cdot \text{pd}_{.124} + \text{IkBbAAAn} \cdot \text{pd}_{.121} + \text{IkBb5050n} \cdot \text{pd}_{.123} + \text{IkBbA50n} \cdot \text{pdi}_{.422} \\ & + \text{IkBbAAAn} \cdot \text{pdi}_{.412} + \text{IkBbC50n} \cdot \text{pdi}_{.442} + \text{IkBb5050n} \cdot \text{pdi}_{.432} + \text{IkBb} \cdot \text{pii}_{.62} - \text{IkBbn} \cdot \text{pii}_{.52} - \text{IkBbn} \\ & \cdot \text{pii}_{.72} - \text{A50n} \cdot \text{IkBbn} \cdot \text{pdi}_{.222} - \text{AAAn} \cdot \text{IkBbn} \cdot \text{pdi}_{.212} - \text{C50n} \cdot \text{IkBbn} \cdot \text{pdi}_{.242} - \text{IkBbn} \cdot \text{P50P50n} \cdot \text{pdi}_{.232} \end{aligned} \quad (1.6)$$

$$\frac{d(\text{tIkBe})}{dt} = \text{kdel}_{.e1} \cdot \text{tpre}_{\text{IkBe1}} - \text{pii}_{.23} \cdot \text{tIkBe} + \frac{\text{pii}_{.13}}{\left(\frac{\text{A50n}}{\text{pii}_{.103}}\right)^{\text{pii}_{.93}} + \left(\frac{\text{AAAn}}{\text{pii}_{.103}}\right)^{\text{pii}_{.93}} + \left(\frac{\text{C50n}}{\text{pii}_{.103}}\right)^{\text{pii}_{.93}} + 1} \quad (1.7)$$

$$\begin{aligned} \frac{d(\text{IkBe})}{dt} = & \text{IkBeA50} \cdot \text{pd}_{.112} + \text{IkBeC50} \cdot \text{pd}_{.114} + \text{IkBeAA} \cdot \text{pd}_{.111} + \text{IkBe5050} \cdot \text{pd}_{.113} + \text{IkBeA50} \cdot \text{pdi}_{.323} + \text{IkBeAA} \cdot \text{pdi}_{.313} \\ & + \text{IkBeC50} \cdot \text{pdi}_{.343} + \text{IkBe5050} \cdot \text{pdi}_{.333} - \text{IkBe} \cdot \text{pii}_{.43} - \text{IkBe} \cdot \text{pii}_{.63} + \text{IkBen} \cdot \text{pii}_{.73} - \text{A50} \cdot \text{IkBe} \cdot \text{pdi}_{.123} - \text{AA} \\ & \cdot \text{IkBe} \cdot \text{pdi}_{.113} - \text{C50} \cdot \text{IkBe} \cdot \text{pdi}_{.143} - \text{IkBe} \cdot \text{P50P50} \cdot \text{pdi}_{.133} - \text{IkBe} \cdot \text{pIKK} \cdot \text{pii}_{.113} + \text{k2}_{.77} \cdot \text{pii}_{.33} \cdot \text{tIkBe} \end{aligned} \quad (1.8)$$

$$\begin{aligned} \frac{d(\text{IkBen})}{dt} = & \text{IkBeA50n} \cdot \text{pd}_{.122} + \text{IkBeC50n} \cdot \text{pd}_{.124} + \text{IkBeAAAn} \cdot \text{pd}_{.121} + \text{IkBe5050n} \cdot \text{pd}_{.123} + \text{IkBeA50n} \cdot \text{pdi}_{.423} \\ & + \text{IkBeAAAn} \cdot \text{pdi}_{.413} + \text{IkBeC50n} \cdot \text{pdi}_{.443} + \text{IkBe5050n} \cdot \text{pdi}_{.433} + \text{IkBe} \cdot \text{pii}_{.63} - \text{IkBen} \cdot \text{pii}_{.53} - \text{IkBen} \\ & \cdot \text{pii}_{.73} - \text{A50n} \cdot \text{IkBen} \cdot \text{pdi}_{.223} - \text{AAAn} \cdot \text{IkBen} \cdot \text{pdi}_{.213} - \text{C50n} \cdot \text{IkBen} \cdot \text{pdi}_{.243} - \text{IkBen} \cdot \text{P50P50n} \cdot \text{pdi}_{.233} \end{aligned} \quad (1.9)$$

$$\frac{d(\text{tRelA})}{dt} = \text{pm}_{.11} - \text{pm}_{.21} \cdot \text{tRelA} \quad (1.10)$$

$$\frac{d(\text{RelA})}{dt} = \text{A50} \cdot \text{pd}_{.52} + 2 \cdot \text{AA} \cdot \text{pd}_{.51} - \text{RelA} \cdot \text{pm}_{.41} - 2 \cdot \text{RelA}^2 \cdot \text{pd}_{.31} - \text{P50} \cdot \text{RelA} \cdot \text{pd}_{.32} + \text{k2}_{.77} \cdot \text{pm}_{.31} \cdot \text{tRelA} \quad (1.11)$$

$$\frac{d(\text{RelAn})}{dt} = \text{A50n} \cdot \text{pd}_{.62} + 2 \cdot \text{AAAn} \cdot \text{pd}_{.61} - \text{RelAn} \cdot \text{pm}_{.51} - 2 \cdot \text{RelAn}^2 \cdot \text{pd}_{.41} - \text{P50n} \cdot \text{RelAn} \cdot \text{pd}_{.42} \quad (1.12)$$

$$\frac{d(\text{tP50})}{dt} = \frac{\text{pm}_{.12}}{\left(\frac{\text{A50n}}{\text{pm}_{.82}}\right)^{\text{pm}_{.72}} + \left(\frac{\text{C50n}}{\text{pm}_{.82}}\right)^{\text{pm}_{.72}} + 1} + \text{kdel}_{\text{p501}} \cdot \text{tpre}_{\text{P501}} - \text{pm}_{.22} \cdot \text{tP50} \quad (1.13)$$

$$\begin{aligned} \frac{d(P50)}{dt} = & A50 \cdot pd\_52 + C50 \cdot pd\_54 + 2 \cdot P50P50 \cdot pd\_53 - P50 \cdot pm\_42 - 2 \cdot P50^2 \\ & \cdot pd\_33 - P50 \cdot RelA \cdot pd\_32 - P50 \cdot cRel \cdot pd\_34 + k2\_77 \cdot pm\_32 \cdot tP50 \end{aligned} \quad (1.14)$$

$$\begin{aligned} \frac{d(P50n)}{dt} = & A50n \cdot pd\_62 + C50n \cdot pd\_64 + 2 \cdot P50P50n \cdot pd\_63 - P50n \cdot pm\_52 \\ & - 2 \cdot P50n^2 \cdot pd\_43 - P50n \cdot RelAn \cdot pd\_42 - P50n \cdot cReIn \cdot pd\_44 \end{aligned} \quad (1.15)$$

$$\frac{d(tcRel)}{dt} = kdel\_crel1 \cdot tpre\_cRel1 - pm\_23 \cdot tcRel + \frac{kASC\_66^{kASC\_67} \cdot pm\_13}{(Blimp\_1^{kASC\_67} + kASC\_66^{kASC\_67}) \cdot \left( \left( \frac{A50n}{pm\_83} \right)^{pm\_73} + \left( \frac{C50n}{pm\_83} \right)^{pm\_73} + 1 \right)} \quad (1.16)$$

$$\frac{d(cRel)}{dt} = C50 \cdot pd\_54 - cRel \cdot pm\_43 - P50 \cdot cRel \cdot pd\_34 + k2\_77 \cdot pm\_33 \cdot tcRel \quad (1.17)$$

$$\frac{d(cReIn)}{dt} = C50n \cdot pd\_64 - cReIn \cdot pm\_53 - P50n \cdot cReIn \cdot pd\_44 \quad (1.18)$$

$$\begin{aligned} \frac{d(AA)}{dt} = & pd\_31 \cdot RelA^2 - AA \cdot pd\_51 - AA \cdot pd\_71 - AA \cdot pd\_91 + AAn \cdot pd\_81 + IkBaAA \cdot pdi\_311 + IkBbAA \cdot pdi\_312 \\ & + IkBeAA \cdot pdi\_313 + IkBaAA \cdot pii\_131 + IkBbAA \cdot pii\_132 + IkBeAA \cdot pii\_133 - AA \cdot IkBa \cdot pdi\_111 - AA \cdot IkBb \\ & \cdot pdi\_112 - AA \cdot IkBe \cdot pdi\_113 + IkBaAA \cdot pIKK \cdot pii\_121 + IkBbAA \cdot pIKK \cdot pii\_122 + IkBeAA \cdot pIKK \cdot pii\_123 \end{aligned} \quad (1.19)$$

$$\begin{aligned} \frac{d(AAn)}{dt} = & pd\_41 \cdot RelAn^2 + AA \cdot pd\_71 - AAn \cdot pd\_61 - AAn \cdot pd\_81 - AAn \cdot pd\_101 + IkBaAAn \\ & \cdot pdi\_411 + IkBbAAn \cdot pdi\_412 + IkBeAAn \cdot pdi\_413 + IkBaAAn \cdot pii\_141 + IkBbAAn \cdot pii\_142 \\ & + IkBeAAn \cdot pii\_143 - AAn \cdot IkBan \cdot pdi\_211 - AAn \cdot IkBbn \cdot pdi\_212 - AAn \cdot IkBen \cdot pdi\_213 \end{aligned} \quad (1.20)$$

$$\begin{aligned} \frac{d(IkBaAA)}{dt} = & IkBaAAn \cdot pdi\_611 - IkBaAA \cdot pdi\_311 - IkBaAA \cdot pdi\_511 - IkBaAA \\ & \cdot pd\_111 - IkBaAA \cdot pii\_131 + AA \cdot IkBa \cdot pdi\_111 - IkBaAA \cdot pIKK \cdot pii\_121 \end{aligned} \quad (1.21)$$

$$\begin{aligned} \frac{d(IkBaAA_n)}{dt} = & IkBaAA \cdot pdi_{.511} - IkBaAA_n \cdot pd_{.121} - IkBaAA_n \cdot pdi_{.411} \\ & - IkBaAA_n \cdot pdi_{.611} - IkBaAA_n \cdot pii_{.141} + AAn \cdot IkBan \cdot pdi_{.211} \end{aligned} \quad (1.22)$$

$$\begin{aligned} \frac{d(IkBbAA)}{dt} = & IkBbAA_n \cdot pdi_{.612} - IkBbAA \cdot pdi_{.312} - IkBbAA \cdot pdi_{.512} - IkBbAA \\ & \cdot pd_{.111} - IkBbAA \cdot pii_{.132} + AA \cdot IkBb \cdot pdi_{.112} - IkBbAA \cdot pIKK \cdot pii_{.122} \end{aligned} \quad (1.23)$$

$$\begin{aligned} \frac{d(IkBbAA_n)}{dt} = & IkBbAA \cdot pdi_{.512} - IkBbAA_n \cdot pd_{.121} - IkBbAA_n \cdot pdi_{.412} \\ & - IkBbAA_n \cdot pdi_{.612} - IkBbAA_n \cdot pii_{.142} + AAn \cdot IkBbn \cdot pdi_{.212} \end{aligned} \quad (1.24)$$

$$\begin{aligned} \frac{d(IkBeAA)}{dt} = & IkBeAA_n \cdot pdi_{.613} - IkBeAA \cdot pdi_{.313} - IkBeAA \cdot pdi_{.513} - IkBeAA \\ & \cdot pd_{.111} - IkBeAA \cdot pii_{.133} + AA \cdot IkBe \cdot pdi_{.113} - IkBeAA \cdot pIKK \cdot pii_{.123} \end{aligned} \quad (1.25)$$

$$\begin{aligned} \frac{d(IkBeAA_n)}{dt} = & IkBeAA \cdot pdi_{.513} - IkBeAA_n \cdot pd_{.121} - IkBeAA_n \cdot pdi_{.413} \\ & - IkBeAA_n \cdot pdi_{.613} - IkBeAA_n \cdot pii_{.143} + AAn \cdot IkBen \cdot pdi_{.213} \end{aligned} \quad (1.26)$$

$$\begin{aligned} \frac{d(A50)}{dt} = & A50_n \cdot pd_{.82} - A50 \cdot pd_{.72} - A50 \cdot pd_{.92} - A50 \cdot pd_{.52} + IkBaA50 \cdot pdi_{.321} + IkBbA50 \cdot pdi_{.322} + IkBeA50 \cdot pdi_{.323} \\ & + IkBaA50 \cdot pii_{.131} + IkBbA50 \cdot pii_{.132} + IkBeA50 \cdot pii_{.133} - A50 \cdot IkBa \cdot pdi_{.121} - A50 \cdot IkBb \cdot pdi_{.122} - A50 \cdot IkBe \\ & \cdot pdi_{.123} + P50 \cdot RelA \cdot pd_{.32} + IkBaA50 \cdot pIKK \cdot pii_{.121} + IkBbA50 \cdot pIKK \cdot pii_{.122} + IkBeA50 \cdot pIKK \cdot pii_{.123} \end{aligned} \quad (1.27)$$

$$\begin{aligned} \frac{d(A50_n)}{dt} = & A50 \cdot pd_{.72} - A50_n \cdot pd_{.62} - A50_n \cdot pd_{.82} - A50_n \cdot pd_{.102} + IkBaA50_n \cdot pdi_{.421} + IkBbA50_n \\ & \cdot pdi_{.422} + IkBeA50_n \cdot pdi_{.423} + IkBaA50_n \cdot pii_{.141} + IkBbA50_n \cdot pii_{.142} + IkBeA50_n \cdot pii_{.143} \\ & - A50_n \cdot IkBan \cdot pdi_{.221} - A50_n \cdot IkBbn \cdot pdi_{.222} - A50_n \cdot IkBen \cdot pdi_{.223} + P50_n \cdot RelAn \cdot pd_{.42} \end{aligned} \quad (1.28)$$

$$\frac{d(IkBaA50)}{dt} = IkBaA50n \cdot pdi\_621 - IkBaA50 \cdot pdi\_321 - IkBaA50 \cdot pdi\_521 - IkBaA50 \cdot pd\_112 - IkBaA50 \cdot pii\_131 + A50 \cdot IkBa \cdot pdi\_121 - IkBaA50 \cdot pIKK \cdot pii\_121 \quad (1.29)$$

$$\frac{d(IkBaA50n)}{dt} = IkBaA50 \cdot pdi\_521 - IkBaA50n \cdot pd\_122 - IkBaA50n \cdot pdi\_421 - IkBaA50n \cdot pdi\_621 - IkBaA50n \cdot pii\_141 + A50n \cdot IkBan \cdot pdi\_221 \quad (1.30)$$

$$\frac{d(IkBbA50)}{dt} = IkBbA50n \cdot pdi\_622 - IkBbA50 \cdot pdi\_322 - IkBbA50 \cdot pdi\_522 - IkBbA50 \cdot pd\_112 - IkBbA50 \cdot pii\_132 + A50 \cdot IkBb \cdot pdi\_122 - IkBbA50 \cdot pIKK \cdot pii\_122 \quad (1.31)$$

$$\frac{d(IkBbA50n)}{dt} = IkBbA50 \cdot pdi\_522 - IkBbA50n \cdot pd\_122 - IkBbA50n \cdot pdi\_422 - IkBbA50n \cdot pdi\_622 - IkBbA50n \cdot pii\_142 + A50n \cdot IkBbn \cdot pdi\_222 \quad (1.32)$$

$$\frac{d(IkBeA50)}{dt} = IkBeA50n \cdot pdi\_623 - IkBeA50 \cdot pdi\_323 - IkBeA50 \cdot pdi\_523 - IkBeA50 \cdot pd\_112 - IkBeA50 \cdot pii\_133 + A50 \cdot IkBe \cdot pdi\_123 - IkBeA50 \cdot pIKK \cdot pii\_123 \quad (1.33)$$

$$\frac{d(IkBeA50n)}{dt} = IkBeA50 \cdot pdi\_523 - IkBeA50n \cdot pd\_122 - IkBeA50n \cdot pdi\_423 - IkBeA50n \cdot pdi\_623 - IkBeA50n \cdot pii\_143 + A50n \cdot IkBen \cdot pdi\_223 \quad (1.34)$$

$$\begin{aligned} \frac{d(P50P50)}{dt} = & pd\_33 \cdot P50^2 + IkBa5050 \cdot pdi\_331 + IkBb5050 \cdot pdi\_332 + IkBe5050 \cdot pdi\_333 + IkBa5050 \cdot pii\_131 + IkBb5050 \cdot pii\_132 \\ & + IkBe5050 \cdot pii\_133 - P50P50 \cdot pd\_53 - P50P50 \cdot pd\_73 - P50P50 \cdot pd\_93 + P50P50n \cdot pd\_83 - IkBa \cdot P50P50 \cdot pdi\_131 - IkBb \\ & \cdot P50P50 \cdot pdi\_132 - IkBe \cdot P50P50 \cdot pdi\_133 + IkBa5050 \cdot pIKK \cdot pii\_121 + IkBb5050 \cdot pIKK \cdot pii\_122 + IkBe5050 \cdot pIKK \cdot pii\_123 \end{aligned} \quad (1.35)$$

$$\begin{aligned} \frac{d(P50P50n)}{dt} = & pd\_43 \cdot P50n^2 + IkBa5050n \cdot pdi\_431 + IkBb5050n \cdot pdi\_432 + IkBe5050n \cdot pdi\_433 + IkBa5050n \cdot pii\_141 \\ & + IkBb5050n \cdot pii\_142 + IkBe5050n \cdot pii\_143 + P50P50 \cdot pd\_73 - P50P50n \cdot pd\_63 - P50P50n \cdot pd\_83 \\ & - P50P50n \cdot pd\_103 - IkBan \cdot P50P50n \cdot pdi\_231 - IkBbn \cdot P50P50n \cdot pdi\_232 - IkBen \cdot P50P50n \cdot pdi\_233 \end{aligned} \quad (1.36)$$

$$\begin{aligned} \frac{d(IkBa5050)}{dt} = & IkBa5050n \cdot pdi\_631 - IkBa5050 \cdot pdi\_331 - IkBa5050 \cdot pdi\_531 - IkBa5050 \\ & \cdot pd\_113 - IkBa5050 \cdot pii\_131 + IkBa \cdot P50P50 \cdot pdi\_131 - IkBa5050 \cdot pIKK \cdot pii\_121 \end{aligned} \quad (1.37)$$

$$\begin{aligned} \frac{d(IkBa5050n)}{dt} = & IkBa5050 \cdot pdi\_531 - IkBa5050n \cdot pd\_123 - IkBa5050n \cdot pdi\_431 \\ & - IkBa5050n \cdot pdi\_631 - IkBa5050n \cdot pii\_141 + IkBan \cdot P50P50n \cdot pdi\_231 \end{aligned} \quad (1.38)$$

$$\begin{aligned} \frac{d(IkBb5050)}{dt} = & IkBb5050n \cdot pdi\_632 - IkBb5050 \cdot pdi\_332 - IkBb5050 \cdot pdi\_532 - IkBb5050 \\ & \cdot pd\_113 - IkBb5050 \cdot pii\_132 + IkBb \cdot P50P50 \cdot pdi\_132 - IkBb5050 \cdot pIKK \cdot pii\_122 \end{aligned} \quad (1.39)$$

$$\begin{aligned} \frac{d(IkBb5050n)}{dt} = & IkBb5050 \cdot pdi\_532 - IkBb5050n \cdot pd\_123 - IkBb5050n \cdot pdi\_432 \\ & - IkBb5050n \cdot pdi\_632 - IkBb5050n \cdot pii\_142 + IkBbn \cdot P50P50n \cdot pdi\_232 \end{aligned} \quad (1.40)$$

$$\begin{aligned} \frac{d(IkBe5050)}{dt} = & IkBe5050n \cdot pdi\_633 - IkBe5050 \cdot pdi\_333 - IkBe5050 \cdot pdi\_533 - IkBe5050 \\ & \cdot pd\_113 - IkBe5050 \cdot pii\_133 + IkBe \cdot P50P50 \cdot pdi\_133 - IkBe5050 \cdot pIKK \cdot pii\_123 \end{aligned} \quad (1.41)$$

$$\begin{aligned} \frac{d(IkBe5050n)}{dt} = & IkBe5050 \cdot pdi\_533 - IkBe5050n \cdot pd\_123 - IkBe5050n \cdot pdi\_433 \\ & - IkBe5050n \cdot pdi\_633 - IkBe5050n \cdot pii\_143 + IkBen \cdot P50P50n \cdot pdi\_233 \end{aligned} \quad (1.42)$$

$$\begin{aligned}
\frac{d(C50)}{dt} = & C50n \cdot pd_{.84} - C50 \cdot pd_{.74} - C50 \cdot pd_{.94} - C50 \cdot pd_{.54} + IkBaC50 \cdot pdi_{.341} + IkBbC50 \cdot pdi_{.342} + IkBeC50 \cdot pdi_{.343} \\
& + IkBaC50 \cdot pii_{.131} + IkBbC50 \cdot pii_{.132} + IkBeC50 \cdot pii_{.133} - C50 \cdot IkBa \cdot pdi_{.141} - C50 \cdot IkBb \cdot pdi_{.142} - C50 \\
& \cdot IkBe \cdot pdi_{.143} + P50 \cdot cRel \cdot pd_{.34} + IkBaC50 \cdot pIKK \cdot pii_{.121} + IkBbC50 \cdot pIKK \cdot pii_{.122} + IkBeC50 \cdot pIKK \cdot pii_{.123}
\end{aligned} \tag{1.43}$$

$$\begin{aligned}
\frac{d(C50n)}{dt} = & C50 \cdot pd_{.74} - C50n \cdot pd_{.64} - C50n \cdot pd_{.84} - C50n \cdot pd_{.104} + IkBaC50n \cdot pdi_{.441} + IkBbC50n \\
& \cdot pdi_{.442} + IkBeC50n \cdot pdi_{.443} + IkBaC50n \cdot pii_{.141} + IkBbC50n \cdot pii_{.142} + IkBeC50n \cdot pii_{.143} \\
& - C50n \cdot IkBan \cdot pdi_{.241} - C50n \cdot IkBbn \cdot pdi_{.242} - C50n \cdot IkBen \cdot pdi_{.243} + P50n \cdot cReIn \cdot pd_{.44}
\end{aligned} \tag{1.44}$$

$$\begin{aligned}
\frac{d(IkBaC50)}{dt} = & IkBaC50n \cdot pdi_{.641} - IkBaC50 \cdot pdi_{.341} - IkBaC50 \cdot pdi_{.541} - IkBaC50 \\
& \cdot pd_{.114} - IkBaC50 \cdot pii_{.131} + C50 \cdot IkBa \cdot pdi_{.141} - IkBaC50 \cdot pIKK \cdot pii_{.121}
\end{aligned} \tag{1.45}$$

$$\begin{aligned}
\frac{d(IkBaC50n)}{dt} = & IkBaC50 \cdot pdi_{.541} - IkBaC50n \cdot pd_{.124} - IkBaC50n \cdot pdi_{.441} \\
& - IkBaC50n \cdot pdi_{.641} - IkBaC50n \cdot pii_{.141} + C50n \cdot IkBan \cdot pdi_{.241}
\end{aligned} \tag{1.46}$$

$$\begin{aligned}
\frac{d(IkBbC50)}{dt} = & IkBbC50n \cdot pdi_{.642} - IkBbC50 \cdot pdi_{.342} - IkBbC50 \cdot pdi_{.542} - IkBbC50 \\
& \cdot pd_{.114} - IkBbC50 \cdot pii_{.132} + C50 \cdot IkBb \cdot pdi_{.142} - IkBbC50 \cdot pIKK \cdot pii_{.122}
\end{aligned} \tag{1.47}$$

$$\begin{aligned}
\frac{d(IkBbC50n)}{dt} = & IkBbC50 \cdot pdi_{.542} - IkBbC50n \cdot pd_{.124} - IkBbC50n \cdot pdi_{.442} \\
& - IkBbC50n \cdot pdi_{.642} - IkBbC50n \cdot pii_{.142} + C50n \cdot IkBbn \cdot pdi_{.242}
\end{aligned} \tag{1.48}$$

$$\begin{aligned}
\frac{d(IkBeC50)}{dt} = & IkBeC50n \cdot pdi_{.643} - IkBeC50 \cdot pdi_{.343} - IkBeC50 \cdot pdi_{.543} - IkBeC50 \\
& \cdot pd_{.114} - IkBeC50 \cdot pii_{.133} + C50 \cdot IkBe \cdot pdi_{.143} - IkBeC50 \cdot pIKK \cdot pii_{.123}
\end{aligned} \tag{1.49}$$

$$\begin{aligned} \frac{d(\text{IkBeC50n})}{dt} = & \text{IkBeC50} \cdot \text{pdi}_{.543} - \text{IkBeC50n} \cdot \text{pd}_{.124} - \text{IkBeC50n} \cdot \text{pdi}_{.443} \\ & - \text{IkBeC50n} \cdot \text{pdi}_{.643} - \text{IkBeC50n} \cdot \text{pii}_{.143} + \text{C50n} \cdot \text{IkBen} \cdot \text{pdi}_{.243} \end{aligned} \quad (1.50)$$

$$\frac{d(\text{LL})}{dt} = 0 \quad (1.51)$$

$$\frac{d(\text{RR})}{dt} = \text{LR} \cdot k_{.2} - \text{RR} \cdot k_{.72} + k_{.71} \cdot k_{2.77} + \text{LL} \cdot \text{RR} \cdot k_{.1} \cdot \left( \frac{\text{Blimp}_1}{\text{Blimp}_1 + 4} - 1 \right) \quad (1.52)$$

$$\frac{d(\text{LR})}{dt} = -\text{LR} \cdot k_{.2} - \text{LR} \cdot k_{.3} - \text{LL} \cdot \text{RR} \cdot k_{.1} \cdot \left( \frac{\text{Blimp}_1}{\text{Blimp}_1 + 4} - 1 \right) \quad (1.53)$$

$$\frac{d(\text{DISC})}{dt} = \text{DISCpC}_8 \cdot k_{.7} + \text{DISCpC}_8 \cdot k_{.8} + \text{LR} \cdot k_{.3} + \text{flipDISC} \cdot k_{.5} - \text{DISC} \cdot \text{flipp} \cdot k_{.4} - \text{DISC} \cdot k_{.6} \cdot \text{pC}_8 \quad (1.54)$$

$$\frac{d(\text{flipp})}{dt} = \text{flipDISC} \cdot k_{.5} - \text{flipp} \cdot k_{.74} + k_{.73} \cdot k_{2.77} - \text{DISC} \cdot \text{flipp} \cdot k_{.4} \quad (1.55)$$

$$\frac{d(\text{flipDISC})}{dt} = \text{DISC} \cdot \text{flipp} \cdot k_{.4} - \text{flipDISC} \cdot k_{.75} - \text{flipDISC} \cdot k_{.5} \quad (1.56)$$

$$\frac{d(\text{pC}_8)}{dt} = \text{C6pC}_8 \cdot k_{.18} + \text{DISCpC}_8 \cdot k_{.7} + k_{.76} \cdot k_{2.77} - k_{.77} \cdot \text{pC}_8 - \text{C}_6 \cdot k_{.17} \cdot \text{pC}_8 - \text{DISC} \cdot k_{.6} \cdot \text{pC}_8 \quad (1.57)$$

$$\frac{d(\text{DISCpC}_8)}{dt} = \text{DISC} \cdot k_{.6} \cdot \text{pC}_8 - \text{DISCpC}_8 \cdot k_{.8} - \text{DISCpC}_8 \cdot k_{.7} \quad (1.58)$$

$$\begin{aligned} \frac{d(\text{C}_8)}{dt} = & \text{BarC}_8 \cdot k_{.10} + \text{C8Bid} \cdot k_{.27} + \text{C8Bid} \cdot k_{.28} + \text{C6pC}_8 \cdot k_{.19} + \text{C8pC}_3 \cdot k_{.12} + \text{C8pC}_3 \\ & \cdot k_{.13} + \text{DISCpC}_8 \cdot k_{.8} - \text{Barp} \cdot \text{C}_8 \cdot k_{.9} - \text{Bid} \cdot \text{C}_8 \cdot k_{.26} - \text{C}_8 \cdot k_{.11} \cdot \text{pC}_3 \end{aligned} \quad (1.59)$$

$$\frac{d(\text{Barp})}{dt} = \text{BarC}_8 \cdot k_{10} - \text{Barp} \cdot k_{79} + k_{78} \cdot k_{277} - \text{Barp} \cdot C_8 \cdot k_9 \quad (1.60)$$

$$\frac{d(\text{BarC}_8)}{dt} = \text{Barp} \cdot C_8 \cdot k_9 - \text{BarC}_8 \cdot k_{80} - \text{BarC}_8 \cdot k_{10} \quad (1.61)$$

$$\frac{d(\text{pC}_3)}{dt} = \text{ApoppC}_3 \cdot k_{63} + \text{C8pC}_3 \cdot k_{12} + k_{101} \cdot k_{277} - k_{102} \cdot \text{pC}_3 - \text{Apop} \cdot k_{62} \cdot \text{pC}_3 - C_8 \cdot k_{11} \cdot \text{pC}_3 \quad (1.62)$$

$$\frac{d(\text{C8pC}_3)}{dt} = C_8 \cdot k_{11} \cdot \text{pC}_3 - \text{C8pC}_3 \cdot k_{13} - \text{C8pC}_3 \cdot k_{12} \quad (1.63)$$

$$\begin{aligned} \frac{d(C_3)}{dt} = & \text{ApoppC}_3 \cdot k_{64} + \text{C3PARP} \cdot k_{24} + \text{C3PARP} \cdot k_{25} + \text{C3pC}_6 \cdot k_{15} + \text{C3pC}_6 \cdot k_{16} \\ & + \text{C8pC}_3 \cdot k_{13} + \text{XIAPC}_3 \cdot k_{21} - C_3 \cdot \text{PARP} \cdot k_{23} - C_3 \cdot \text{XIAP} \cdot k_{20} - C_3 \cdot k_{14} \cdot \text{pC}_6 \end{aligned} \quad (1.64)$$

$$\frac{d(\text{pC}_6)}{dt} = \text{C3pC}_6 \cdot k_{15} + k_{104} \cdot k_{277} - k_{105} \cdot \text{pC}_6 - C_3 \cdot k_{14} \cdot \text{pC}_6 \quad (1.65)$$

$$\frac{d(\text{C3pC}_6)}{dt} = C_3 \cdot k_{14} \cdot \text{pC}_6 - \text{C3pC}_6 \cdot k_{16} - \text{C3pC}_6 \cdot k_{15} \quad (1.66)$$

$$\frac{d(C_6)}{dt} = \text{C3pC}_6 \cdot k_{16} - C_6 \cdot k_{106} + \text{C6pC}_8 \cdot k_{18} + \text{C6pC}_8 \cdot k_{19} - C_6 \cdot k_{17} \cdot \text{pC}_8 \quad (1.67)$$

$$\frac{d(\text{C6pC}_8)}{dt} = C_6 \cdot k_{17} \cdot \text{pC}_8 - \text{C6pC}_8 \cdot k_{19} - \text{C6pC}_8 \cdot k_{18} \quad (1.68)$$

$$\begin{aligned} \frac{d(\text{XIAP})}{dt} = & \text{ApopXIAP} \cdot k_{68} + \text{XIAPC}_3 \cdot k_{21} + \text{XIAPC}_3 \cdot k_{22} - \text{XIAP} \cdot k_{96} + \text{cSmacXIAP} \\ & \cdot k_{70} + k_{95} \cdot k_{277} - \text{Apop} \cdot \text{XIAP} \cdot k_{67} - C_3 \cdot \text{XIAP} \cdot k_{20} - \text{XIAP} \cdot \text{cSmac} \cdot k_{69} \end{aligned} \quad (1.69)$$

$$\frac{d(\text{XIAPC}_3)}{dt} = C_3 \cdot \text{XIAP} \cdot k_{20} - \text{XIAPC}_3 \cdot k_{22} - \text{XIAPC}_3 \cdot k_{21} \quad (1.70)$$

$$\frac{d(\text{PARP})}{dt} = \text{C3PARP} \cdot k_{24} - \text{PARP} \cdot k_{109} + k_{108} \cdot k_{277} - C_3 \cdot \text{PARP} \cdot k_{23} \quad (1.71)$$

$$\frac{d(\text{C3PARP})}{dt} = C_3 \cdot \text{PARP} \cdot k_{23} - \text{C3PARP} \cdot k_{25} - \text{C3PARP} \cdot k_{24} \quad (1.72)$$

$$\frac{d(\text{CPARP})}{dt} = \text{C3PARP} \cdot k_{25} - \text{CPARP} \cdot k_{110} \quad (1.73)$$

$$\frac{d(\text{Bid})}{dt} = \text{C8Bid} \cdot k_{27} - \text{Bid} \cdot k_{82} + k_{81} \cdot k_{277} - \text{Bid} \cdot C_8 \cdot k_{26} \quad (1.74)$$

$$\frac{d(\text{C8Bid})}{dt} = \text{Bid} \cdot C_8 \cdot k_{26} - \text{C8Bid} \cdot k_{28} - \text{C8Bid} \cdot k_{27} \quad (1.75)$$

$$\frac{d(\text{tBid})}{dt} = \text{C8Bid} \cdot k_{28} + \text{Mcl1tBid} \cdot k_{30} + k_{32} \cdot \text{tBidBax} + k_{33} \cdot \text{tBidBax} - \text{Bax} \cdot k_{31} \cdot \text{tBid} - \text{Mcl1} \cdot k_{29} \cdot \text{tBid} \quad (1.76)$$

$$\begin{aligned} \frac{d(\text{Mcl1})}{dt} = & \text{Mcl1tBid} \cdot k_{30} - \text{Mcl1} \cdot k_{84} + k_{277} \cdot k_{\text{mcl}} + \text{MCLMCLi} \cdot \text{kimcli} \\ & \cdot \text{phase} - \text{Mcl1} \cdot k_{29} \cdot \text{tBid} - \text{MCLi} \cdot \text{Mcl1} \cdot \text{kmcli} \cdot \text{phase} \end{aligned} \quad (1.77)$$

$$\frac{d(\text{Mcl1tBid})}{dt} = \text{Mcl1} \cdot k_{29} \cdot \text{tBid} - \text{Mcl1tBid} \cdot k_{85} - \text{Mcl1tBid} \cdot k_{30} \quad (1.78)$$

$$\frac{d(\text{Bax})}{dt} = k_{86} \cdot k_{277} - \text{Bax} \cdot k_{87} + k_{32} \cdot \text{tBidBax} - \text{Bax} \cdot k_{31} \cdot \text{tBid} \quad (1.79)$$

$$\frac{d(\text{tBidBax})}{dt} = \text{Bax} \cdot k_{31} \cdot \text{tBid} - k_{33} \cdot \text{tBidBax} - k_{32} \cdot \text{tBidBax} \quad (1.80)$$

$$\frac{d(\text{act\_Bax})}{dt} = \text{Baxm} \cdot k_{35} - \text{act\_Bax} \cdot k_{34} + k_{33} \cdot \text{tBidBax} \quad (1.81)$$

$$\frac{d(\text{Baxm})}{dt} = 2 \cdot \text{Bax}_2 \cdot k_{39} - \text{Baxm} \cdot k_{35} + \text{BaxmBcl}_2 \cdot k_{37} + \text{act\_Bax} \cdot k_{34} - \frac{2 \cdot \text{Baxm}^2 \cdot k_{38}}{\text{mvol}} - \frac{\text{Baxm} \cdot \text{Bcl}_2 \cdot k_{36}}{\text{mvol}} \quad (1.82)$$

$$\begin{aligned} \frac{d(\text{Bcl}_2)}{dt} = & \text{Bax2Bcl}_2 \cdot k_{41} + \text{Bax4Bcl}_2 \cdot k_{45} + \text{BaxmBcl}_2 \cdot k_{37} - \text{Bcl}_2 \cdot k_{89} - 277.2133 \cdot k_{277} \cdot (\text{phase} - 1) \\ & + 0.3070 \cdot k_{277} \cdot \text{mBcl}_2 \cdot \text{phase} - \frac{\text{Bax}_2 \cdot \text{Bcl}_2 \cdot k_{40}}{\text{mvol}} - \frac{\text{Bax}_4 \cdot \text{Bcl}_2 \cdot k_{44}}{\text{mvol}} - \frac{\text{Baxm} \cdot \text{Bcl}_2 \cdot k_{36}}{\text{mvol}} \end{aligned} \quad (1.83)$$

$$\frac{d(\text{BaxmBcl}_2)}{dt} = \frac{\text{Baxm} \cdot \text{Bcl}_2 \cdot k_{36}}{\text{mvol}} - \text{BaxmBcl}_2 \cdot k_{90} - \text{BaxmBcl}_2 \cdot k_{37} \quad (1.84)$$

$$\frac{d(\text{Bax}_2)}{dt} = 2 \cdot \text{Bax}_4 \cdot k_{43} - \text{Bax}_2 \cdot k_{39} + \text{Bax2Bcl}_2 \cdot k_{41} - \frac{2 \cdot \text{Bax}_2^2 \cdot k_{42}}{\text{mvol}} + \frac{\text{Baxm}^2 \cdot k_{38}}{\text{mvol}} - \frac{\text{Bax}_2 \cdot \text{Bcl}_2 \cdot k_{40}}{\text{mvol}} \quad (1.85)$$

$$\frac{d(\text{Bax2Bcl}_2)}{dt} = \frac{\text{Bax}_2 \cdot \text{Bcl}_2 \cdot k_{40}}{\text{mvol}} - \text{Bax2Bcl}_2 \cdot k_{91} - \text{Bax2Bcl}_2 \cdot k_{41} \quad (1.86)$$

$$\frac{d(\text{Bax}_4)}{dt} = \text{Bax4M} \cdot k_{47} - \text{Bax}_4 \cdot k_{43} + \text{Bax4Bcl}_2 \cdot k_{45} + \frac{\text{Bax}_2^2 \cdot k_{42}}{\text{mvol}} - \frac{\text{Bax}_4 \cdot \text{Bcl}_2 \cdot k_{44}}{\text{mvol}} - \frac{\text{Bax}_4 \cdot \text{MM} \cdot k_{46}}{\text{mvol}} \quad (1.87)$$

$$\frac{d(\text{Bax4Bcl}_2)}{dt} = \frac{\text{Bax}_4 \cdot \text{Bcl}_2 \cdot k_{44}}{\text{mvol}} - \text{Bax4Bcl}_2 \cdot k_{92} - \text{Bax4Bcl}_2 \cdot k_{45} \quad (1.88)$$

$$\frac{d(\text{MM})}{dt} = \text{AMito} \cdot k_{93} + \text{Bax4M} \cdot k_{47} - \frac{\text{Bax}_4 \cdot \text{MM} \cdot k_{46}}{\text{mvol}} \quad (1.89)$$

$$\frac{d(\text{Bax4M})}{dt} = \frac{\text{Bax}_4 \cdot \text{MM} \cdot k_{46}}{\text{mvol}} - \text{Bax4M} \cdot k_{48} - \text{Bax4M} \cdot k_{47} \quad (1.90)$$

$$\begin{aligned} \frac{d(\text{AMito})}{dt} = & \text{AMitomSmac} \cdot k_{.53} - \text{AMito} \cdot k_{.93} + \text{AMitomSmac} \cdot k_{.54} + \text{AMitomCytoC} \cdot k_{.50} \\ & + \text{AMitomCytoC} \cdot k_{.51} + \text{Bax4M} \cdot k_{.48} - \frac{\text{AMito} \cdot k_{.49} \cdot \text{mCytoC}}{\text{mvol}} - \frac{\text{AMito} \cdot k_{.52} \cdot \text{mSmac}}{\text{mvol}} \end{aligned} \quad (1.91)$$

$$\frac{d(\text{mCytoC})}{dt} = \text{AMitomCytoC} \cdot k_{.50} + k_{.113} \cdot k_{2.77} - k_{.114} \cdot \text{mCytoC} - \frac{\text{AMito} \cdot k_{.49} \cdot \text{mCytoC}}{\text{mvol}} \quad (1.92)$$

$$\frac{d(\text{AMitomCytoC})}{dt} = \frac{\text{AMito} \cdot k_{.49} \cdot \text{mCytoC}}{\text{mvol}} - \text{AMitomCytoC} \cdot k_{.51} - \text{AMitomCytoC} \cdot k_{.50} \quad (1.93)$$

$$\frac{d(\text{ACytoC})}{dt} = \text{AMitomCytoC} \cdot k_{.51} - \text{ACytoC} \cdot k_{.55} + \text{CytoC} \cdot k_{.56} \quad (1.94)$$

$$\frac{d(\text{mSmac})}{dt} = \text{AMitomSmac} \cdot k_{.53} + k_{.97} \cdot k_{2.77} - k_{.98} \cdot \text{mSmac} - \frac{\text{AMito} \cdot k_{.52} \cdot \text{mSmac}}{\text{mvol}} \quad (1.95)$$

$$\frac{d(\text{AMitomSmac})}{dt} = \frac{\text{AMito} \cdot k_{.52} \cdot \text{mSmac}}{\text{mvol}} - \text{AMitomSmac} \cdot k_{.54} - \text{AMitomSmac} \cdot k_{.53} \quad (1.96)$$

$$\frac{d(\text{ASmac})}{dt} = \text{AMitomSmac} \cdot k_{.54} - \text{ASmac} \cdot k_{.65} + \text{cSmac} \cdot k_{.66} \quad (1.97)$$

$$\frac{d(\text{CytoC})}{dt} = \text{ACytoC} \cdot k_{.55} + \text{ApafCytoC} \cdot k_{.57} + \text{ApafCytoC} \cdot k_{.59} - \text{CytoC} \cdot k_{.56} - \text{CytoC} \cdot k_{.115} - \text{Apaf} \cdot \text{CytoC} \cdot k_{.58} \quad (1.98)$$

$$\frac{d(\text{Apaf})}{dt} = \text{ApafCytoC} \cdot k_{.59} + \text{act\_Apaf} \cdot k_{.94} - \text{Apaf} \cdot \text{CytoC} \cdot k_{.58} \quad (1.99)$$

$$\frac{d(\text{ApafCytoC})}{dt} = \text{Apaf} \cdot \text{CytoC} \cdot k_{.58} - \text{ApafCytoC} \cdot k_{.59} - \text{ApafCytoC} \cdot k_{.57} \quad (1.100)$$

$$\frac{d(\text{act\_Apaf})}{dt} = \text{ApafCytoC} \cdot k_{.57} + \text{Apop} \cdot k_{.61} - \text{act\_Apaf} \cdot k_{.94} - \text{act\_Apaf} \cdot k_{.60} \cdot \text{pC}_9 \quad (1.101)$$

$$\frac{d(\text{pC}_9)}{dt} = \text{Apop} \cdot k_{.61} - \text{act\_Apaf} \cdot k_{.60} \cdot \text{pC}_9 \quad (1.102)$$

$$\frac{d(\text{Apop})}{dt} = \text{ApoppC}_3 \cdot k_{.63} - \text{Apop} \cdot k_{.61} + \text{ApoppC}_3 \cdot k_{.64} + \text{ApopXIAP} \cdot k_{.68} + \text{ApopXIAP} \cdot k_{.107} - \text{Apop} \cdot \text{XIAP} \cdot k_{.67} - \text{Apop} \cdot k_{.62} \cdot \text{pC}_3 + \text{act\_Apaf} \cdot k_{.60} \cdot \text{pC}_9 \quad (1.103)$$

$$\frac{d(\text{ApoppC}_3)}{dt} = \text{Apop} \cdot k_{.62} \cdot \text{pC}_3 - \text{ApoppC}_3 \cdot k_{.64} - \text{ApoppC}_3 \cdot k_{.63} \quad (1.104)$$

$$\frac{d(\text{cSmac})}{dt} = \text{ASmac} \cdot k_{.65} - \text{cSmac} \cdot k_{.66} - \text{cSmac} \cdot k_{.99} + \text{cSmacXIAP} \cdot k_{.70} - \text{XIAP} \cdot \text{cSmac} \cdot k_{.69} \quad (1.105)$$

$$\frac{d(\text{ApopXIAP})}{dt} = \text{Apop} \cdot \text{XIAP} \cdot k_{.67} - \text{ApopXIAP} \cdot k_{.107} - \text{ApopXIAP} \cdot k_{.68} \quad (1.106)$$

$$\frac{d(\text{cSmacXIAP})}{dt} = \text{XIAP} \cdot \text{cSmac} \cdot k_{.69} - \text{cSmacXIAP} \cdot k_{.100} - \text{cSmacXIAP} \cdot k_{.70} \quad (1.107)$$

$$\frac{d(C_3\text{-Ub})}{dt} = \text{XIAPC}_3 \cdot k_{.22} - C_3\text{-Ub} \cdot k_{.103} \quad (1.108)$$

$$\frac{d(\text{CycA})}{dt} = \text{expr}_3 + \text{CA} \cdot k_{2.17} + \text{CA} \cdot (k_{2.30} + k_{2.31} \cdot (\text{CycA} \cdot k_{2.34} + \text{CycB} \cdot k_{2.33} + \text{CycE} \cdot k_{2.32})) - \text{CDc}_{.20} \cdot \text{CycA} \cdot k_{2.22} - \text{CycA} \cdot k_{2.16} \cdot \text{p27} \quad (1.109)$$

$$\frac{d(\text{CycB})}{dt} = k_{2.77} \cdot \left( k_{2.23} + \frac{\text{CycB}^2 \cdot k_{2.24}}{k_{2.25}^2 \cdot \left( \frac{\text{CycB}^2}{k_{2.25}^2} + 1 \right)} \right) - \text{CycB} \cdot (\text{CDc}_{.20} \cdot k_{2.28} + \text{Cdh}_{.1} \cdot k_{2.27} - k_{2.26} \cdot (\text{Cdh}_{.1} - 1)) \quad (1.110)$$

$$\begin{aligned} \frac{d(\text{CycD})}{dt} = & \text{CD} \cdot k2\_11 - \text{CycD} \cdot k2\_9 + \text{CD} \cdot (k2\_30 + k2\_31 \cdot (\text{CycA} \cdot k2\_34 + \text{CycB} \cdot k2\_33 + \text{CycE} \cdot k2\_32)) \\ & - \text{CycD} \cdot k2\_10 \cdot p27 + k2\_8 \cdot k2\_77 \cdot m\text{CycD} \end{aligned} \quad (1.111)$$

$$\begin{aligned} \frac{d(\text{CycE})}{dt} = & \text{CE} \cdot k2\_17 - \text{CycE} \cdot \left( k2\_14 + \frac{k2\_15 \cdot (\text{CycB} \cdot k2\_20 + k2\_19 \cdot (\text{CycA} + \text{CycE}))}{\text{CE} + \text{CycE} + k2\_18} \right) + k2\_77 \cdot (k2\_12 + \text{E2F} \cdot k2\_13) \\ & + \text{CE} \cdot (k2\_30 + k2\_31 \cdot (\text{CycA} \cdot k2\_34 + \text{CycB} \cdot k2\_33 + \text{CycE} \cdot k2\_32)) - \text{CycE} \cdot k2\_16 \cdot p27 \end{aligned} \quad (1.112)$$

$$\begin{aligned} \frac{d(m\text{CycD})}{dt} = & k2\_78 \\ & \cdot \left( \frac{0.9900 \cdot (\text{A50n} \cdot kp\_NC + \text{C50n} \cdot kp\_NC + kp\_mtb \cdot otherTFs\_activity + kmtb\_off \cdot kp\_PMBC \cdot otherTFs\_activity)^2}{\text{CYCD\_THRESHOLD}^2 \cdot \left( \frac{(\text{A50n} \cdot kp\_NC + \text{C50n} \cdot kp\_NC + kp\_mtb \cdot otherTFs\_activity + kmtb\_off \cdot kp\_PMBC \cdot otherTFs\_activity)^2}{\text{CYCD\_THRESHOLD}^2} + 1 \right)} \right. \\ & \left. + 0.0100 \right) - k2\_79 \cdot m\text{CycD} \end{aligned} \quad (1.113)$$

$$\frac{d(m\text{Bcl}_2)}{dt} = \text{expr}_4 + ke\_bcl2 - k2\_81 \cdot m\text{Bcl}_2 \quad (1.114)$$

$$\frac{d(\text{Cdh}_1)}{dt} = \text{expr}_1 - \frac{\text{Cdh}_1 \cdot k2\_51 \cdot (\text{CycA} \cdot k2\_54 + \text{CycB} \cdot k2\_53 + \text{CycE} \cdot k2\_52)}{\text{Cdh}_1 + k2\_50} \quad (1.115)$$

$$\frac{d(\text{CA})}{dt} = \text{CycA} \cdot k2\_16 \cdot p27 - \text{CA} \cdot (k2\_30 + k2\_31 \cdot (\text{CycA} \cdot k2\_34 + \text{CycB} \cdot k2\_33 + \text{CycE} \cdot k2\_32)) - \text{CA} \cdot \text{CDc}_20 \cdot k2\_22 - \text{CA} \cdot k2\_17 \quad (1.116)$$

$$\frac{d(\text{CD})}{dt} = \text{CycD} \cdot k2\_10 \cdot p27 - \text{CD} \cdot k2\_11 - \text{CD} \cdot (k2\_30 + k2\_31 \cdot (\text{CycA} \cdot k2\_34 + \text{CycB} \cdot k2\_33 + \text{CycE} \cdot k2\_32)) - \text{CD} \cdot k2\_9 \quad (1.117)$$

$$\frac{d(\text{CDc}_20)}{dt} = -\text{CDc}_20 \cdot k2.63 - \frac{\text{CDc}_20 \cdot k2.65}{\text{CDc}_20 + k2.67} - \frac{\text{IEP} \cdot k2.64 \cdot (\text{CDc}_20 - \text{CDc}20\text{T})}{\text{CDc}20\text{T} - \text{CDc}_20 + k2.66} \quad (1.118)$$

$$\frac{d(\text{CDc}20\text{T})}{dt} = k2.77 \cdot (k2.61 + \text{CycB} \cdot k2.62) - \text{CDc}20\text{T} \cdot k2.63 \quad (1.119)$$

$$\begin{aligned} \frac{d(\text{CE})}{dt} = & \text{CycE} \cdot k2.16 \cdot p27 - \text{CE} \cdot k2.17 - \text{CE} \cdot (k2.30 + k2.31 \cdot (\text{CycA} \cdot k2.34 + \text{CycB} \cdot k2.33 + \text{CycE} \cdot k2.32)) \\ & - \text{CE} \cdot \left( k2.14 + \frac{k2.15 \cdot (\text{CycB} \cdot k2.20 + k2.19 \cdot (\text{CycA} + \text{CycE}))}{\text{CE} + \text{CycE} + k2.18} \right) \end{aligned} \quad (1.120)$$

$$\frac{d(\text{GM})}{dt} = \text{expr}_2 - \text{GM} \cdot k2.75 \quad (1.121)$$

$$\frac{d(\text{IEP})}{dt} = -\frac{\text{CycB} \cdot k2.57 \cdot (\text{IEP} - 1)}{k2.59 - \text{IEP} + 1} - \frac{\text{IEP} \cdot \text{PPX} \cdot k2.58}{\text{IEP} + k2.60} \quad (1.122)$$

$$\frac{d(\text{Mass})}{dt} = \text{GM} \cdot k2.76 \cdot k2.77 - \text{Mass} \cdot k2.84 \quad (1.123)$$

$$\begin{aligned} \frac{d(p27)}{dt} = & \text{CE} \cdot \left( k2.14 + \frac{k2.15 \cdot (\text{CycB} \cdot k2.20 + k2.19 \cdot (\text{CycA} + \text{CycE}))}{\text{CE} + \text{CycE} + k2.18} \right) + \text{CA} \cdot k2.17 + \text{CD} \cdot k2.9 + \text{CD} \cdot k2.11 + \text{CE} \\ & \cdot k2.17 + k2.29 \cdot k2.77 - p27 \cdot (k2.30 + k2.31 \cdot (\text{CycA} \cdot k2.34 + \text{CycB} \cdot k2.33 + \text{CycE} \cdot k2.32)) \\ & + \text{CA} \cdot \text{CDc}_20 \cdot k2.22 - \text{CycD} \cdot k2.10 \cdot p27 - \text{CycA} \cdot k2.16 \cdot p27 - \text{CycE} \cdot k2.16 \cdot p27 \end{aligned} \quad (1.124)$$

$$\frac{d(\text{PPX})}{dt} = k2.55 \cdot k2.77 - \text{PPX} \cdot k2.56 \quad (1.125)$$

$$\begin{aligned} \frac{d(\text{ppRb})}{dt} = & \text{E2FRb} \cdot k2.40 \cdot (\text{CycA} \cdot k2.39 + \text{CycB} \cdot k2.38 + \text{CycE} \cdot k2.37 + k2.36 \cdot (\text{CD} + \text{CycD})) - \text{ppRb} \cdot \left( k2.41 \right. \\ & \cdot \left( k2.44 - \frac{k2.44}{k2.43 \cdot (\text{CycB} \cdot k2.46 + k2.45 \cdot (\text{CycA} + \text{CycE})) + 1} \right) + \frac{k2.42 \cdot k2.44}{k2.43 \cdot (\text{CycB} \cdot k2.46 + k2.45 \cdot (\text{CycA} + \text{CycE})) + 1} \left. \right) \\ & + \text{Rb} \cdot k2.40 \cdot (\text{CycA} \cdot k2.39 + \text{CycB} \cdot k2.38 + \text{CycE} \cdot k2.37 + k2.36 \cdot (\text{CD} + \text{CycD})) + k2.40 \\ & \cdot \text{pE2FRb} \cdot (\text{CycA} \cdot k2.39 + \text{CycB} \cdot k2.38 + \text{CycE} \cdot k2.37 + k2.36 \cdot (\text{CD} + \text{CycD})) \end{aligned} \quad (1.126)$$

$$\begin{aligned} \frac{d(E2F)}{dt} = & E2FRb \cdot k_{2.73} - E2F \cdot (k_{2.70} + k_{2.71} \cdot (CycA + CycB)) + k_{2.69} \cdot pE2F + E2FRb \cdot k_{2.40} \\ & \cdot (CycA \cdot k_{2.39} + CycB \cdot k_{2.38} + CycE \cdot k_{2.37} + k_{2.36} \cdot (CD + CycD)) - E2F \cdot Rb \cdot k_{2.72} \end{aligned} \quad (1.127)$$

$$\begin{aligned} \frac{d(pE2F)}{dt} = & E2F \cdot (k_{2.70} + k_{2.71} \cdot (CycA + CycB)) - k_{2.69} \cdot pE2F + k_{2.73} \cdot pE2FRb + k_{2.40} \cdot pE2FRb \\ & \cdot (CycA \cdot k_{2.39} + CycB \cdot k_{2.38} + CycE \cdot k_{2.37} + k_{2.36} \cdot (CD + CycD)) - Rb \cdot k_{2.72} \cdot pE2F \end{aligned} \quad (1.128)$$

$$\begin{aligned} \frac{d(Rb)}{dt} = & E2FRb \cdot k_{2.73} + ppRb \cdot \left( k_{2.41} \cdot \left( k_{2.44} - \frac{k_{2.44}}{k_{2.43} \cdot (CycB \cdot k_{2.46} + k_{2.45} \cdot (CycA + CycE)) + 1} \right) \right. \\ & \left. + \frac{k_{2.42} \cdot k_{2.44}}{k_{2.43} \cdot (CycB \cdot k_{2.46} + k_{2.45} \cdot (CycA + CycE)) + 1} \right) + k_{2.73} \cdot pE2FRb - Rb \cdot k_{2.40} \\ & \cdot (CycA \cdot k_{2.39} + CycB \cdot k_{2.38} + CycE \cdot k_{2.37} + k_{2.36} \cdot (CD + CycD)) - E2F \cdot Rb \cdot k_{2.72} - Rb \cdot k_{2.72} \cdot pE2F \end{aligned} \quad (1.129)$$

$$\begin{aligned} \frac{d(E2FRb)}{dt} = & k_{2.69} \cdot pE2FRb - E2FRb \cdot (k_{2.70} + k_{2.71} \cdot (CycA + CycB)) - E2FRb \cdot k_{2.73} - E2FRb \cdot k_{2.40} \\ & \cdot (CycA \cdot k_{2.39} + CycB \cdot k_{2.38} + CycE \cdot k_{2.37} + k_{2.36} \cdot (CD + CycD)) + E2F \cdot Rb \cdot k_{2.72} \end{aligned} \quad (1.130)$$

$$\begin{aligned} \frac{d(pE2FRb)}{dt} = & E2FRb \cdot (k_{2.70} + k_{2.71} \cdot (CycA + CycB)) - k_{2.69} \cdot pE2FRb - k_{2.73} \cdot pE2FRb - k_{2.40} \cdot pE2FRb \\ & \cdot (CycA \cdot k_{2.39} + CycB \cdot k_{2.38} + CycE \cdot k_{2.37} + k_{2.36} \cdot (CD + CycD)) + Rb \cdot k_{2.72} \cdot pE2F \end{aligned} \quad (1.131)$$

$$\frac{d(Growth)}{dt} = MYC \cdot k_{2.82} - Growth \cdot k_{2.83} \quad (1.132)$$

$$\begin{aligned} \frac{d(\text{MYC})}{dt} &= \text{ke\_myc} - \text{MYC} \cdot \text{k2\_86} + \text{k2\_85} \\ &\cdot \left( \frac{0.9900 \cdot (\text{A50n} \cdot \text{kp\_NM} + \text{C50n} \cdot \text{kp\_NM} + \text{kp\_mtb} \cdot \text{otherTFs\_activity} + \text{kmtb\_off} \cdot \text{kp\_PMBC} \cdot \text{otherTFs\_activity})^2}{\text{MYC\_THRESHOLD}^2 \cdot \left( \frac{(\text{A50n} \cdot \text{kp\_NM} + \text{C50n} \cdot \text{kp\_NM} + \text{kp\_mtb} \cdot \text{otherTFs\_activity} + \text{kmtb\_off} \cdot \text{kp\_PMBC} \cdot \text{otherTFs\_activity})^2}{\text{MYC\_THRESHOLD}^2} + 1 \right)} \right. \\ &\quad \left. + 0.0100 \right) \end{aligned} \quad (1.133)$$

$$\begin{aligned} \frac{d(\text{IRF})}{dt} &= \frac{\text{kASC\_16}^{\text{kASC\_17}} \cdot \left( \text{kASC\_15} + \frac{\text{A50n}^{\text{kASC\_13}} \cdot \text{kASC\_11} \cdot \text{kASC\_12}}{40 \cdot \text{A50n}^{\text{kASC\_13}} + 40 \cdot (50 \cdot \text{kASC\_11})^{\text{kASC\_13}}} + \frac{\text{C50n}^{\text{kASC\_13}} \cdot \text{kASC\_11} \cdot \text{kASC\_12}}{40 \cdot \text{C50n}^{\text{kASC\_13}} + 40 \cdot (3 \cdot \text{kASC\_11})^{\text{kASC\_13}}} + \frac{\text{Blimp\_1}^{\text{kASC\_13}} \cdot \text{kASC\_11} \cdot \text{kASC\_12}}{3 \cdot (\text{kASC\_11} \cdot \text{kASC\_14})^{\text{kASC\_13}} + 3 \cdot \text{Blimp\_1}^{\text{kASC\_13}}} \right)}{\text{kASC\_16}^{\text{kASC\_17}} + 0^{\text{kASC\_17}}} \\ &- \text{IRF} \cdot \text{kASC\_18} \end{aligned} \quad (1.134)$$

$$\frac{d(\text{Blimp\_1})}{dt} = \frac{\text{kASC\_26}^{\text{kASC\_27}} \cdot \left( \frac{\text{A50n}^{\text{kASC\_23}} \cdot \text{kASC\_21} \cdot \text{kASC\_22}}{\text{A50n}^{\text{kASC\_23}} + (50 \cdot \text{kASC\_21})^{\text{kASC\_23}}} + \frac{\text{IRF}^{\text{kASC\_23}} \cdot \text{kASC\_21} \cdot \text{kASC\_22} \cdot \text{kirfmut}}{(\text{kASC\_21} \cdot \text{kASC\_24})^{\text{kASC\_23}} + \text{IRF}^{\text{kASC\_23}}} \right)}{\text{kASC\_26}^{\text{kASC\_27}} + (\text{Bcl} \cdot \text{k\_bclRep2})^{\text{kASC\_27}}} - \text{Blimp\_1} \cdot \text{kASC\_28} \quad (1.135)$$

$$\frac{d(\text{Pax\_5})}{dt} = \frac{\text{kASC\_35} \cdot \text{kASC\_36}^{\text{kASC\_37}}}{\text{Blimp\_1}^{\text{kASC\_37}} + \text{kASC\_36}^{\text{kASC\_37}}} - \text{Pax\_5} \cdot \text{kASC\_38} \quad (1.136)$$

$$\frac{d(\text{Bcl})}{dt} = \text{ke\_bcl6} - \text{Bcl} \cdot \text{kASC\_48} + \frac{\text{kASC\_46}^{\text{kASC\_47}} \cdot \left( \frac{\text{C50n}^{\text{kASC\_43}} \cdot \text{kASC\_41} \cdot \text{kASC\_42}}{\text{C50n}^{\text{kASC\_43}} + (3 \cdot \text{kASC\_41})^{\text{kASC\_43}}} + \frac{\text{kASC\_41} \cdot \text{kASC\_42} \cdot (\text{Pax\_5} \cdot \text{kpax5mut})^{\text{kASC\_43}}}{(\text{kASC\_41} \cdot \text{kASC\_44})^{\text{kASC\_43}} + (\text{Pax\_5} \cdot \text{kpax5mut})^{\text{kASC\_43}}} \right)}{\text{kASC\_46}^{\text{kASC\_47}} + \text{Blimp\_1}^{\text{kASC\_47}} \cdot \text{k\_bclRep} + \text{IRF}^{\text{kASC\_47}} \cdot \text{k\_bclRep} \cdot \text{kirfmut}} \quad (1.137)$$

$$\begin{aligned} \frac{d(\text{Aid})}{dt} &= \frac{\text{kASC\_56}^{\text{kASC\_57}} \cdot \left( \frac{\text{A50n}^{\text{kASC\_53}} \cdot \text{kASC\_51} \cdot \text{kASC\_52}}{\text{A50n}^{\text{kASC\_53}} + (50 \cdot \text{kASC\_51})^{\text{kASC\_53}}} + \frac{\text{C50n}^{\text{kASC\_53}} \cdot \text{kASC\_51} \cdot \text{kASC\_52}}{\text{C50n}^{\text{kASC\_53}} + (3 \cdot \text{kASC\_51})^{\text{kASC\_53}}} + \frac{\text{kASC\_51} \cdot \text{kASC\_52} \cdot \text{kirfmut} \cdot \text{kpax5mut} \cdot (\text{IRF} \cdot \text{Pax\_5}^2)^{\text{kASC\_53}}}{(\text{kASC\_51} \cdot \text{kASC\_54})^{\text{kASC\_53}} + (\text{IRF} \cdot \text{Pax\_5}^2)^{\text{kASC\_53}}} \right)}{\text{kASC\_56}^{\text{kASC\_57}} + 0^{\text{kASC\_57}}} \\ &- \text{Aid} \cdot \text{kASC\_58} \end{aligned} \quad (1.138)$$

$$\frac{d(\text{tpre\_IkBe1})}{dt} = \frac{\text{pii}_{13} \cdot \left( \text{pdi}_{723} \cdot \left( \frac{\text{A50n}}{\text{pii}_{103}} \right)^{\text{pii}_{93}} + \text{pdi}_{713} \cdot \left( \frac{\text{AAn}}{\text{pii}_{103}} \right)^{\text{pii}_{93}} + \text{pdi}_{743} \cdot \left( \frac{\text{C50n}}{\text{pii}_{103}} \right)^{\text{pii}_{93}} \right)}{\left( \frac{\text{A50n}}{\text{pii}_{103}} \right)^{\text{pii}_{93}} + \left( \frac{\text{AAn}}{\text{pii}_{103}} \right)^{\text{pii}_{93}} + \left( \frac{\text{C50n}}{\text{pii}_{103}} \right)^{\text{pii}_{93}} + 1} - \text{kdel}_{e1} \cdot \text{tpre\_IkBe1} \quad (1.139)$$

$$\frac{d(\text{tpre\_P501})}{dt} = \frac{\text{pm}_{12} \cdot \left( \text{pdm}_{122} \cdot \left( \frac{\text{A50n}}{\text{pm}_{82}} \right)^{\text{pm}_{72}} + \text{pdm}_{142} \cdot \left( \frac{\text{C50n}}{\text{pm}_{82}} \right)^{\text{pm}_{72}} \right)}{\left( \frac{\text{A50n}}{\text{pm}_{82}} \right)^{\text{pm}_{72}} + \left( \frac{\text{C50n}}{\text{pm}_{82}} \right)^{\text{pm}_{72}} + 1} - \text{kdel}_{p501} \cdot \text{tpre\_P501} \quad (1.140)$$

$$\frac{d(\text{tpre\_cRel1})}{dt} = \frac{\text{kASC}_{66}^{\text{kASC}_{67}} \cdot \text{pm}_{13} \cdot \left( \text{pdm}_{123} \cdot \left( \frac{\text{A50n}}{\text{pm}_{83}} \right)^{\text{pm}_{73}} + \text{pdm}_{143} \cdot \left( \frac{\text{C50n}}{\text{pm}_{83}} \right)^{\text{pm}_{73}} \right)}{(\text{Blimp}_1^{\text{kASC}_{67}} + \text{kASC}_{66}^{\text{kASC}_{67}}) \cdot \left( \left( \frac{\text{A50n}}{\text{pm}_{83}} \right)^{\text{pm}_{73}} + \left( \frac{\text{C50n}}{\text{pm}_{83}} \right)^{\text{pm}_{73}} + 1 \right)} - \text{kdel}_{crel1} \cdot \text{tpre\_cRel1} \quad (1.141)$$

$$\begin{aligned} \frac{d(\text{pIKK})}{dt} &= \frac{\text{kmtb}}{\text{kmtb} + \text{A20} \cdot \text{ka20mut}} + \frac{\text{ktlr}}{\text{ktlr} + \text{A20} \cdot \text{ka20mut}} - \text{pIKK} \cdot \text{pikk}_2 \\ &+ \frac{\text{kmtb}_{\text{off}} \cdot \text{pikk}_1}{\text{pikk}_1 + \text{A20} \cdot \text{ka20mut}} + \text{kmtb}_{\text{off}} \cdot \text{phase} \cdot \text{pikk}_3 \cdot e^{-\text{A20} \cdot \text{ka20mut}} \end{aligned} \quad (1.142)$$

$$\frac{d(tA20)}{dt} = \text{A50n} \cdot \text{pikk}_4 - \text{pikk}_5 \cdot tA20 \quad (1.143)$$

$$\frac{d(A20)}{dt} = \text{pikk}_6 \cdot tA20 - \text{A20} \cdot \text{pikk}_7 \quad (1.144)$$

$$\frac{d(\text{pAKT})}{dt} = \text{pakt}_1 - \text{pAKT} \cdot \text{pakt}_2 + \text{pakt}_3 \cdot \text{phase} \cdot e^{-\text{PTEN} \cdot \text{kpi3kmut}} \quad (1.145)$$

$$\frac{d(tPTEN)}{dt} = \text{pakt}_4 \cdot e^{-\text{A50n}} - \text{pakt}_5 \cdot tPTEN \quad (1.146)$$

$$\frac{d(\text{PTEN})}{dt} = \text{pakt}_6 \cdot tPTEN - \text{PTEN} \cdot \text{pakt}_7 \quad (1.147)$$

## 2 Definitions of expressions

$$expr\_1 = \left\{ \begin{array}{ll} \frac{((k2\_47+k2\_48 \cdot CDe20) \cdot (1-Cdh1))}{(k2\_49-Cdh1+1)}, & Cdh1 \leq 1 \\ 0, & Cdh1 > 1 \end{array} \right\} \quad (2.1)$$

$$expr\_2 = \left\{ \begin{array}{ll} k2\_74 \cdot (0.01 + 0.99 \cdot GrowthMultiplier \cdot GMgrowth), & \frac{numerator}{denominator} < 0.8 \\ k2\_74 \cdot 0.01, & otherwise \end{array} \right\} \quad (2.2)$$

$$expr\_3 = \left\{ \begin{array}{ll} k2\_77 \cdot k2\_21 \cdot E2F \cdot \max(0, (GrowthMultiplier \cdot (GM \cdot k2\_76 \cdot k2\_77 - Mass \cdot k2\_84) \cdot 30)), & Mass > 0.5 \\ 0, & otherwise \end{array} \right\} \quad (2.3)$$

$$expr\_4 = \left\{ \begin{array}{ll} \max(k2\_80 \cdot Bcl2Activity, \frac{k2\_80}{100}) & \\ \frac{k2\_80}{100}, & otherwise \end{array} \right\} \quad (2.4)$$

$$numerator = Rb + E2FRb + pE2FRb \quad (2.5)$$

$$denominator = numerator + ppRb \quad (2.6)$$

$$GMgrowth = (2.8 \cdot Mass^2)^{(-0.14 \cdot Mass^2)} \quad (2.7)$$

$$GrowthMultiplier = \frac{\left(\frac{Growth}{GROWTH\_THRESHOLD}\right)^2}{\left(1 + \frac{Growth}{GROWTH\_THRESHOLD}\right)^2} \quad (2.8)$$

$$BclNumerator = \left(\frac{0.3 \cdot A50n + 0.6 \cdot C50n + 0.1 \cdot otherTFs\_activity}{BCL2\_THRESHOLD}\right)^2 \quad (2.9)$$

$$Bcl2Activity = \frac{BclNumerator}{1 + BclNumerator} \cdot (1 - 0.01) + 0.01 \quad (2.10)$$

$$(2.11)$$