Combining photonic crystal and optical Monte Carlo simulations: implementation, validation and application in a positron emission tomography detector.

Combining Photonic Crystal and Optical Monte Carlo Simulations: Implementation, Validation and Application in a Positron Emission Tomography Detector

Christof Thalhammer, Johannes Breuer, Thorsten Führer, Alexandru Popescu, Harry Hedler, Thomas Walther, and Thoralf Niendorf

Abstract—This paper presents a novel approach towards incorporating photonic crystals (PhCs) into optical Monte Carlo (MC) simulations. This approach affords modeling the full diffractive nature of PhCs including their reflection and transmission behavior as well as the manipulation of the photon trajectories through light scattering. The main purpose of this tool is to study the impact of PhCs on the light yield and timing performance of scintillator-based detectors for positron emission tomography (PET). To this end, the PhCs are translated into look-up tables and implemented into the optical MC algorithm. Our simulations are validated in optical experiments using PhC samples fabricated with electron beam lithography. The experimental results indicate that the simulations match the measurements within the accuracy of the experiments. The application of the combined simulation technique to a PET detector module predicts an increase of the total light yield by up to 23% for PhC coatings versus the reference without PhCs. Timing calculations reveal an improvement of the coincident resolving time by up to 6%. The results underline the potential of PhCs to improve light yield and timing of PET detector modules.

Index Terms—Positron emission tomography (PET), Photonic Crystals, Monte Carlo simulations, coincident resolving time, timing resolution, PET detector.

I. INTRODUCTION

DETAILING the propagation and extraction of light in scintillator-based detectors used for positron emission tomography (PET) is beneficial to understand and enhance the total amount of light reaching the photosensor and the coincidence resolving time (CRT) [1]–[5]. Energy resolution and CRT are limited by insufficient light extraction from the scintillators [6]. If the photons are reflected many times from the scintillator exit face, the path length inside the scintillator is prolonged, hence increasing absorption losses. An efficient extraction of photons at their first incidence on the exit face is expected to improve the CRT because the timing is not exclusively defined by the total amount of detected photons, but also depends on their propagation time distribution [7]. Currently, photon extraction is limited by light trapping inside the scintillator due to total internal reflection (TIR) since common inorganic scintillators such as lutetium oxyorthosilicate (LSO) have a high refractive index \((n_{\text{LSO}} = 1.82)\) versus the optical glue \((n_{\text{Glue}} \approx 1.5)\) used to couple the scintillator and the photosensor [8]. Thin layers of photonic crystals (PhCs) bear the potential to reduce light trapping and increase the extraction efficiency from high index media [9]. PhC structures exhibit a periodically modulated refractive index with characteristic dimensions in the range of the wavelength of the incident light, thus acting like a diffraction grating that scatters impinging photons into various diffraction orders [10]. This effect can lead to the extraction of photons with shallow incident angles beyond the TIR threshold. First applications of PhC technology to inorganic scintillators showed improved light output and timing resolution for individual LSO crystals [7], [11].

Monte Carlo (MC) simulations are a powerful tool to study the propagation of scintillation photons in PET detectors using ray tracing algorithms based on geometric optics [1]–[3], [12]. Since these techniques are not capable of computing the diffractive effects of PhCs, an additional tool is required to solve Maxwell’s equations. For the combination of these two techniques, analytical models [8] or look-up tables containing the transmission coefficients with respect to the incident angle [6] were proposed. Apart from exhibiting a distinct transmission behavior, PhCs also manipulate the photon trajectories through light scattering into various diffraction orders which presents a limitation of previous approaches. Realizing this challenge, this work proposes the implementation of PhCs into optical MC simulations. This combined approach allows modeling the full diffractive nature of PhCs including their transmission characteristics and light scattering properties. The technique is validated in angle-resolved transmission measurements using PhC samples fabricated with electron beam lithography (EBL). The approach is then applied to study the impact of an optimized PhC configuration on the light yield and CRT of a state-of-the-art PET detector module.
II. MATERIALS AND METHODS

A. Implementation of PhCs into Optical Simulations

All optical MC simulations were conducted with the commercial software Zemax (Radiant Zemax, Redmond, WA, USA). To calculate the diffractive behavior of PhCs, GD-Calc (KJ Innovation, Santa Clara, CA, USA) was used which is based on the rigorous coupled-wave analysis [13]. In this approach, the PhC geometry is represented by a stack of layers that contain cuboids of a certain refractive index forming a periodic pattern (see Fig. 1). The algorithm solves Maxwell’s equations using a Fourier expansion of the electric field and yields scattering matrices $R$ and $T$. These matrices correlate the amplitudes and phases of the incident and diffracted electromagnetic waves and facilitate the calculation of the diffraction order efficiencies for any given polarization of the incident electromagnetic wave [14].

For the implementation, PhCs were translated into look-up tables (LUTs) that contain bins of incident angles $\theta$ and $\phi$ (see Fig. 1). The elevation angle $\theta$ ranges from 0° to 180° with $\theta$-values larger than 90° corresponding to photons that impinge on the PhC from the optical glue side instead of the scintillator side. Due to the symmetry of the PhC, the azimuth angle $\phi$ was varied from 0° to 30° for hexagonal and from 0° to 45° for orthogonal PhC gratings. For each pair of $\theta$ and $\phi$, the scattering matrices and wave vectors of all non-evanescent reflected and transmitted orders were calculated with GD-Calc and written into the LUT. To take into account the wavelength-dependent behavior of PhCs, this procedure was repeated for each wavelength of the spectrum of interest yielding a series of LUTs. The LUTs were included into a custom procedure based on a dynamic link library (DLL) written in the programming language C. The PhC coating was implemented into Zemax by assigning the DLL to a certain material interface in the ray tracing tool. For each photon hitting this interface, Zemax passes the direction cosines, polarization, and wavelength of the incident photon to the DLL, which utilizes this information in conjunction with the LUT entries to calculate the diffraction efficiencies. Interpreting these diffraction efficiencies as MC probabilities, a random number is used to decide between reflection and transmission and to select a certain order. Finally, the photon is returned to Zemax with the diffracted wave vector $\mathbf{k}'$ taken from the LUT for the selected order (see Fig. 2).

B. Experimental Validation of Transmission Characteristics

1) PhC Fabrication: PhC samples were fabricated with hexagonal and orthogonal grating symmetry. The bulk material of the PhCs was a 450 nm thick layer of electron beam resist ($n_{\text{Resist}} = 1.59$ at wavelength $\lambda = 405$ nm), which was spin-coated on a glass substrate (Borofloat, $n_{\text{BF}} = 1.48$ at $\lambda = 405$ nm). The PhC structures were written directly into the resist layer by electron beam lithography (EBL) with a square shaped beam followed by wet development. The patterned area was $8 \text{ mm} \times 8 \text{ mm}$ per sample. Using EBL requires a conducting substrate to avoid charging effects. For this purpose, magnetron sputtering was used to deposit a 100 nm thick layer of tin-doped indium oxide (ITO, $n_{\text{ITO}} = 2.06$ at $\lambda = 405$ nm) on the glass substrate prior to spin-coating of the resist. Finally, the glass wafer was cut into individual chips using a dicing saw. The geometric parameters $a$, $s$, and $h$ (see Fig. 1) were chosen based on preliminary simulations with the goal to obtain diverse transmission characteristics with pronounced diffractive effects. To measure the actual geometric parameters of the fabricated PhCs, scanning electron microscopy (SEM) images were acquired.

2) Transmission Measurements: The angular transmission characteristics of the samples were measured with the experimental setup shown in Fig. 3a. In this setup, the samples were positioned in a holder providing a distance of 200 $\mu$m to a bare silicon photodiode (PD) with a sensitive area of $10 \text{ mm} \times 10 \text{ mm}$. The orientation of the samples was chosen so that the PhC coating was facing the sensor (see Fig. 3b). The sample was illuminated under various incident angles through a glass hemisphere ($n_{\text{HS}} = 1.82$ at $\lambda = 405$ nm) placed on top. A 700 $\mu$m thick film of Polydimethylsiloxan (PDMS, $n_{\text{PDMS}} = 1.45$ at $\lambda = 405$ nm) was used as optical coupling agent between sample and hemisphere. The sample holder was placed in a motorized goniometer which allowed the variation of the azimuth angle $\phi_L$. A laser diode module was mounted on the arm of the goniometer to vary the elevation angle $\theta_L$ of the light beam. The laser had a wavelength of 405 nm and was equipped with lenses and an aperture to provide a collimated beam with a Gaussian profile. Its full width at half maximum is FWHM = 400 $\mu$m. The polarization of the beam was adjusted using a half-wave plate. The lateral position of the sample and the PD was chosen off-center of the goniometer to account for the lateral displacement of the laser beam for $\theta_L > 0^\circ$. 

![Fig. 1. Schematic representation of a PhC coating within GD-Calc.](image-url)
Fig. 2. Schematic illustration of the custom-written DLL and its implementation into the ray tracing algorithm Zemax.

(see Fig. 3b). The incident angle $\theta_{\text{Sample}}$ on the sample/air interface and the elevation angle $\theta_L$ of the laser beam are correlated by Snell’s law via $\theta_{\text{Sample}} = \arcsin[\sin(\theta_L) \cdot n_{\text{HS}} / n_{\text{BF}}]$. This allows sweeping $\theta_{\text{Sample}}$ from 0° to 90° using a range for $\theta_L$ of 0° to 54.4°. A custom-written program controlled the goniometer movement and the laser power. The PD current was converted into voltage by a transimpedance amplifier and recorded by a computer equipped with an analog-to-digital converter as $U_{\text{Meas}}(\theta_L, \phi_L, p)$, where $p$ identifies the polarization state of the laser beam. The elevation angle $\theta_L$ was varied from 0° to 60° in 0.5°-increments, the azimuth angle $\phi_L$ ranged from 0° to 90° with 1°-increments. For each incident angle, measurements were performed using S- and P-polarization (electric field vector perpendicular or parallel to the plane of incidence). Each measurement was repeated 50 times with an individual duration of 28.5 ms at a laser output power of 5 mW, which led to a standard deviation below 0.1%.

3) Transmission Simulations: The experimental setup was simulated with the ray tracing tool. The profile of the laser beam was measured using a charge-coupled device camera and used to model a light source in the optical simulations. The polarization- and angle-dependent sensitivity of the photodiode was measured using the goniometer setup without sample and hemisphere. This characteristic was also implemented into the simulation model. Since scattering from impurities caused fluctuations in $U_{\text{Meas}}$ at some $\theta_L$-values, the average measured signal $U_{\text{Meas}}$ for $\theta_L < 3°$ was used to scale the simulated data instead of using only $\theta_L = 0°$. To estimate the accuracy of the computational model, a calibration experiment was conducted using a sample without PhC coating $\theta_{\text{Sample},2}$ larger than $\theta_{L,2}$.
coplanar and light scattering through electrical connections or mechanical fixations. The statistical error of the MC simulations was estimated through the standard deviation of the results from 10 repeated computations. It was found to be less than 0.1%, since $10^5$ photons were simulated per incident angle and polarization state. The calibration experiment was also used to estimate the accuracy of the goniometer setup $\Delta \theta$, regarding the calibration of $\theta$. For this purpose the TIR-related cutoff was located in the measured PD signal and compared to the position in the simulated signal with its intrinsically perfect accuracy in $\theta$. To evaluate $\Delta \phi$, i.e. the precision of the experiment regarding $\phi$, the locations of certain periodic features in measured and simulated PhC transmission characteristics were compared. Finally, the uncertainty $\gamma_{\text{Meas}}$ of the measured PD signal was determined by analyzing the variations of $U_{\text{Meas}}$ for changes $\pm \Delta \theta$ and $\pm \Delta \phi$. The results of this analysis are given in section III-B2. The agreement between $U_{\text{Meas}}$ and $U_{\text{Simu}}$ was analyzed using a two-sample Kolmogorov-Smirnov (KS) test [15]. In this procedure, a p-value is calculated based on the differences of two continuous distributions. The null hypothesis $H_0$, which states that the two functions stem from the same distribution, is rejected if the derived p-value is lower than the significance level $\alpha$. In this study, a KS test was conducted for all samples comparing the one-dimensional data sets $U_{\text{Meas}}(\theta_{L})$ and $U_{\text{Simu}}(\theta_{L})$ for fixed values of $\phi_{L}$ and $p$ at a significance level $\alpha = 0.05$. The results of this analysis are summarized in the agreement metric $\eta$, which is defined as the number of one-dimensional data sets for which $H_0$ was not rejected, divided by the total amount of data sets per sample.

C. Simulation Study of the Impact of PhCs on the Performance of a State-of-the-Art PET Detector

1) Detector Setup: The simulated PET detector consists of an array of 8×8 LSO scintillator crystals of the size 4 mm × 4 mm × 20 mm and a refractive index of $n_{\text{LSO}} = 1.82$ [12], [16] as depicted in Fig. 4. The LSO pixels were modeled as polished crystals with a Gaussian surface scattering coefficient of 0.02 rad. Bulk absorption and scattering are characterized by mean free paths of 600 mm and 250 mm [12]. The scintillator pixels are closely packed and separated from each other by thin air gaps. Due to limitations of the reflection models at rough surfaces in Zemax, these air gaps were chosen to be only 50 nm to approximate light transmission behavior from pixel to pixel. The array is surrounded on 5 sides by a 20 µm layer of air and specular reflective wrapping which has a reflection, transmission and absorption coefficient of 92%, 3%, and 5%, respectively. As for the pixel spacing, these parameters were chosen to match experimental results. On the bottom, the LSO array is coupled to an 8×8 array of silicon photomultipliers (SiPM) [17], [18] via a 100 µm layer of optical glue ($n_{\text{Glue}} = 1.47$) [12]. The SiPMs are modeled as bulk silicon material with a refractive index of 5.06 [19], which is encapsulated with a 300 µm thick epoxy window ($n_{\text{Epoxy}} = 1.59$) [20]. The SiPMs are equipped with a single layer antireflective coating based on a quarter wave film for 420 nm with a thickness of 37 nm and a refractive index of

![Image](314x512 to 561x735)

Fig. 4. Schematic view of the PET detector module used in the simulation study. The module includes an 8×8 array of LSO pixels, reflective wrapping, optical glue, and an array of 8×8 SiPMs with an epoxy window. (Dimensions are not to scale)

2) Optical Simulations: The software Geant4 [23] was used to calculate the interaction of gamma photons with the scintillator crystals (absorption length = 12 mm [16]). For this, a monoenergetic gamma source was simulated, which produced 511 keV photons that were uniformly distributed over the entrance face of the LSO crystals and entered the scintillators perpendicularly. The locations of energy deposition of 4000 gamma photons were listed and transferred to Zemax as coordinates of the scintillation light sources. The scintillation light is assumed to be emitted isotropic and randomly polarized. As explained above, the PhC DLL analyzes the polarization of each photon to calculate the diffraction efficiencies. Hence, the incidence of randomly polarized photons onto a PhC leads to a transmission behavior that corresponds to the average of the S- and P-polarized PhC characteristics. The optical simulations in Zemax used a spectral distribution of the generated scintillation photons derived from sampling the LSO emission spectrum presented in [16] in 20 nm intervals from 380 nm to 600 nm. To pronounce the impact of the wavelength-dependent PhC behavior on the light yield and timing, dispersion effects of the optical properties of the detector components were neglected with the exception of the SiPMs. These were modeled to have a photon detection efficiency (PDE) as described by the vendor [20] with values ranging from 25% at $\lambda = 600$ nm up to 35% at $\lambda = 420$ nm. With $4 \cdot 10^6$ simulated scintillation photons the statistical error for the light yield, i.e. the fraction of all simulated photons reaching a photosensor, was below 0.1%. The results from
the MC computations were post-processed with Matlab (The Mathworks, Natick, MA, USA).

3) Timing Simulations: The timing resolution was estimated with a MC algorithm introduced by Breuer et al. [24], that uses the results from the optical simulations. This technique takes into account specific SiPM characteristics such as optical crosstalk, dark counts and afterpulsing. Also, the amplifier electronics and a leading edge discriminator are simulated in order to derive the CRT of the detector. For these simulations, data of a commercially available SiPM was used [20], with a cross talk probability of 27%, a dark count rate of 100 kcps/mm², an afterpulsing probability of 40%, an overvoltage of 2.5 V, a peak PDE of 35%, and a single photon timing resolution of 230 ps. For each detector configuration, the discriminator threshold was optimized to obtain the minimum possible CRT. The timing simulations used $10^5$ gamma events, which resulted in a statistical error of the CRT below 0.5 ps.

4) Optimization of PhCs: The transmission characteristic of a PhC is influenced by its geometry and the refractive indices of its constituents. Together with the angular distribution of photons incident on the PhC, it defines the extraction efficiency which is the fraction of the extracted light relative to the number of incident photons. The angular distribution derived from the optical simulations for the reference setup was used in conjunction with a sweep of the geometry parameters $a$, $s$ and $h$ (see Fig. 1) to obtain optimized PhC configurations with a high extraction efficiency. Preliminary simulations and the results presented in [8], [25] show that a bulk material with a high refractive index and strong index modulation within the PhC yields the strongest diffraction effects. Hence, the PhC was modeled to consist of a high index polymer ($n_{\text{Polymer}} = 2.09$ at $\lambda = 420$ nm [26]) with air cavities.

III. RESULTS AND DISCUSSION

A. Implementation of PhCs into Optical Simulations

For each PhC configuration, the corresponding LUTs were calculated prior to their implementation. The maximum number of $(\theta_L, \phi_L)$-pairs was 16 200 per wavelength ($\theta_L$ from $0^\circ$ to $180^\circ$ with $0.5^\circ$ increment; $\phi_L$ from $0^\circ$ to $45^\circ$ with $1^\circ$ increment). This required a mean computation time of 45 s per $(\theta_L, \phi_L)$-pair using a computer equipped with a dual core processor (Intel Core2Duo E8400, 3 GHz). The implementation of the PhC DLL into the optical simulations causes an increase in the ray tracing computation time by up to 50% per invocation. The impact on the total simulation time for more complex models strongly depends on the geometry, the number of photon-PhC interactions, and the lengths of the individual photon trajectories. In this work, the simulation time for the PET detector module was reduced by up to 30% for configurations using PhCs due to attenuated light trapping which led to shorter photon paths.

B. Experimental Validation of Transmission Characteristics

1) PhC Fabrication: Five different PhC samples were fabricated, two with a hexagonal and three with an orthogonal grating symmetry. A summary of the specified geometry parameters and their values confirmed with SEM is surveyed in Table I. The measured values for the pitch $a$ differ from the specifications by 3% or less. The cavity size $s$ deviates by up to 17% (O1), which is significantly larger than the expected accuracy of a few nanometers. This stems from inaccuracies in the adjustment of the EBL focus plane, which were caused by the transparency of the substrate. For the same reason, the cavities shown in the SEM images in Fig. 5 have a rather round geometry although a quadratic electron beam was used. Variations of the PhC bulk thickness $h$ were negligible.

2) Comparison between Transmission Measurements and Simulations: The calibration using a sample without PhC coating indicates that the relative difference between measured and simulated PD signals varies only weakly with $\phi_L$ and the polarization. The largest discrepancies are observed at $\theta_L$-values close to the TIR-cutoff. In this region, the division by very small PD voltages can lead to relative differences of up to 90%. The mean difference is $7\% \pm 1\%$, which leads to an uncertainty of the simulations $\gamma_{\text{Simu}}$ of 8%. Fig. 6 shows the comparison of the measured and simulated calibration experiment for S- and P-polarization. Since the sample had no PhC coating, TIR was expected to occur at $\theta_L = 33^\circ$ which is the critical angle for the extraction of light from the glass hemisphere into air. This is clearly exemplified by the sharp cutoff in the PD voltage curve shown in Fig. 6.

After this calibration, transmission measurements of the PhC samples were performed. The LUTs corresponding to the PhC samples were calculated for a single wavelength of 405 nm using the geometry parameters from the SEM investigations. These computations also took into account the presence of the ITO layer between substrate and resist, which

![Fig. 5. SEM images of PhC samples O2 (a) and H1 (b) written into the electron beam resist. The images illustrate the rounding of the cavities due to the misalignment of the electron beam focus. The image in (a) was taken from a perpendicular perspective, whereas the perspective is tilted by 20° in (b).](image)

### Table I

<table>
<thead>
<tr>
<th>Sample name</th>
<th>Grating symmetry</th>
<th>$a_{\text{Spec}}$ in nm</th>
<th>$a_{\text{Meas}}$ in nm</th>
<th>$s_{\text{Spec}}$ in nm</th>
<th>$s_{\text{Meas}}$ in nm</th>
<th>Agreement metric $\eta$</th>
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<td>H1</td>
<td>Hex.</td>
<td>798</td>
<td>793±4</td>
<td>463</td>
<td>506±20</td>
<td>71%</td>
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<tr>
<td>H2</td>
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<tr>
<td>O1</td>
<td>Orth.</td>
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<td>670±6</td>
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<td>379±10</td>
<td>73%</td>
</tr>
<tr>
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<td>584±7</td>
<td>282</td>
<td>325±12</td>
<td>71%</td>
</tr>
<tr>
<td>O3</td>
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<td>290</td>
<td>299±9</td>
<td>77%</td>
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was found to have only minor impact on the transmission properties of the samples. Subsequently, the samples were included into the MC simulations using the DLL-based approach. The periodic transmission behavior of the PhC samples was used to determine $\Delta \phi_L$. The data acquired with a sampling increment for $\phi_L$ of $1^\circ$ reveals no misalignment which leads to a value of $1^\circ$ for $\Delta \phi_L$. Based on the agreement of the simulated and measured cutoff angle in Fig. 6, $\Delta \theta_L$, is estimated to be $0.5^\circ$ which is the sampling increment for $\theta_L$ of the experiment. Analyzing the variation of $U_{\text{Meas}}$ for changes of $\pm \Delta \theta_L$ and $\pm \Delta \phi_L$ yields an uncertainty $\gamma_{\text{Meas}}$ of 7%.

The simulations were found to be in good agreement with the measured characteristics as illustrated in Fig. 7. Distinct features such as peaks and dips can be reproduced by the simulations. The statistical analysis revealed that 71% or more of the data exhibited no significant difference between simulation and experiment as detailed through the agreement metric $\eta$ in Table I. These results indicate that the DLL-based approach of integrating PhCs into MC computations is suitable for detailing light propagation in a PhC enhanced PET detector module. Besides the validation of the simulation techniques, the results also prove that PhCs exhibit a transmission behavior different from plain interfaces (see Fig. 7c). On the one hand, the PD voltage for $\theta_L = 0^\circ$ is up to 25% lower versus the plain surface of the calibration sample. On the other hand, there is no TIR-related cutoff at $\theta_L = 33^\circ$. Instead, the transmission coefficient gradually decreases to zero up to an elevation angle $\theta_L$ of $52^\circ$, which corresponds to an incident angle on the sample of $\theta_{\text{Sample}} = 76^\circ$. Larger values for $\theta_{\text{Sample}}$ could not be studied due to the finite size of the PhC sample and the limited active area of the PD. The complete transmission data of sample H1 is depicted in Fig. 7d and shows the agreement between measurements and simulations for the entire $\phi_L$-range. Also, the $60^\circ$-periodic characteristic of the hexagonal sample can be clearly identified.

C. Simulation Study of the Impact of PhCs on the Performance of a State-of-the-Art PET Detector

The results derived from the validation of the PhC characteristics affords optical MC simulations of PhC enhanced PET detector modules and benchmarking against the reference module which has no PhC coating. For the reference setup these calculations yield $3.42 \times 10^6$ scintillation photons that impinge on the LSO exit face at least once. Of these photons $1.61 \times 10^6$ are extracted at the first incidence yielding an extraction efficiency of 0.472. The total amount of photons registered by the SiPMs is $1.02 \times 10^6$ which results in a reference light yield of 0.255. The remaining photons are lost through absorption in the LSO bulk, the reflective wrapping, the inactive SiPM areas, or by escaping from the $8 \times 8$ array. The timing simulation yields a CRT of 244 ps.

The angular distribution shown in Fig. 8a was used for the optimization of two different PhC configurations, one with hexagonal symmetry ($C_H$) and one with orthogonal symmetry ($C_O$). This optimization also took into account the wavelength-dependent behavior of PhCs. The parameter sweeps indicate the highest extraction efficiencies for the parameters $a = 368$ nm, $s = 199$ nm, $h = 325$ nm ($C_H$) and $a = 554$ nm, $s = 288$ nm, $h = 300$ nm ($C_O$). The rather distinct spectral transmission characteristics of these configurations are depicted in Fig. 8b,c. The transmission coefficient of $C_O$ (see Fig. 8b) exhibits only minor changes over the spectrum whereas the characteristic of $C_H$ (see Fig. 8c) varies considerably with the wavelength. Nevertheless, the amount of extracted photons over the entire spectrum (see curves in Fig. 8a) exceeds the value of the reference setup for both configurations. The resulting extraction efficiencies at first incidence are 0.527 for $C_H$ and 0.515 for $C_O$, an increase by 12% and 9% in comparison to the reference setup.

The PET detector module was modified to obtain two new setups, one using the PhC coating $C_H$ at the interface LSO/glue, the other using $C_O$. In both cases, the PhC DLLs contained 12 LUTs, one for each wavelength of the considered LSO spectrum. The simulations of the two modules indicate a light yield of $0.314$ ($C_H$) and $0.313$ ($C_O$), an improvement by 23% versus the reference with no PhC coating. For both settings, the increases in light yield are larger than the improvements regarding the extraction efficiencies at first incidence due to the positive effect of the PhC accumulated over several recurrences of photons on the LSO exit face. This is because the setup of the detector module leads to little scattering of the scintillation light. For the reference configuration, those photons which have been reflected at their first incidence on the LSO exit face and return a second or third time tend to have a similar incident angle as before, leading to a low extraction efficiency (see Fig 8d). Unlike the reference configuration, PhCs transmit a broad spectrum of incident angles. Also, those photons which are not transmitted are scattered by the PhC upon their reflection, which causes broad spectra of incident angles (see Fig. 8e). This has an influence on the extraction efficiencies depicted in Fig. 8f,
Fig. 7. Measured and simulated PD voltage versus elevation angle $\theta_L$ for sample H2 at $\phi_L = 30^\circ$ (a), sample O1 at $\phi_L = 45^\circ$ (b), and sample O3 at $\phi_L = 90^\circ$ (c) for both polarizations. The curves illustrate the agreement between experiments and simulations. In (c), the measured transmission characteristic of the plain calibration sample is added for comparison. The curves show that PhCs have a lower transmission for small values of $\theta_L$ and do not exhibit TIR at $\theta_L = 33^\circ$. Error bars of simulated and measured data are displayed only at interleaved selected points for clarity. (d) PD voltage versus incident angles $\theta_L$ and $\phi_L$ for sample H1 comparing the measured and simulated data. The hexagonal symmetry of the PhC leads to a 60°-periodic pattern of the distribution.
Fig. 8. (a) Angle distribution of photons at first incidence on the LSO exit face and curves of extracted photons for the 3 different configurations. Spectral transmission characteristics of PhC configuration C₀ (b) and C₁ (c). Angle distributions of photons incident on the LSO exit face over 5 recurrences for the reference (d) and the PhC configuration C₀ (e). The PhC interface yields improved extraction efficiencies over several recurrences (f) which causes an accumulating positive effect for the total light yield.

which are defined as the number of extracted photons at a certain recurrence divided by the total amount of incident photons at this recurrence. The fact that PhC configurations exhibit higher extraction efficiencies compared to the reference over several recurrences leads to an accumulating positive effect.

The propagation time distribution of detected photons is shown in Fig. 9a for the three detector setups. As observed in the optical experiments, PhC coatings lead to a reduced transmission for photons with low incident angles. Since the fastest photons mostly correspond to direct incidence on the exit face with a low angle, the propagation time distribution of the reference setup exhibits a higher peak of the leading pulse than the curves obtained for C₁ and C₀ configurations. However, approximately 240 ps after the first detected photons, the accumulated light yield for the PhC configurations starts to exceed the reference setup (see dashed line in Fig. 9b). The timing simulations yield CRT values of 229 ps for C₁ and 232 ps for C₀ constituting an improvement by 6% and 5%, respectively. Although these values represent only modest changes, they are significantly larger than the inaccuracies of optical and timing simulations. According to the theory presented in [27], the gains in light yield obtained for configurations C₁ and C₀ should lead to an improvement of the CRT by 10%. This discrepancy stems from the slightly lower leading peaks in the photon propagation time distributions of the PhC configurations compared to the reference (see Fig. 9a). This leads to only modest improvements of the CRT, which suggest that the derived PhC configurations do not represent optimal solutions to enhance the timing performance. This shortcoming can potentially be corrected by using an optimization procedure for the PhC parameters that considers not only the total light extraction, but also takes into account the photon propagation times and their impact on the CRT.

IV. CONCLUSIONS AND OUTLOOK

This work demonstrates the implementation of photonic crystal simulations into optical MC simulations with the goal of detailing the diffractive nature of PhCs including transmission characteristics and light scattering properties. Combining photonic crystal and optical MC simulations allows modeling the impact of PhC coatings on the propagation of photons within complex geometries such as PET detector modules. The proposed approach was successfully validated by optical transmission measurements. The experimental results demonstrate that PhC coatings help to avoid a cutoff in transmission due to TIR and provide a non-zero transmission up to large incident angles. The simulation technique was used to incorporate an optimized PhC coating into a state-of-the-art PET detector module. Our results underline the potential of improving the total light yield and CRT by PhCs, although the reported values are more modest than the results presented in [7], [11]. However, care must be taken for comparing these results with our study, as they were derived for individual scintillators instead of an 8×8 array and used air instead of optical glue to couple the scintillator with the photosensor. With regard to the modest gains predicted for the CRT compared to the substantial improvements in light yield by PhCs, it is our goal...
to improve the optimization procedure to find configurations with increased timing performance. Also, the relatively low gains in CRT in relation to the high costs of using EBL for the PhC fabrication emphasizes the need for new production technologies that provide reduced costs and complexity. Hence, we anticipate to extend our studies to alternative fabrication procedures with the ultimate goal to provide a technique that is compatible with potential implementations in commercial PET detectors. To summarize, the proposed approach for implementing PhCs into an optical MC code is not restricted to a specific detector configuration and rather represents a versatile tool for modeling diffractive elements within the framework of suitable ray tracing software.

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